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Inflation in String Theory

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String Theorists Think Small



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Unification of elementary particles and forces!

Cosmologists Think **Big**



400 billion stars in our galaxy

Hubble Space Telescope



And ... there are many billions of galaxies in our universe.



What is String Cosmology?







Multiple Cosmological Probes



Precision Cosmology

Observational cosmology has given us a new window into our universe, complementary to particle physics experiments.



Quantitative info about our universe, both at its earliest moment and at the present time, but many puzzles remain.... e.g., the physics of inflation, dark matter & dark energy.

Inflation

Generic predictions of inflation are in excellent agreement with data, e.g., Cosmic Microwave Background:



History of the Universe



History of the Universe



History of the Universe



Cosmic Microwave Background



The CMB is homogeneous and isotropic to 1 part in 100,000.

Originally proposed as a solution to the flatness and horizon problems in standard big bang cosmology, inflation has emerged to be the leading paradigm for explaining the observed CMB anisotropies.

Quantum Fluctuations

36

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36

Quantum Fluctuations



Quantum fluctuations translate to perturbations in local energy density, & explains the measured temperature anisotropy: $\delta T/T$







> Tiny density perturbations grew under the influence of gravity



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Galaxies and structures are quantum effects writ large!



Inflation is an effective theory in search of a fundamental description!



Alan Guth



To solve the flatness & horizon problems, need to satisfy

"Slow-roll":
$$\epsilon = \frac{1}{2} M_P^2 \left(\frac{V'}{V}\right)^2 << 1$$
; $\eta = M_P^2 \frac{V''}{V} << 1$

These conditions are sensitive to **Planck scale physics**:

$$\delta V \sim \frac{V}{M_P^2} \phi^2 \quad \longrightarrow \quad \eta \sim \mathcal{O}(1)$$

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Effective Field Theory:

- Physics can be understood scale by scale.
- Short distance physics: "irrelevant operators".



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Examples:



BCS Theory of Superconductivity





Fermi theory of weak interaction

Particle Physics



Precision tests, such as those that constrain the proton lifetime, are sensitive to GUT scale physics

INFLATION & UV PHYSICS

A sufficient degree of UV completeness is needed to calculate such corrections.

This applies to <u>any</u> model of inflation.

Models with detectable non-Gaussianities and gravity waves are even more UV sensitive!

Any massless field experiences quantum fluctuations during inflation:



Inflation stretches these to macroscopic scales:



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Inflation stretches these to macroscopic scales:



Two massless fields that are guaranteed to exist are:

h_{ij}

graviton



Goldstone boson

of broken time translations

Two massless fields that are guaranteed to exist are:



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Planck scale 10⁻⁴³s

A distinguishing parameter is the tensor-to-scalar ratio r.



Many experiments including BICEP/KECK, PLANCK, ACT, PolarBeaR, SPT, SPIDER, QUEIT, Clover, EBEX, QUaD... can potentially detect such primordial B-mode if r≤10⁻².

LiteBIRD may even have the sensitivity to detect $r \sim 10^{-3}$.

B-mode and Inflation

If primordial B-mode is detected, natural interpretations:

Inflation took place

The energy scale of inflation is the GUT scale

$$E_{\rm inf} \simeq 0.75 \times \left(\frac{r}{0.1}\right)^{1/4} \times 10^{-2} M_{\rm Pl}$$

The inflaton field excursion was super-Planckian

$$\Delta \phi \gtrsim \left(\frac{r}{0.01}\right)^{1/2} M_{\rm Pl} \qquad \qquad \text{Lyth '96}$$

Great news for string theory due to strong UV sensitivity!

Super-Planckian Fields

Chaotic Inflation

Linde '86



Chaotic Inflation

Linde '86



Classical backreaction is under control.



Quantum corrections are small.

Concerns arise if we consider coupling the theory to the UV degrees of freedom of a putative theory of quantum gravity.



Large Field Inflation in String Theory

Large corrections, unless the inflaton couples weaker than gravitationally to everything else.

This even stronger UV sensitivity intrinsic to *large field inflation* should be explained in the UV-completion.

Controlling an *infinite number of corrections* seems hopeless.

Natural inflaton candidates are fields with symmetries.



"Symmetries dictate interactions"

Axions & Large Field Inflation

Pseudo-Nambu-Goldstone bosons are natural inflaton candidates:



Natural Inflation: [Freese, Frieman, Olinto]; Axion Monodromy: [McAllister Silverstein, Westphal]; [Marchesano, GS, Uranga]

Axions & Large Field Inflation

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Axions & Large field inflation

• Inflation with axion: $\Lambda^{(k)} \sim e^{-km}$, $m \sim \frac{1}{q^2}$

$$V(\phi) = 1 - \Lambda^{(1)} \cos\left(\frac{\phi}{f}\right) + \sum_{k>1} \Lambda^{(k)} \left[1 - \cos\left(\frac{k\phi}{f}\right)\right]$$



• Slow roll conditions imply

$$f > M_P$$
 $\frac{\Lambda^{(n+1)}}{\Lambda^{(n)}} \sim e^{-m} \ll 1 \Longrightarrow m \gtrsim 1$

Axions in String Theory

String theory has many **higher-dimensional form-fields**:

e.g. $F = \mathrm{d}A$ 3-form flux ______ 1 ____ 2-form gauge potential: gauge symmetry: $A \to A + \mathrm{d}\Lambda$

Integrating the 2-form over a 2-cycle gives an **axion**:

$$a(x) \equiv \int_{\Sigma_2} A$$

The gauge symmetry becomes a **shift symmetry**.

Axions with super-Planckian decay constants don't seem to exist in controlled limits of string theory. Svrcek and Witten

Banks et al.

Multiple Axions



- N-flation [Dimopoulos, Kachru, McGreevy, Wacker '05]
- Alignment [Kim, Nilles, Peloso '04];[Bachlechner, Long, McAllister, '14]
- Kinetic and Stuckelberg Mixings [GS, Staessens, Ye, '15]

seem to give f_{eff} > M_{p.} Can these models trick fool quantum gravity or they lie in the swampland?

Arkani-Hamed et al. '06

• The conjecture:

"Gravity is the Weakest Force"

• For every long range gauge field there exists a particle of charge q and mass m, s.t.

$$\frac{q}{m}M_P \ge ``1"$$

• Take a U(1) and a single family with q < m (WGC)



 $M_P \equiv 1$

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• Trouble with remnants

Susskind '95

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 $M_P \equiv 1$

• Need a light state into which they can decay

$$\frac{q}{m} \ge ``1" \equiv \frac{Q_{Ext}}{M_{Ext}}$$

Arkani-Hamed et al. '06

• The conjecture:

"Gravity is the Weakest Force"

• For a U (1) symmetry there must exist a particle with charge q and mass m such that

$$\frac{q}{m} \ge ``1" \equiv \frac{Q_{Ext}}{M_{Ext}}$$

Strong-WGC: satisfied by *lightest* charged particle Weak-WGC: satisfied by *any* charged particle

Convex Hull Condition

• For multiple U(1)'s and multiple charged particles, construct the vectors in charge space

$$\vec{z}_k = \frac{\vec{q}_k M_P}{m_k}$$

• Convex hull generated by the vectors $\pm \vec{z}_k$ must contain the ball of radius $|\vec{Z}|_{EBH}$ [Cheung et al, '14]



$\Delta x = \frac{hc}{E} + \frac{GE}{c^4}$ An equivalence between different universes:



T-duality: WGC for Axions

• Consider C₂ axions, canonically normalized as cⁱ

$$V \supset \sum_{k} \Lambda^4 e^{-m_k} \left(1 - \cos \left(\mathcal{Q}_k^i rac{c^i}{M_p}
ight)
ight)$$

 Compactify and T-dualize (c-map) Type 11A Type IIB Dp-D(p+1)-Particle Instanton (Gauge bosons) (Axíons) \mathbf{R}^{d} \mathbf{R}^d $\tilde{S}^1 \uparrow$ $\int S^1$ $\mathbf{R}^{d-1} \times S^{2}$ $\mathbf{R}^{d-1} \times \tilde{S}^1$

T-duality: WGC for Axions

[Brown,Cottrell, GS, Soler]

- Through this T-duality:
 - Axions \rightarrow U(1) gauge fields
 - Instantons → particles
- These particles are charged under U(1) symmetries

$$ec{z}_k = rac{ec{\mathcal{Q}}_k}{m_k}$$

• Considering EBH in the T-dual theory, the WGC states

The convex hull generated by \vec{z}_k must contain the ball of radius $2/\sqrt{3}$.

Apply WGC to Axion Inflation

• For a single axion and an instanton $Q=M_p/f$:

$$f \cdot m \leq \frac{\sqrt{3}}{2} M_p$$

• For multiple axions



Axion Monodromy



[McAllister, Silverstein and Westphal];[Marchesano, GS, Uranga]

Axion Monodromy Inflation



The axion periodicity is lifted, allowing for super-Planckian displacements. The UV corrections to the potential should still be constrained by the underlying symmetry.

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Axion Monodromy Inflation

• In string theory one may elegantly implement large field inflation by identifying the inflaton with an axion and applying the axion-monodromy proposal

Silverstein & Westphal'08

• String theory constructions using boundaries:

McAllister, Silverstein, Westphal'08 Berg, Pajer, Sjörs'09 Palti & Weigand'14





taken from McAllister, Silverstein, Westphal '08

F-term Axion Monodromy

Obs:

Giving a mass to an axíon

Marchesano, GS. Uranga'14

• Done in string theory within the moduli stabilisation program: adding ingredients like background fluxes generate superpotentials in the effective 4d theory

Use same techniques to generate an inflation potential Idea:

Axíon Monodromy



taken from Ibañez & Uranga '12

F-term Axion Monodromy Inflation





- Simpler models, all sectors understood at weak coupling
- Spontaneous SUSY breaking, no need for brane-anti-brane
- Supergravity description at small field, allows to connect with large field inflation models in SUGRA
- Realizes Kaloper-Sorbo 4d formalism in string theory

$$\int d^4x \, |dC_3|^2 + \frac{\mu^2}{k^2} |db_2 - kC_3|^2 \longrightarrow \int d^4x \, |F_4|^2 + |d\phi|^2 + \phi F_4$$

 $F_4 = dC_3$ Kaloper & Sorbo '08 $d\phi = *_4 db_2$ Kaloper, Lawrence, Sorbo '11
Example: (Massive) Wilson line

Simple example of axion: (4+d)-dimensional gauge field integrated over a circle in a compact space Π_d

$$\phi = \int_{S^1} A_1$$
 or $A_1 = \phi(x) \eta_1(y)$

- ϕ massless if $\Delta \eta_1 = 0 \Rightarrow S^1$ is a non-trivial circle in Π_d exact periodicity and (pert.) shift symmetry



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$$F_2 = dA_1 = \phi \, d\eta_1 \sim \mu \phi \, \omega_2 \quad \Rightarrow \text{ shifts in } \phi \text{ increase energy}$$

via the induced flux F₂

⇒ periodicity is broken and shift symmetry approximate

MWL and monodromy



Question:

How does monodromy and approximate shift symmetry help prevent wild UV corrections?

Torsion and gauge invariance

* Let us again consider a 7d gauge theory on $\rm M^{1,3}$ x $\tilde{\mathbb{T}}^3$

Instead of A₁ we consider its magnetic dual V₄

$$d\eta_1 = k \,\sigma_2$$

$$V_4 = C_3 \wedge \eta_1 + b_2 \wedge \sigma_2 \longrightarrow dV_4 = dC_3 \wedge \eta_1 + (db_2 - kC_3) \wedge \sigma_2$$

From dimensional reduction of the kinetic term:

$$\int d^7 x \, |dV_4|^2 \longrightarrow \left(\int d^4 x \, |dC_3|^2 + \frac{\mu^2}{k^2} |db_2 - kC_3|^2 \right)$$

- Gauge invariance $C_3 \rightarrow C_3 + d\Lambda_2$ $b_2 \rightarrow b_2 + k\Lambda_2$
- Shift symmetry is broken spontaneously

$$\int d^4x \, |F_4|^2 + |d\phi|^2 + \phi F_4 \qquad \qquad F_4 = dC_3 \\ d\phi = *_4 db_2$$

Torsion and gauge invariance

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- Gauge invariance $C_3 \rightarrow C_3 + d\Lambda_2$ $b_2 \rightarrow b_2 + k\Lambda_2$
- Shift symmetry is broken spontaneously

$$\int d^4x \, |F_4|^2 + |d\phi|^2 \left(\phi F_4\right) \qquad \begin{array}{c} F_4 = dC_3 \\ d\phi = *_4 db_2 \end{array}$$

an F-term when realized in SUGRA: "F-term axion monodromy" [Marchesano, GS, Uranga]

Effective 4d theory

Effective 4d Lagrangian

$$\int d^4x \, |dC_3|^2 + \frac{\mu^2}{k^2} |db_2 - kC_3|^2 \qquad F_4 = dC_3 \\ d\phi = *_4 db_2$$

Gauge symmetry UV corrections only depend on F₄

$$\mathcal{L}_{\text{eff}}[\phi] = \frac{1}{2} (\partial \phi)^2 - \frac{1}{2} \mu^2 \phi^2 + \Lambda^4 \sum_{i=1}^{\infty} c_i \frac{\phi^{2i}}{\Lambda^{2i}}$$
$$\sum_n c_n \frac{F^{2n}}{\Lambda^{4n}} \longrightarrow \mu^2 \phi^2 \sum_n c_n \left(\frac{\mu^2 \phi^2}{\Lambda^4}\right)^n$$

- \Rightarrow suppressed corrections up to the scale where V(ϕ) ~ Λ^4
- \Rightarrow effective scale for corrections $\Lambda \rightarrow \Lambda_{eff} = \Lambda^2/\mu$

Effective 4d theory

Effective 4d Lagrangian

$$\int d^4x \, |dC_3|^2 + \frac{\mu^2}{k^2} |db_2 - kC_3|^2 \qquad F_4 = dC_3 \\ d\phi = *_4 db_2$$

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Multi-branched Potential

Related to the torsional homologies of compactifications or Ktheory charges of fluxes.



Branch jumps are made via nucleation of domain walls that couple to C₃, and this puts a maximum to the inflaton range.

F-term Axion Monodromy Inflation

A wide variety of potentials (topology in the sky!):

$$V(\phi) \propto \phi, \phi^{2/3}, \phi^2, \dots, \text{ or even } V(\phi) = \sum_n c_n \phi^n \text{ with } n > 2$$

UV effects *flatten* the inflaton potential.

Resonant non-Gaussianity:



Non-Gaussianity

If Gaussian: completely specified $\langle \zeta(\mathbf{k}) \rangle = (2\pi)^3 \delta^3(\mathbf{k} + \mathbf{k}') P_s(k)$ The leading non-Gaussianity $\langle \zeta(\mathbf{k_1}) \zeta(\mathbf{k_2}) \zeta(\mathbf{k_3}) \rangle$ characterized by its size $\mathbf{f_{NL}}$ and \mathbf{shape} (functional form) Complete single field result: [Chen,Huang,Kachru, GS]

 $f_{NL}^{equil} \sim \mathcal{O}(\gamma^2)$

Equilateral shape:

 $f_{NL}^{local} \sim \mathcal{O}(\epsilon)$

Current bound [Planck]:

 $f_{NL}^{local} = 2.7 \pm 5.8$ $f_{NL}^{equil} = -42 \pm 75$

Large non-Gaussianity probes UV physics!

Local shape:

Holographic Non-Gaussianity

• Motivated partly by CHKS, various shape templates have been proposed:



• Inflation is approx. dS, holography may offer an organizing principle for NG:



$$\langle \zeta_{\mathbf{k}} \zeta_{-\mathbf{k}} \rangle' = -\frac{1}{2 \operatorname{Re} \langle \Theta_{\mathbf{k}} \Theta_{-\mathbf{k}} \rangle'}$$
$$\langle \zeta_{\mathbf{k}_{1}} \zeta_{\mathbf{k}_{2}} \zeta_{\mathbf{k}_{3}} \rangle' = \frac{2 \operatorname{Re} \langle \Theta_{\mathbf{k}_{1}} \Theta_{\mathbf{k}_{2}} \Theta_{\mathbf{k}_{3}} \rangle'}{\prod_{j=1}^{3} \left(-2 \operatorname{Re} \langle \Theta_{\mathbf{k}_{j}} \Theta_{-\mathbf{k}_{j}} \rangle' \right)}$$

[Maldacena]; [Schalm, GS, van der Aalst]

Inflation is a successful effective theory in search of a microscopic description.

* Superconductivity



Effective theory



Microscopic theory

* Weak Interaction





Microscopic theory

Many Candidates



A New Synergy





A New Synergy



Grdon Research Conferences

String Theory & Cosmology

New Ideas Meet New Experimental Data

May 31 - June 5, 2015 The Hong Kong University of Science and Technology Hong Kong, China

Chair: Gary Shiu

Vice Chair: Ulf Danielsson

Application Deadline

Applications for this meeting must be submitted by **May 3, 2015**. Please apply early, as some meetings become oversubscribed (full) before this deadline. If the meeting is oversubscribed, it will be stated here. *Note*: Applications for oversubscribed meetings will only be considered by the Conference Chair if more seats become available due to cancellations.

Gordon Research Conferences

G String Theory & Cosmology Gordon Research Conference

Dates

May 28 - June 2, 2017

Location

Renaissance Tuscany II Ciocco Lucca (Barga), Italy

Application Deadline

Organizers

Chair: **Ulf Danielsson**

Vice Chairs: Ben Wandelt & Savdeep Sethi

Applications for this meeting must be submitted by **April 30, 2017**. Please apply early, as some meetings become oversubscribed (full) before this deadline. If the meeting is oversubscribed, it will be stated here. *Note*: Applications for oversubscribed meetings will only be considered by the Conference Chair if more seats become available due to cancellations.

Check out the website: <u>https://www.grc.org/programs.aspx?id=16939</u> Meeting Description

Gordon Research Conferences



5/2/16, 11:47 AM



THANKS

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