

Probing millicharge @ electron colliders

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Millicharge is a very small electric charge

photon



$$e Q_f A_\mu^\gamma \bar{f} \gamma^\mu f$$

Millicharge is a very small electric charge

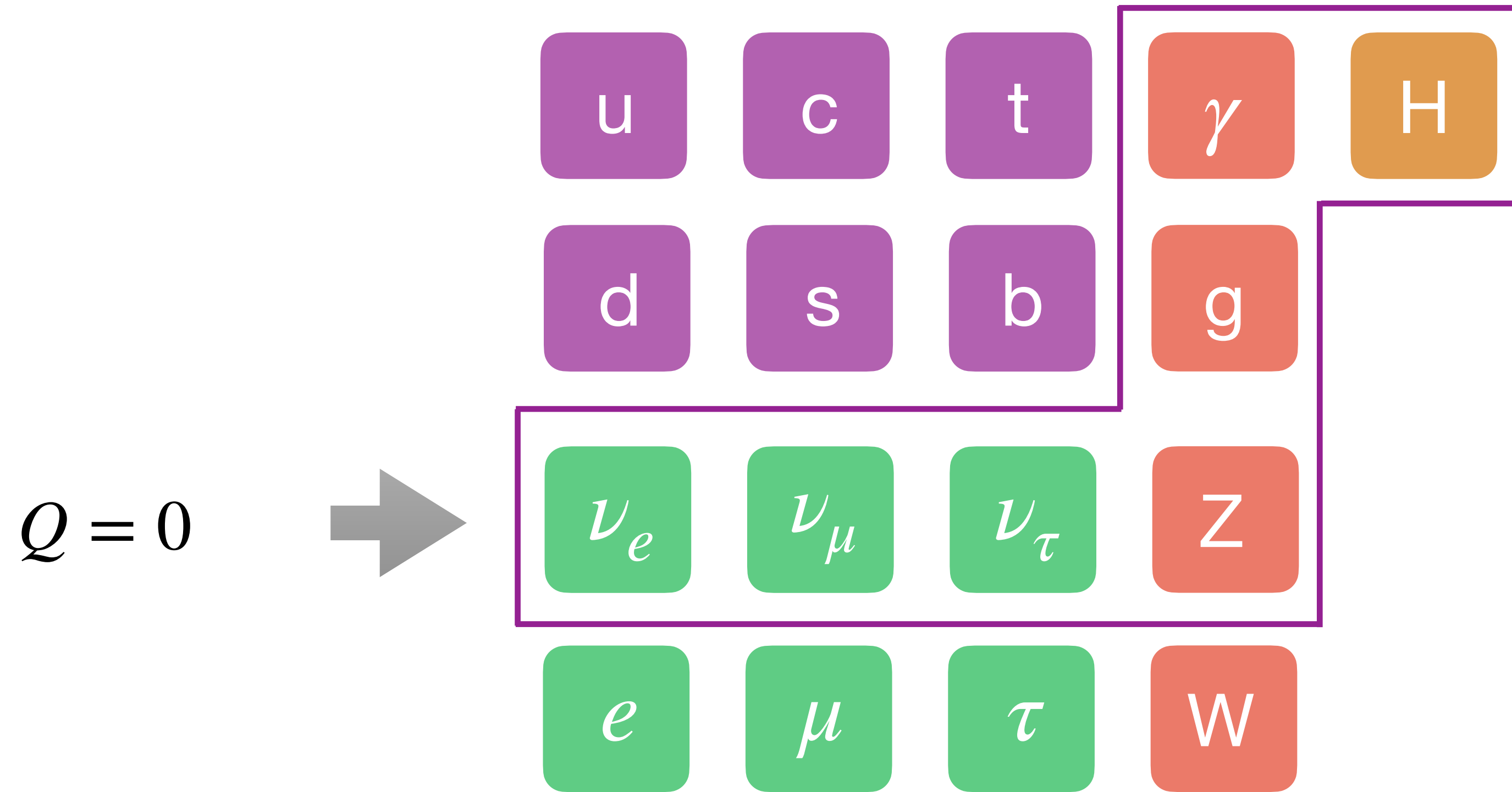


photon

↓

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Millicharge is a very small electric charge

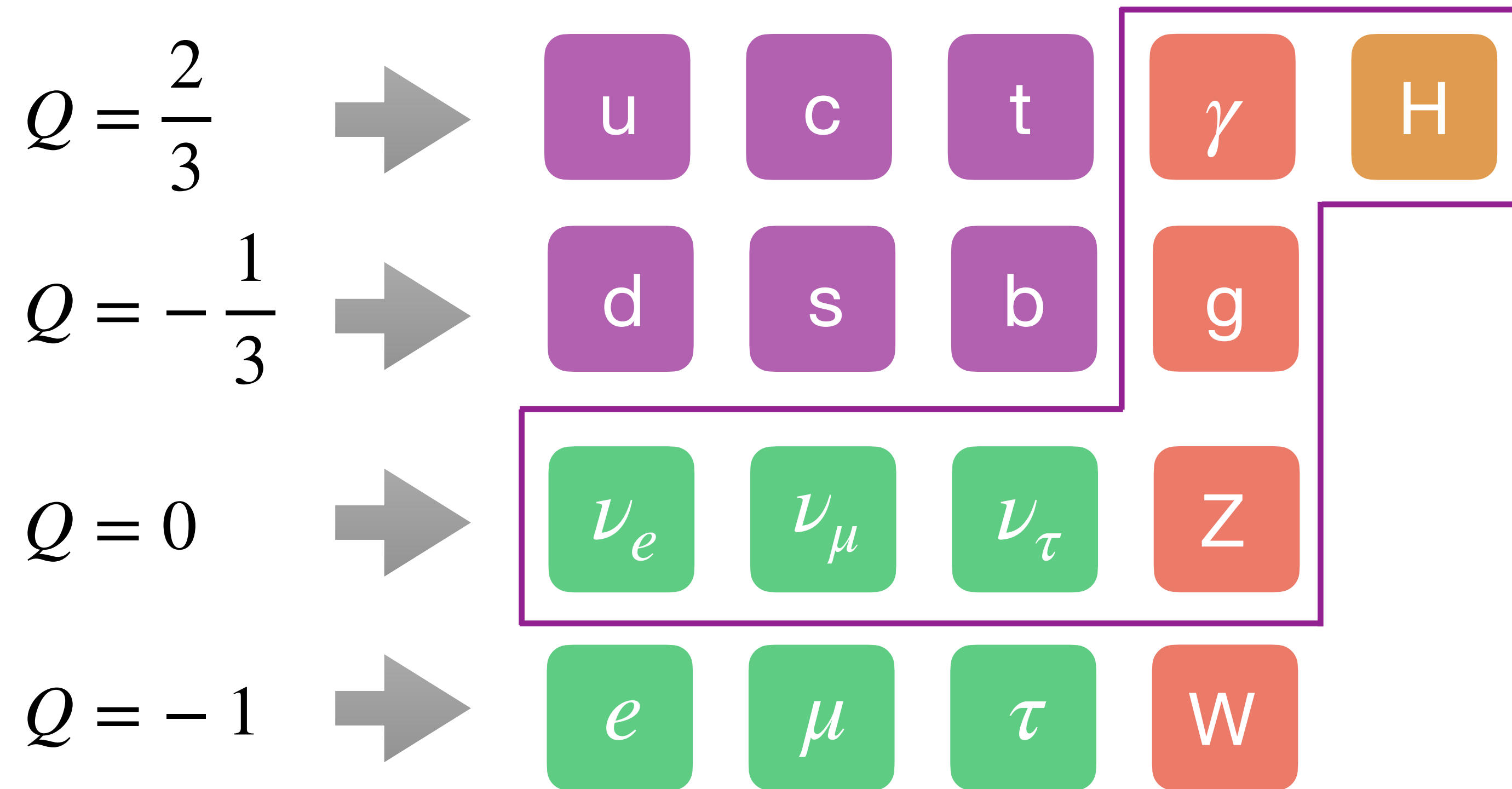


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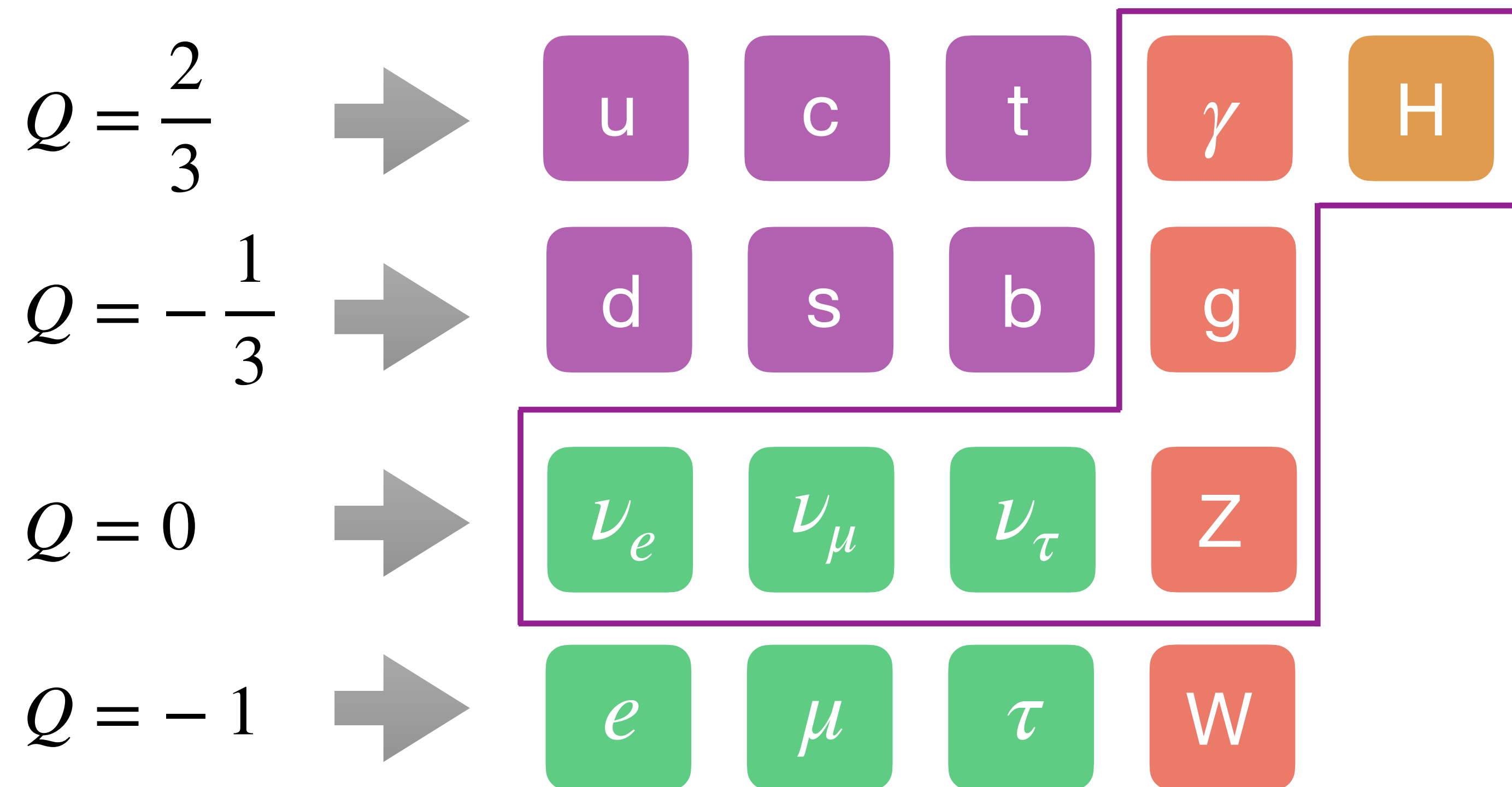


photon

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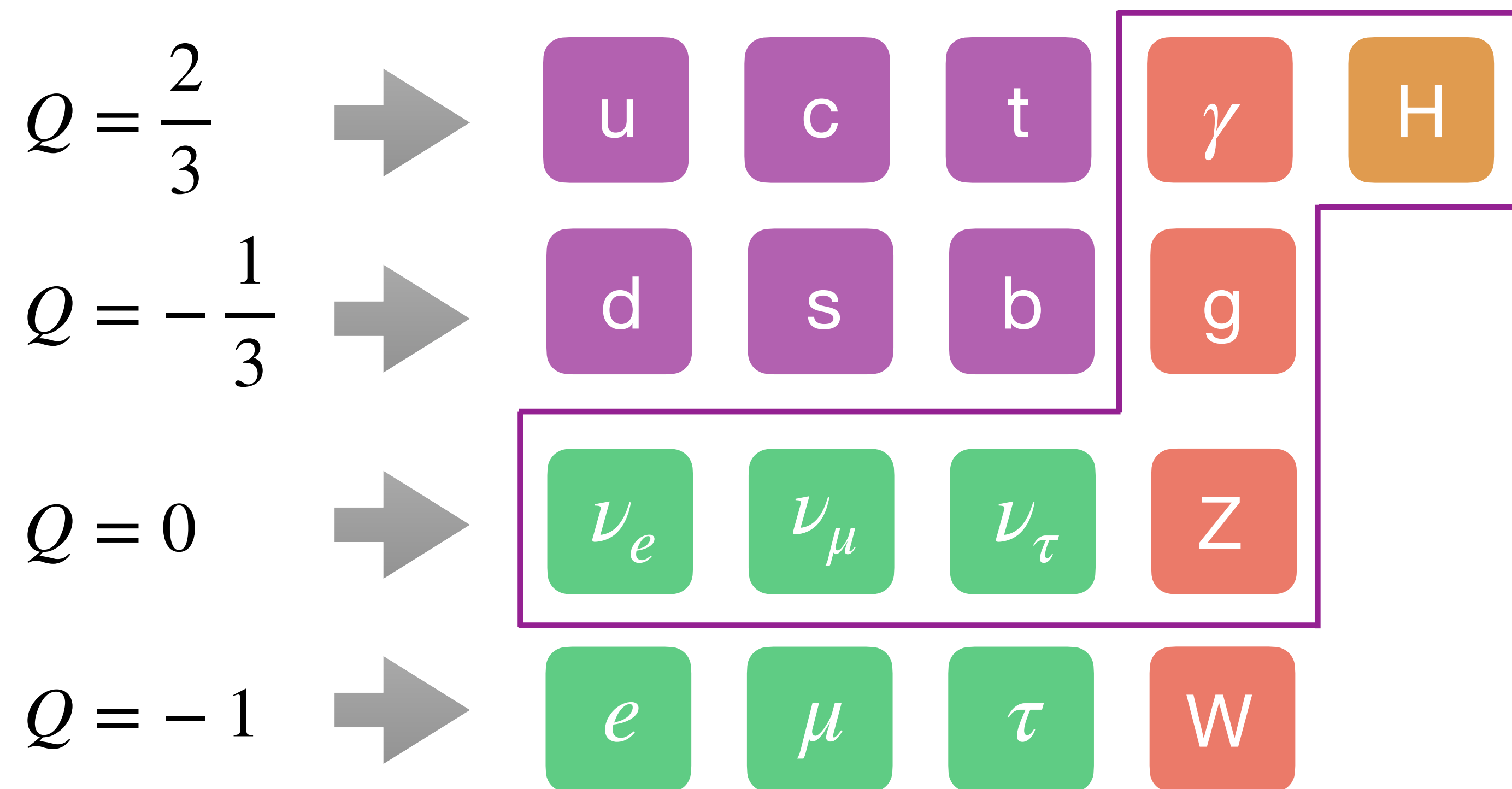
photon



$$e Q_f A_\mu^\gamma \bar{f} \gamma^\mu f$$

$Q_f = \frac{n}{3}$ is quantized in SM

Millicharge is a very small electric charge



photon

↓

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$Q_f = \frac{n}{3}$ is quantized in SM

non-quantized $Q_f \equiv \epsilon \ll 1$ → millicharge

Magnetic monopole leads to charge quantization

Dirac's paper on magnetic monopole & charge quantization in 1931

Quantised singularities in the electromagnetic field, [\[from https://inspirehep.net/\]](https://inspirehep.net/)

Paul Adrien Maurice Dirac (St John's Coll., Cambridge) (Sep 1, 1931)

Published in: *Proc.Roy.Soc.Lond.A* 133 (1931) 821, 60-72

[DOI](#) [cite](#)

[↻](#) 2,263 citations


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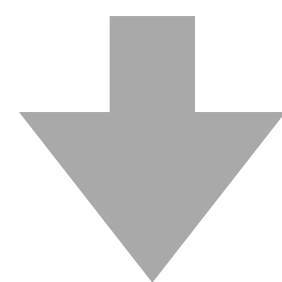
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magnetic monopole



charge quantization

$$e = \frac{2\pi\hbar n}{\mu}$$

n is integer

μ is magnetic strength

e is electric strength

Standard model & grand unified theories

“charge quantization” is not resolved completely in SM

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

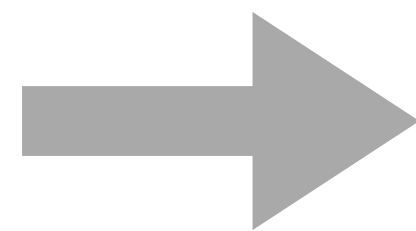
Standard model & grand unified theories

“charge quantization” is not resolved completely in SM

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

Embedded into a bigger gauge group, e.g. SU(5)

[Georgi & Glashow, PRL.32.438, 1974]



charge quantization

Stringent constraints on millicharge in SM

$$Q_p - Q_e < (0.8 \pm 0.8) \times 10^{-21} e$$

[Marinelli et al. 1984]

$$Q_n < (-0.1 \pm 1.1) \times 10^{-21} e$$

[Bressi et al. 2011]

$$Q_n < (-0.4 \pm 1.1) \times 10^{-21} e$$

[Baumann et al. 1988]

$$Q_\nu < 10^{-17} e$$

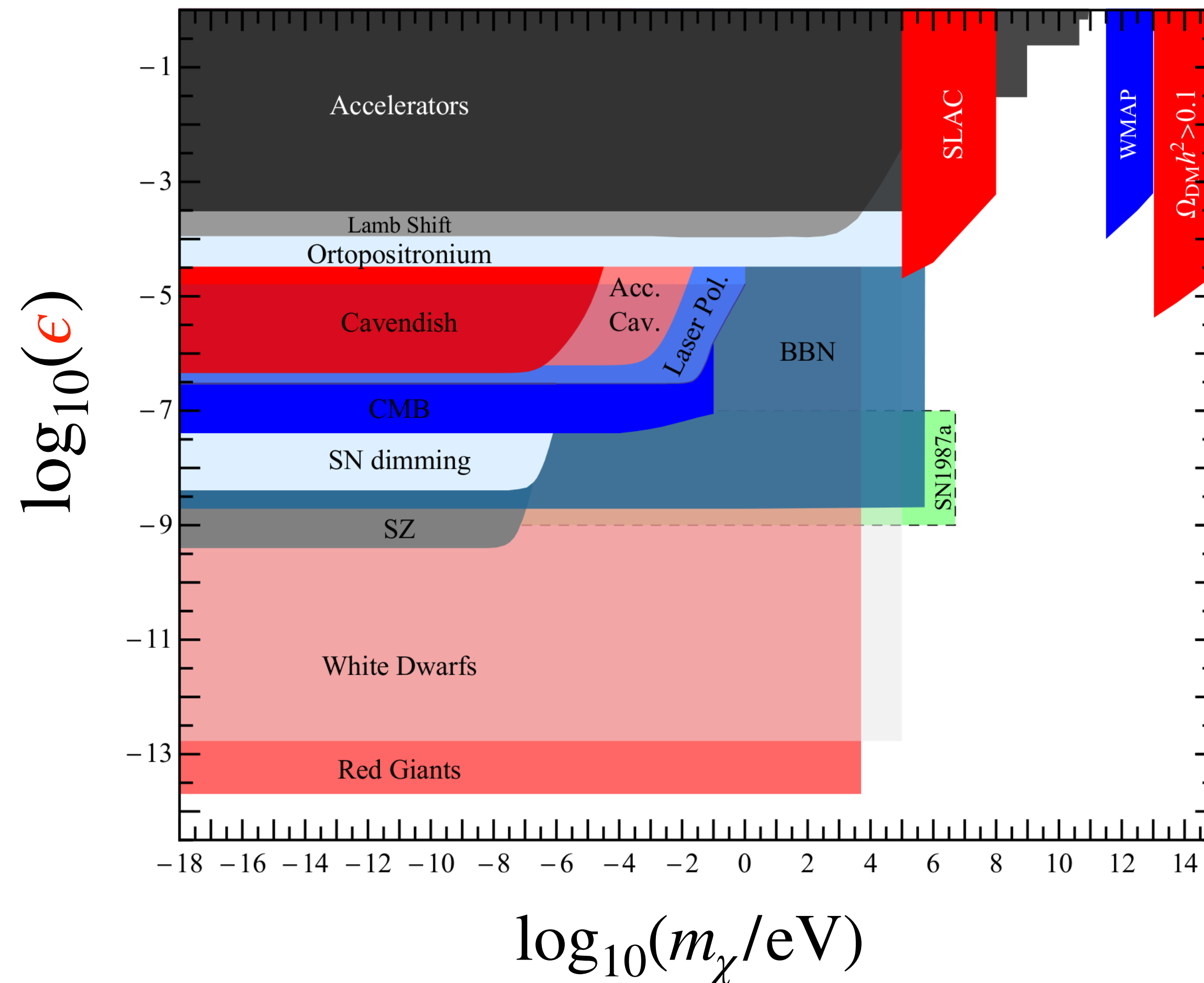
[Barbiellini et al. 1987]

[Siemensen et al., PRD 97, 052004 (2018)]

Millicharge in BSM can be quite “large”

[Jaeckel & Ringwald, 1002.0329]

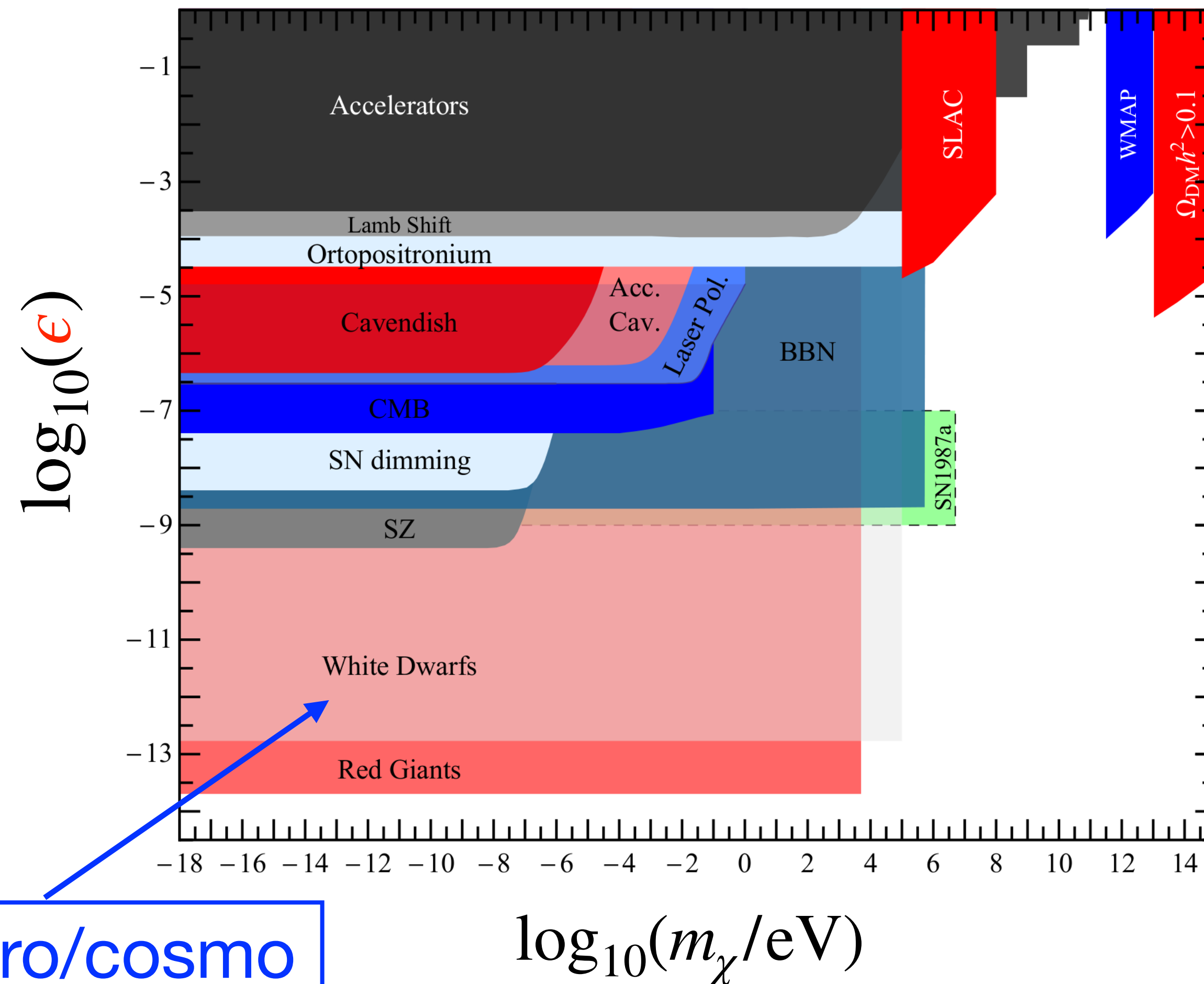
$$e \epsilon A_\mu^\gamma \bar{\chi} \gamma^\mu \chi$$



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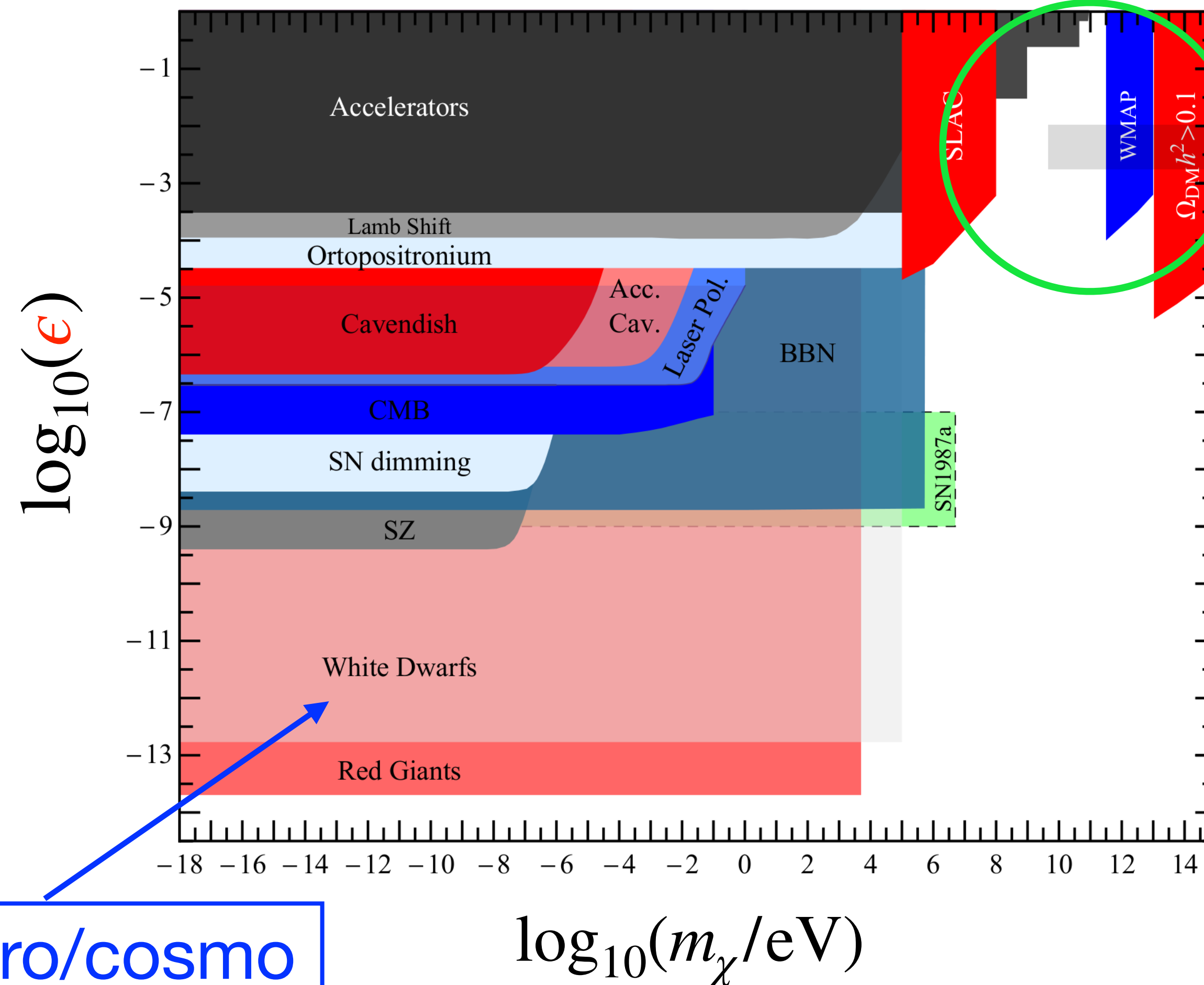


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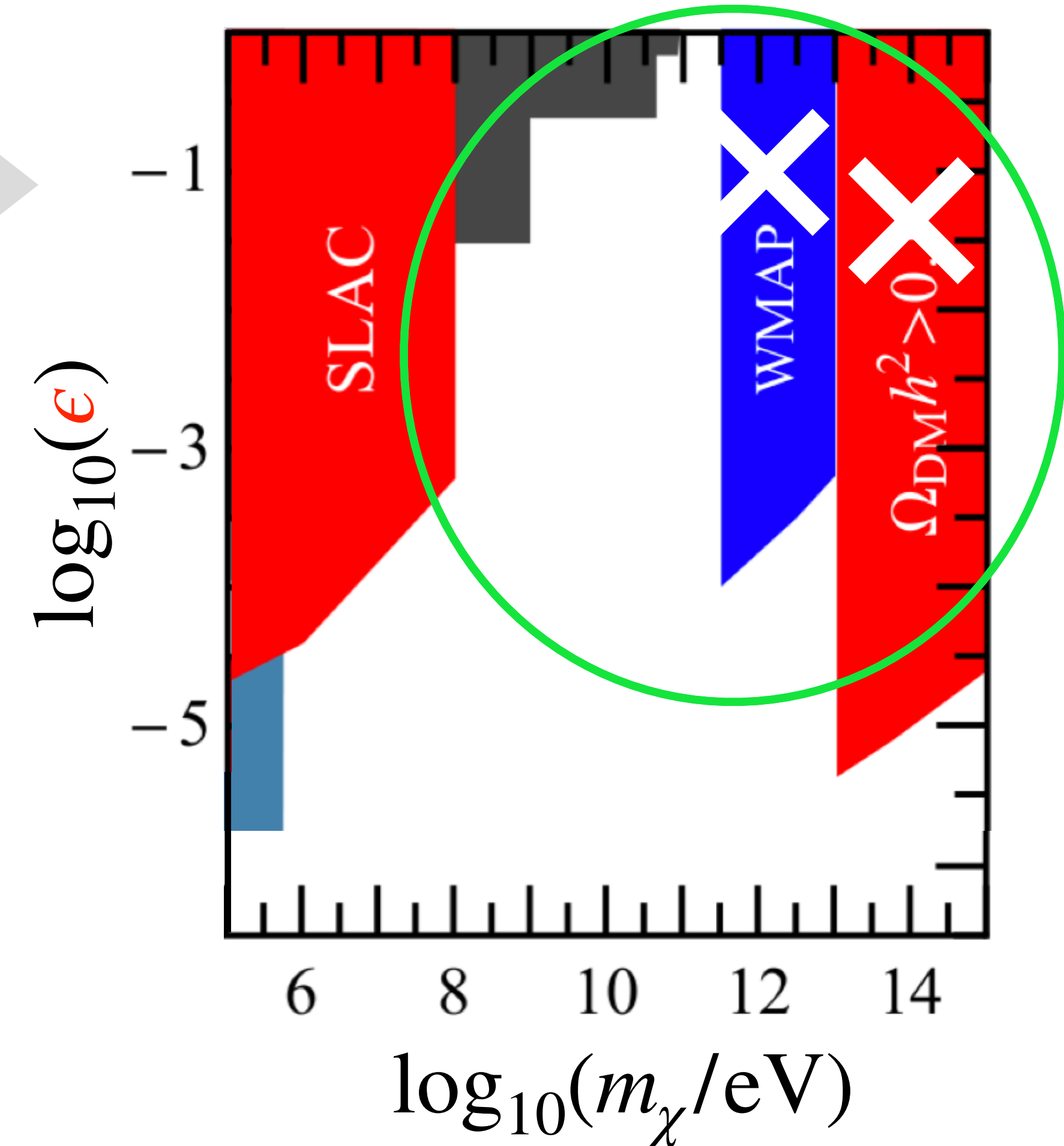
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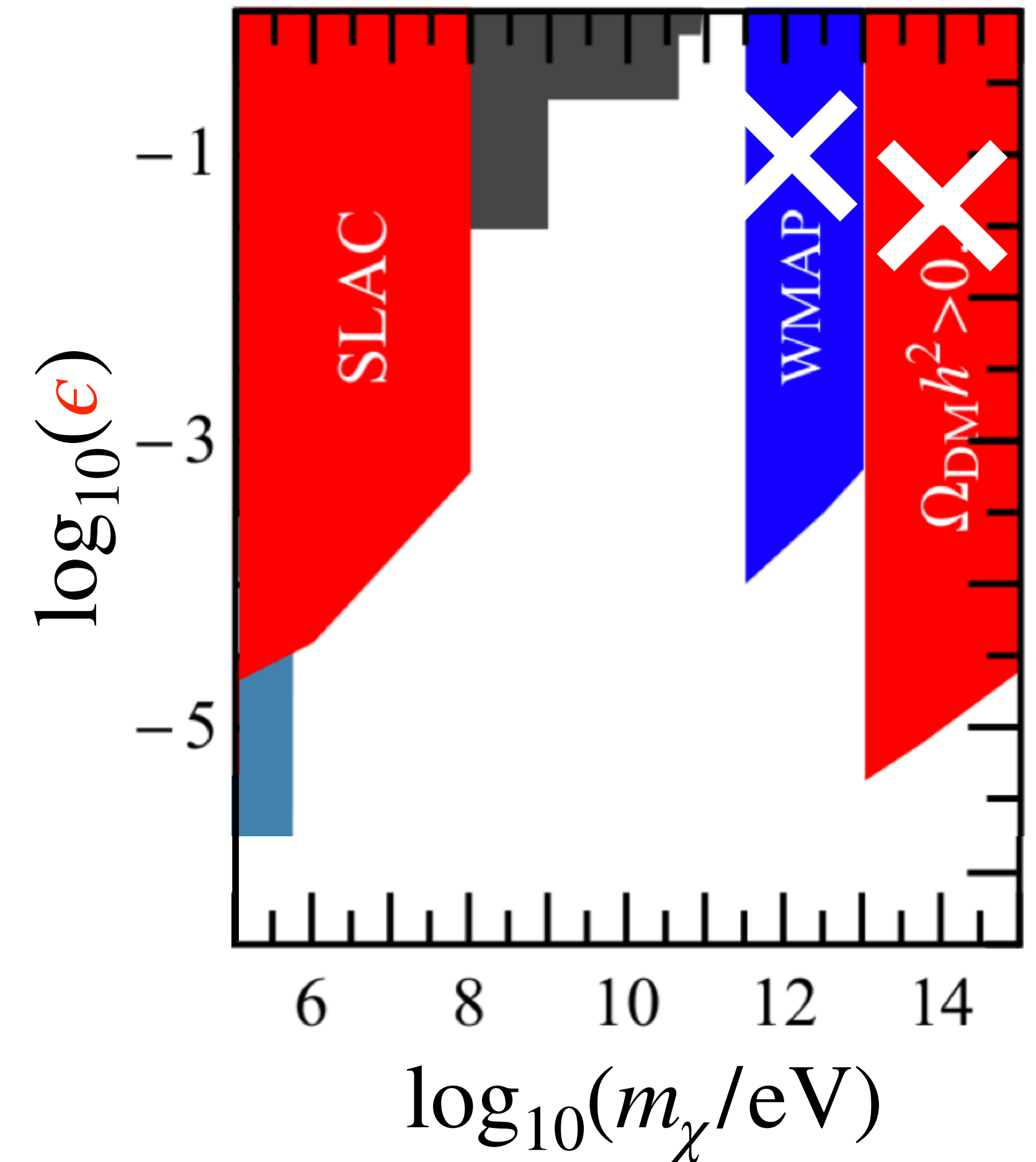
significant ϵ allowed



astro/cosmo



Probing millicharge at electron colliders

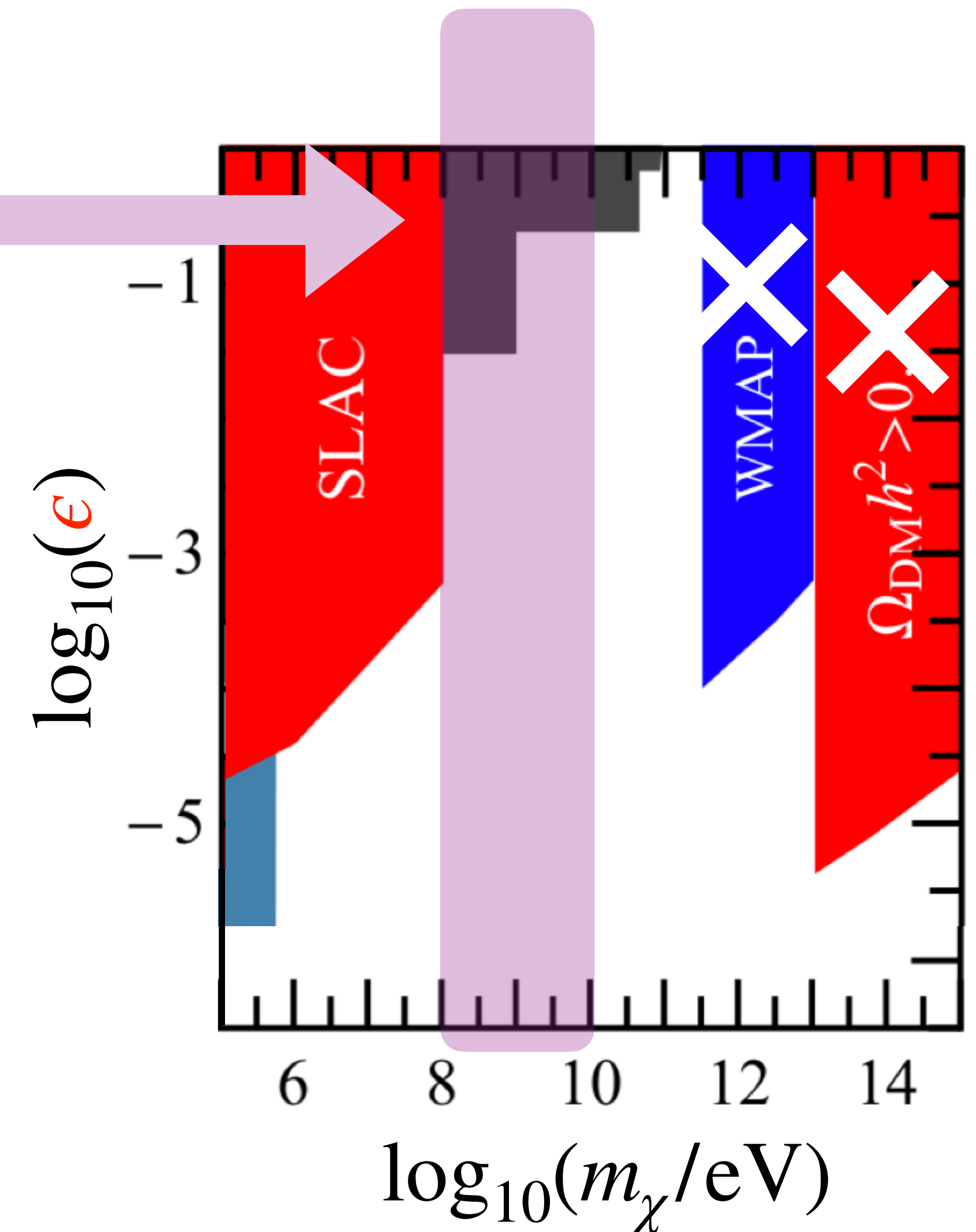


Probing millicharge at electron colliders

0.1-10 GeV

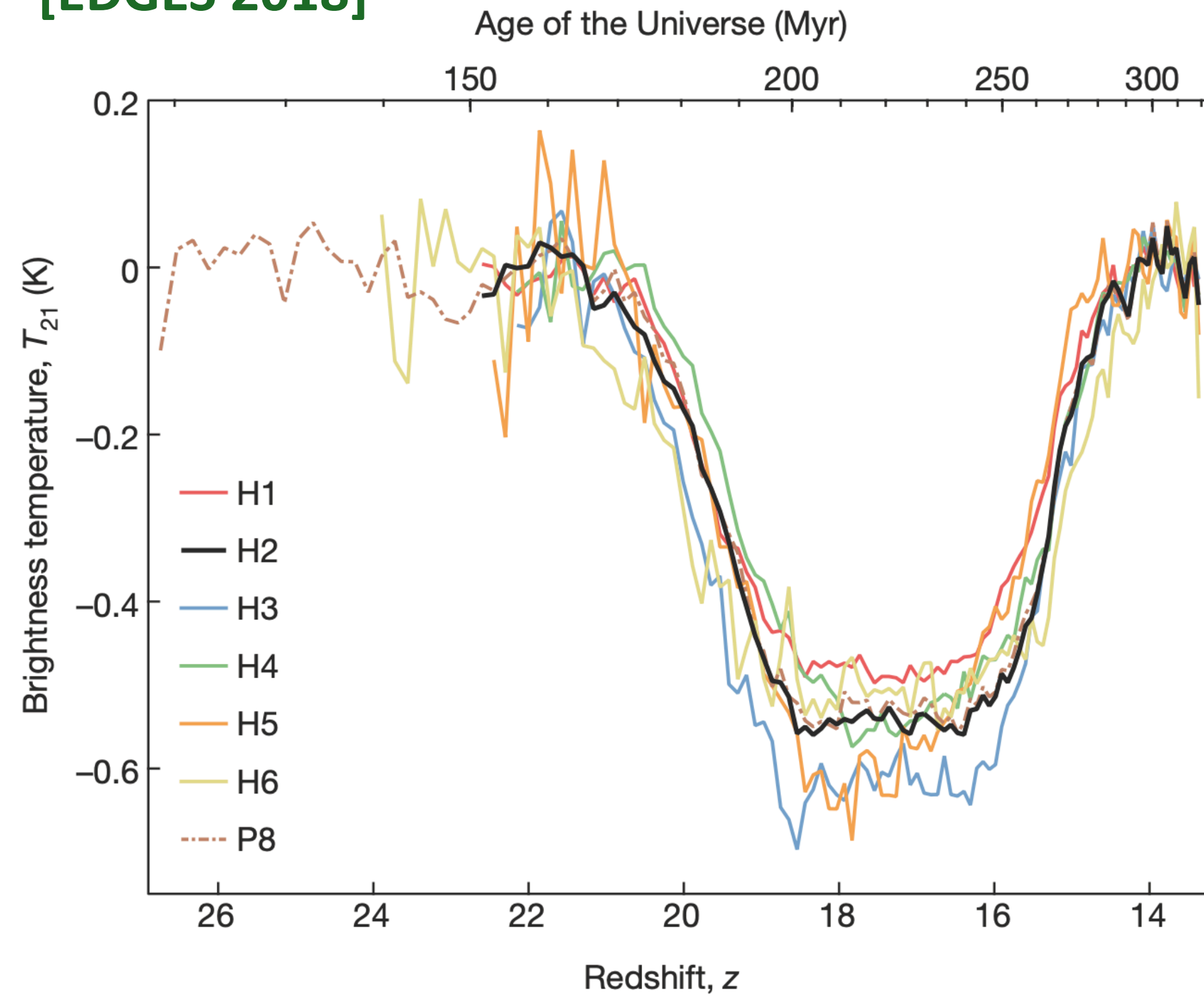
accessible at
electron colliders

BaBar
BESIII
Belle II
STCF



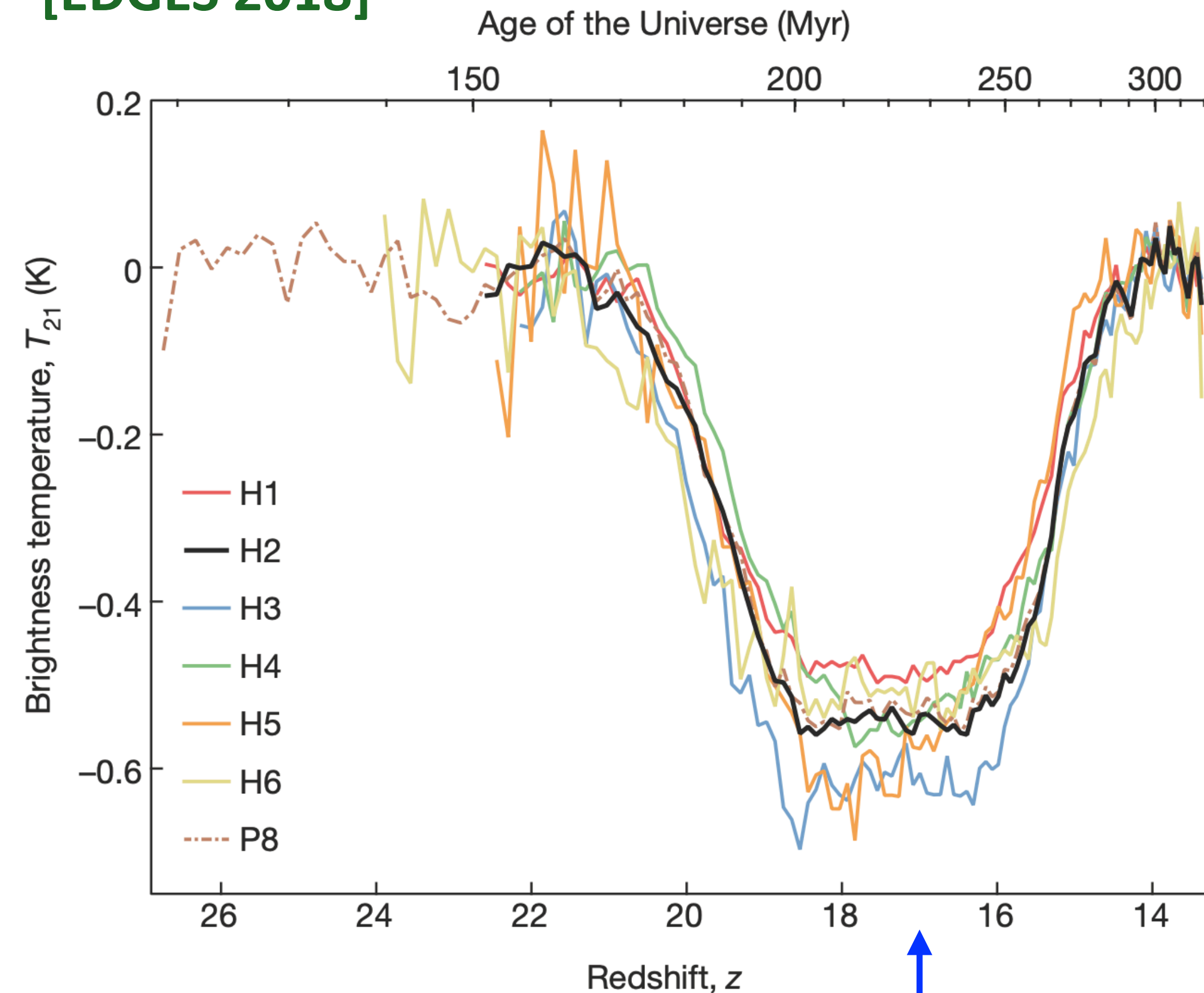
Millicharged DM explains EDGES 21 cm anomaly

[EDGES 2018]



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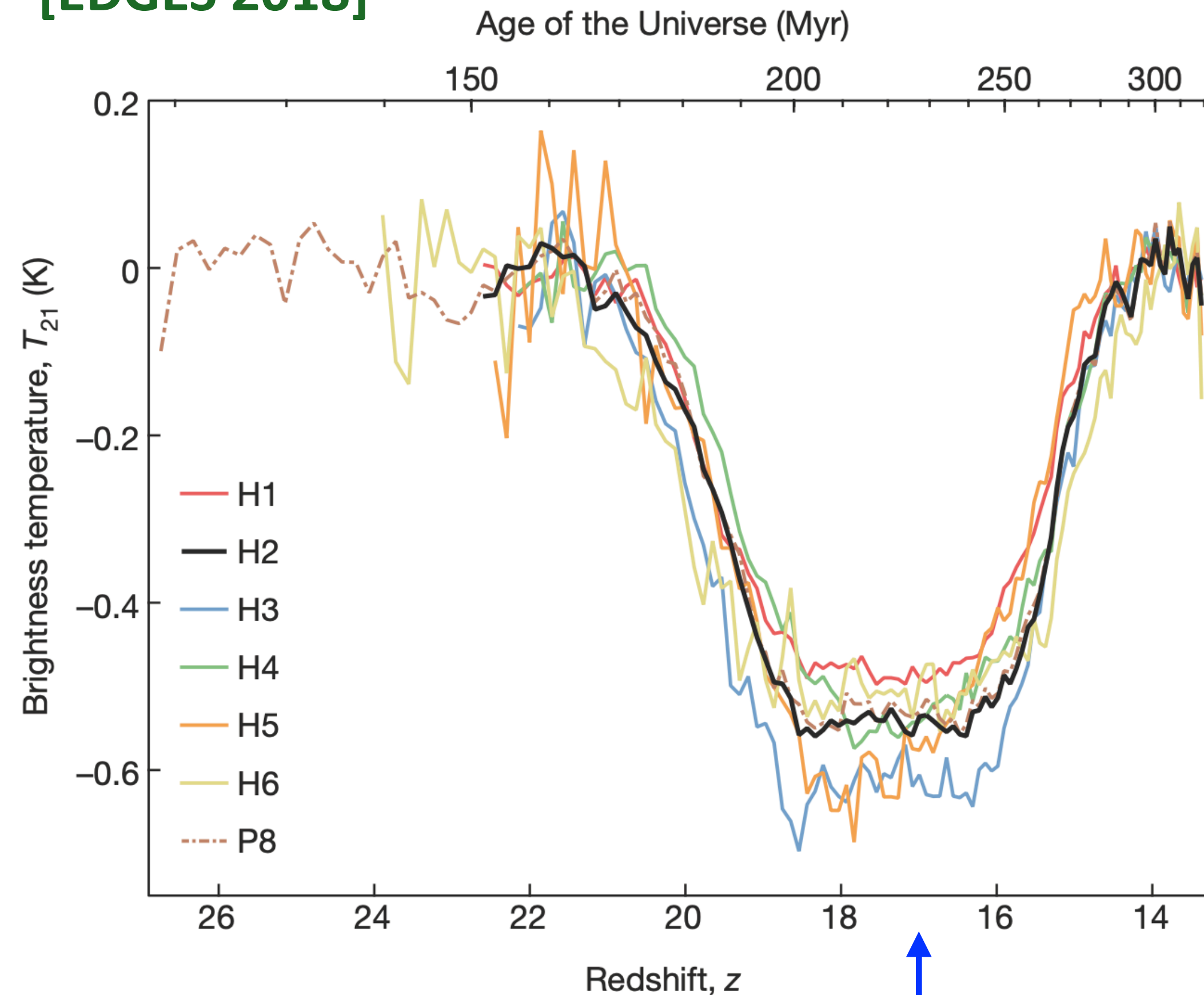
[EDGES 2018]



colder gas or hotter CMB than expected

Millicharged DM explains EDGES 21 cm anomaly

[EDGES 2018]



colder gas or hotter CMB than expected

DM can cool gas

Millicharged DM xsec

$$\sigma \propto v^{-4}$$

easier to evade early universe constraints

Outline: discussions on millicharge

1

theoretical models

[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

2

terrestrial searches

3

electron colliders' sensitivity

[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]

1 theoretical models

[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

Models to generate millicharged particles (MCPs)

$$e \epsilon A_{\mu}^{\gamma} \bar{\chi} \gamma^{\mu} \chi \quad \longrightarrow \quad \chi \text{ is MCP}$$

Kinetic mixing

Mass mixing

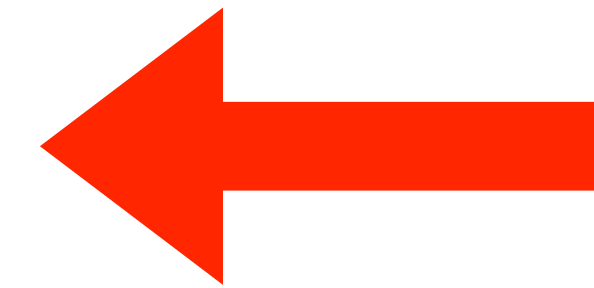
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Kinetic mixing

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[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

Kinetic mixing between two U(1) fields

Kinetic mixing between two U(1) fields: A_1 & A_2

$$\mathcal{L} = -\frac{1}{4}F_{2\mu\nu}F_2^{\mu\nu} - \frac{\delta}{2}F_{2\mu\nu}F_1^{\mu\nu} - \frac{1}{4}F_{1\mu\nu}F_1^{\mu\nu}$$

[Holdom, Phys.Lett. 166B, 196 (1986)]

[Foot & He, Phys. Lett. 267B, 509 (1991)]

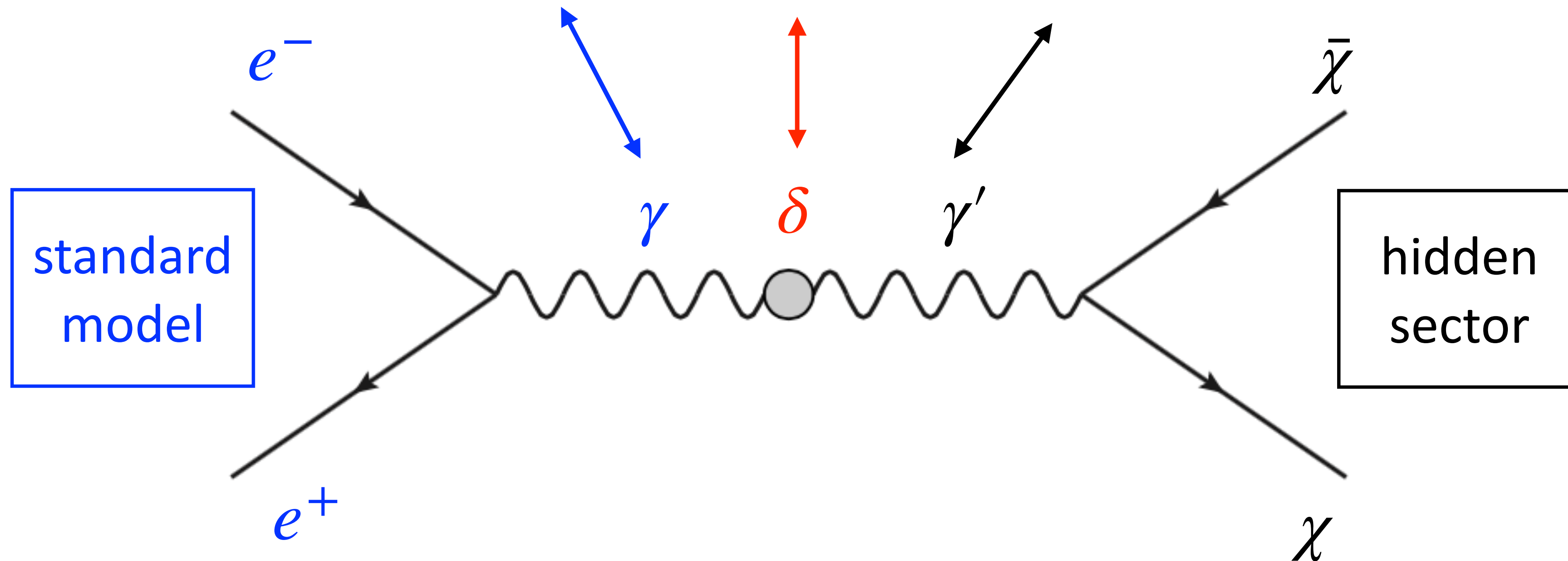
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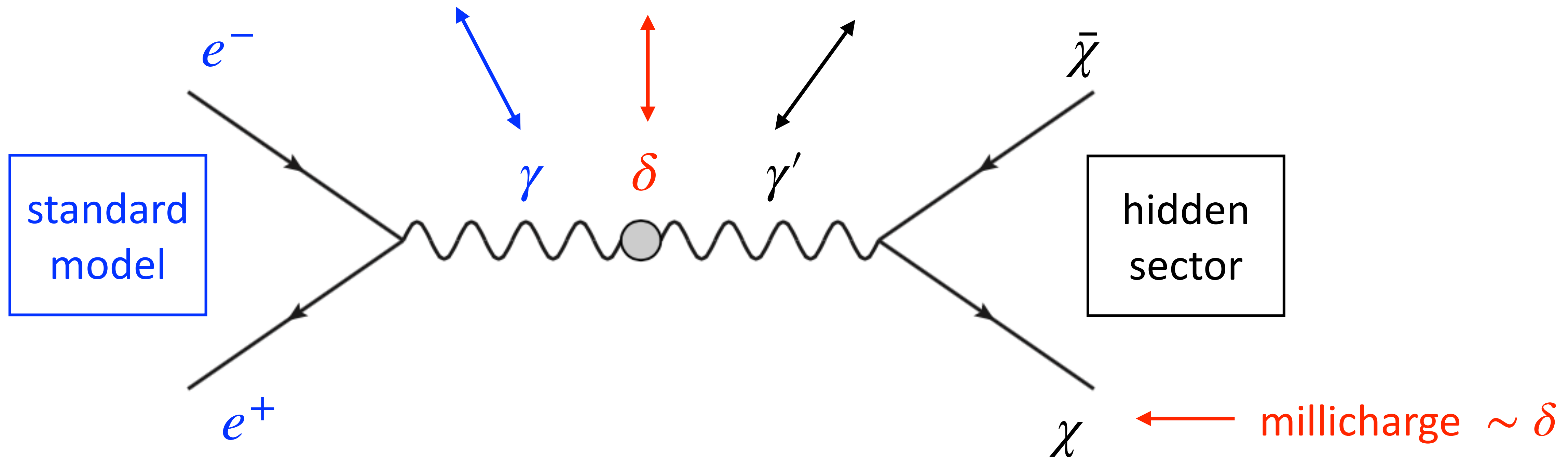
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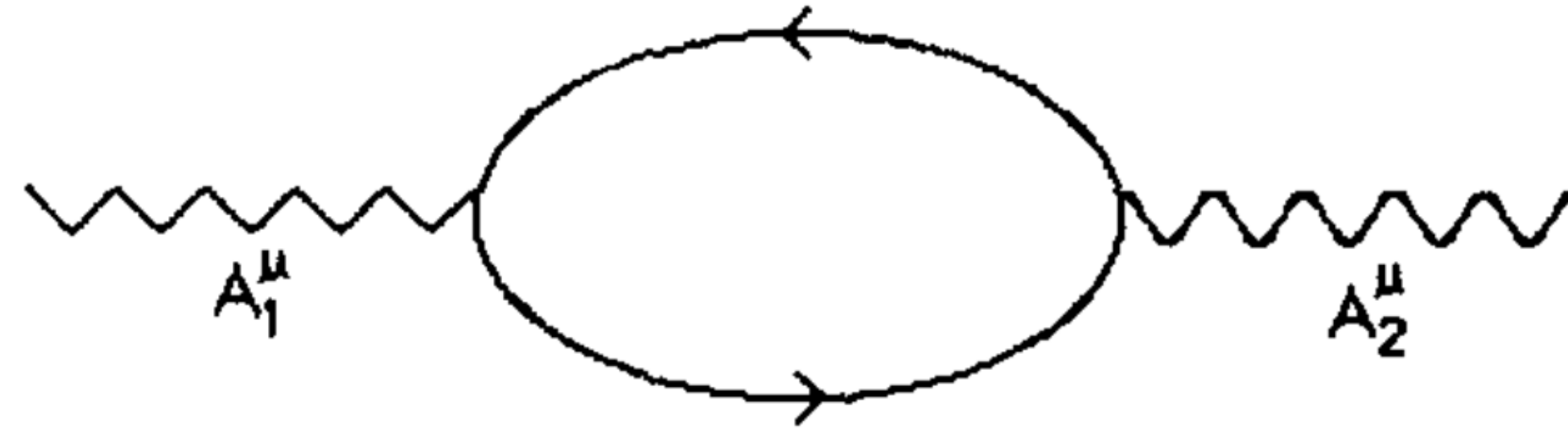
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One example to generate kinetic mixing

[Holdom, Phys.Lett. 166B (1986) 196-198]

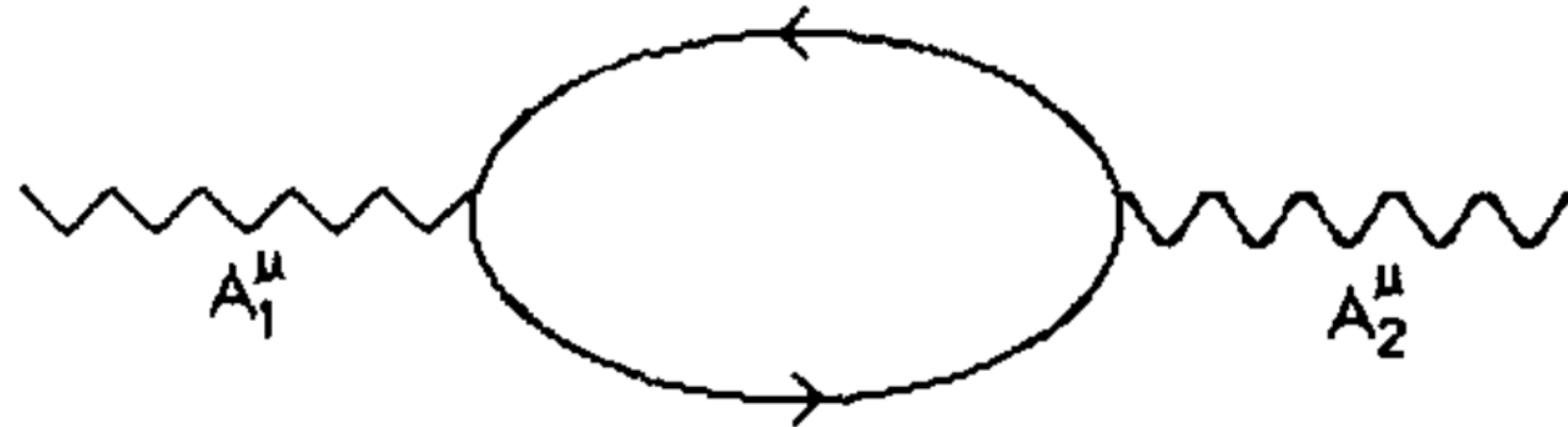
2 high scale fermions charged under two U(1)s



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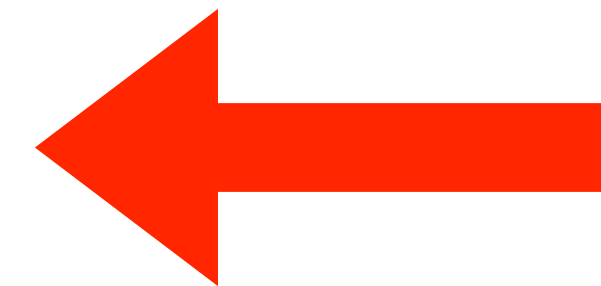
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$$\delta = \frac{e_1 e_2}{6\pi^2} \ln \frac{m'_{12}}{m_{12}}$$

Models to generate millicharged particles (MCPs)

Kinetic mixing

Mass mixing



Stueckelberg mass mixing between two U(1) fields

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[Kors & Nath hep-ph/0402047]

[Feldman, ZL, Nath, hep-ph/0603039]

[Cheung & Yuan hep-ph/0701107]

Stueckelberg mass mixing between two U(1) fields

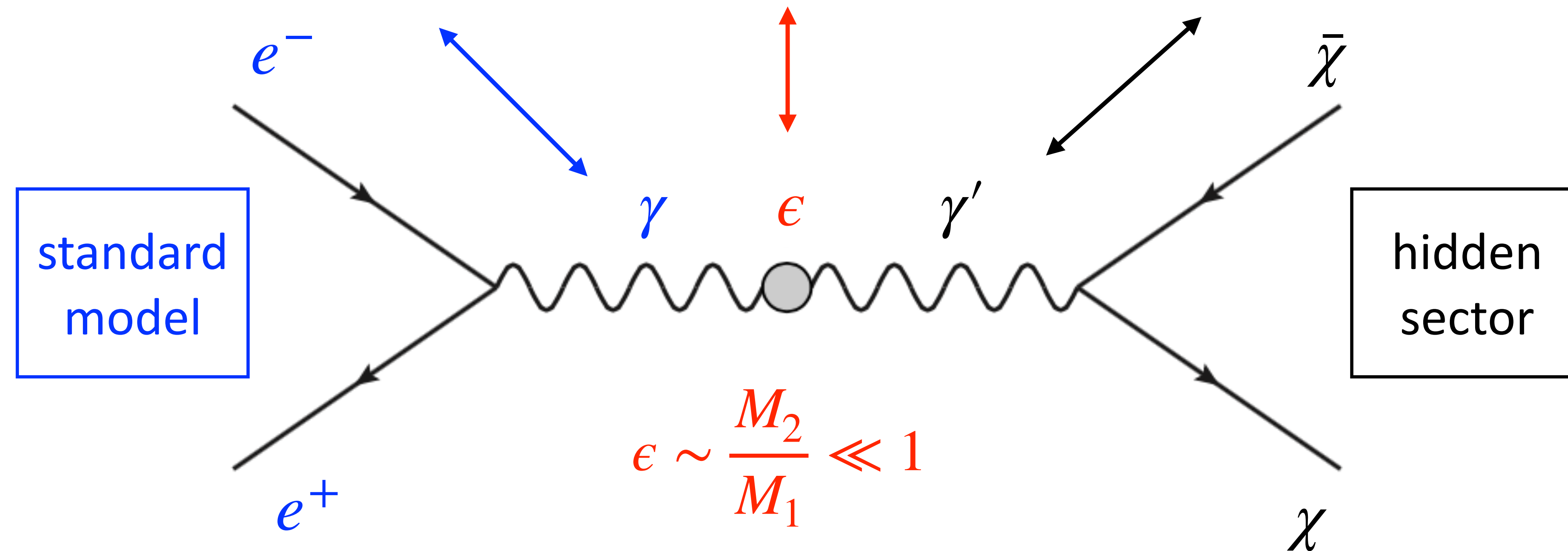
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Stueckelberg mass mixing between two U(1) fields

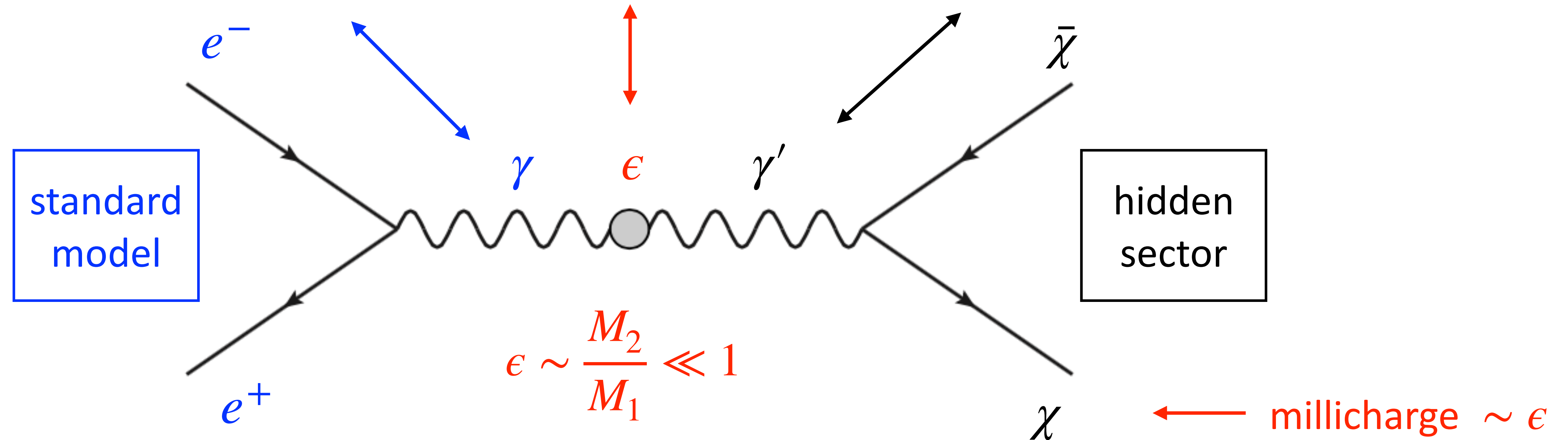
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“Toy” model w/ both kinetic & mass mixings

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[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

[Fabbrichesi et al., 2005.01515, The Dark Photon, p 7-9]

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after field redefinition & rotation \longrightarrow canonical ($-F^2/4$) & diagonal mass matrix

$$\frac{1}{\sqrt{1 - 2\delta\epsilon + \epsilon^2}} \left(\frac{\epsilon - \delta}{\sqrt{1 - \delta^2}} J_\mu + \frac{1 - \delta\epsilon}{\sqrt{1 - \delta^2}} J'_\mu \right) A_M^\mu + \frac{1}{\sqrt{1 - 2\delta\epsilon + \epsilon^2}} \left(J_\mu - \epsilon J'_\mu \right) A_\gamma^\mu$$

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SM photon



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dark photon

SM photon

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degeneracy

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mass mixing \rightarrow millicharge

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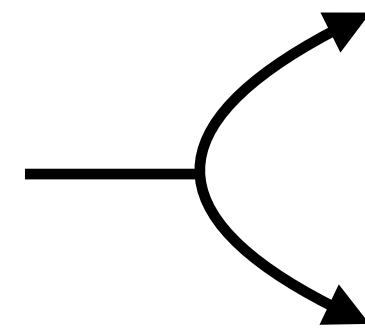
“Realistic” model w/ both kinetic & mass mixings

common
features

hidden boson mix w/ **hypercharge**
(instead of photon)

\Rightarrow **3 by 3** mass matrix

hidden boson



photon-like (dark photon)

$$m_{A'} \ll m_Z$$

hypercharge-like

$$m_{A'} \gg m_Z$$

[Feldman, ZL, Nath, hep-ph/0702123, **299** cites]

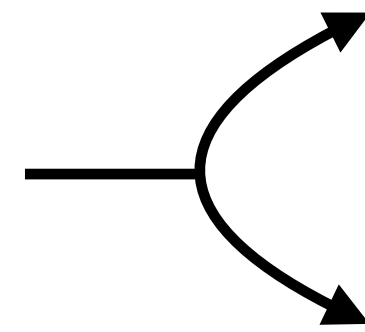
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hypercharge-like

$$m_{A'} \gg m_Z$$

difference

mass mixing \implies millicharge & massive dark photon

kinetic mixing \implies millicharge & massless dark photon

[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

2 terrestrial searches

Two ways to “detect” millicharged particles

$$e \epsilon A_{\mu}^{\gamma} \bar{\chi} \gamma^{\mu} \chi \quad \longrightarrow \quad \chi \text{ is MCP}$$

scintillation/ionization/scattering

missing energy

[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]

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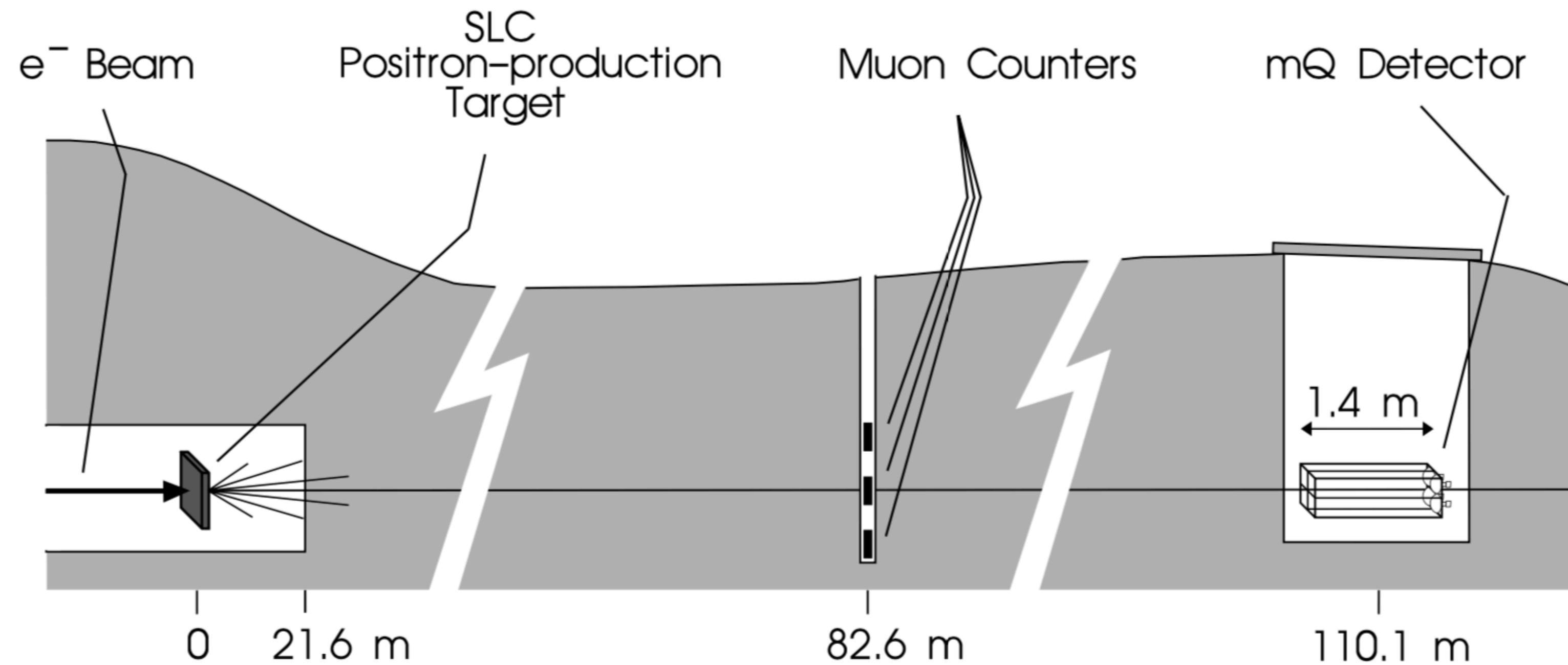
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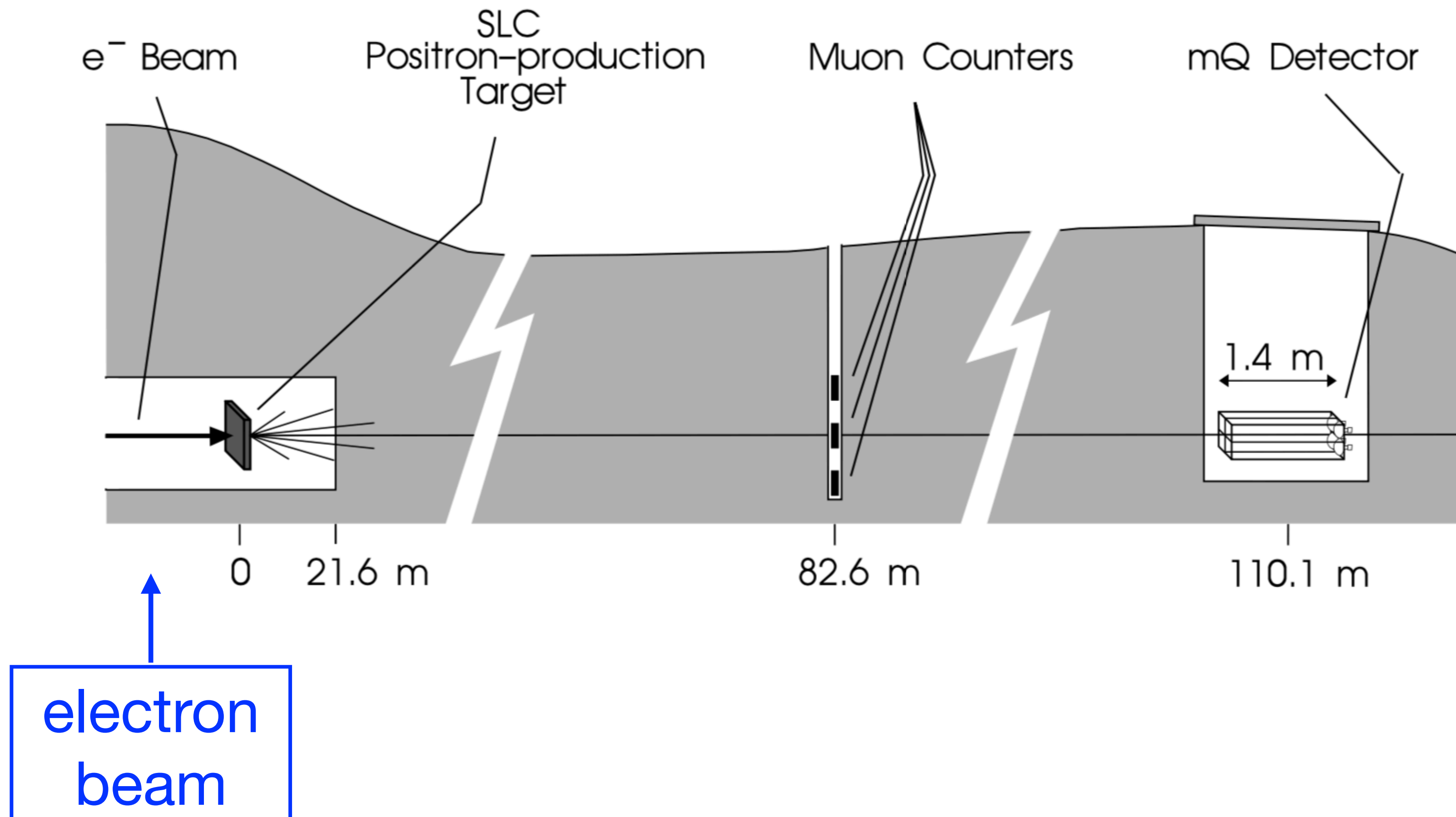
SLAC mQ: electron beam dump experiment

[Prinz et al, PRL 81.1175, 1998]



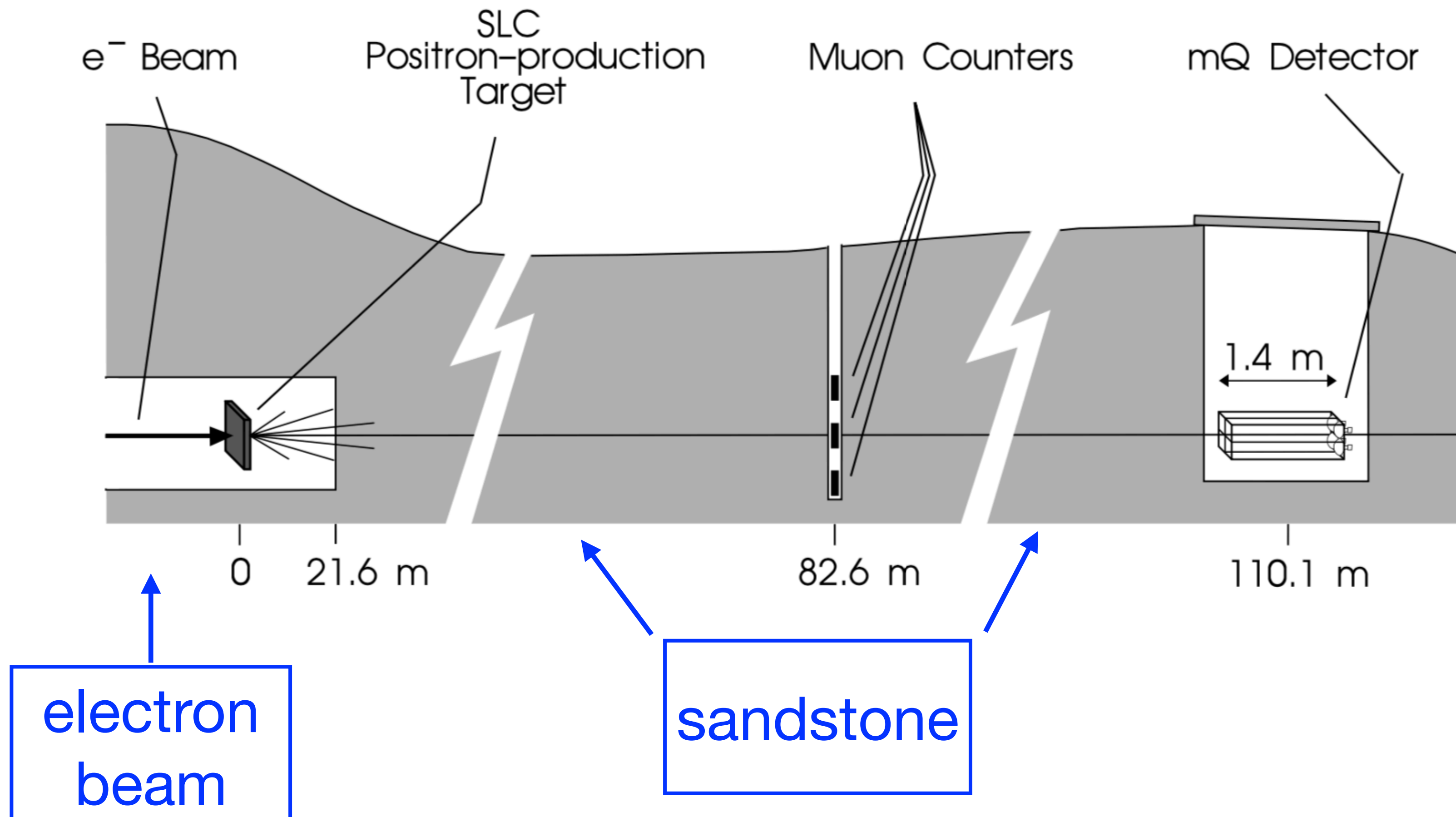
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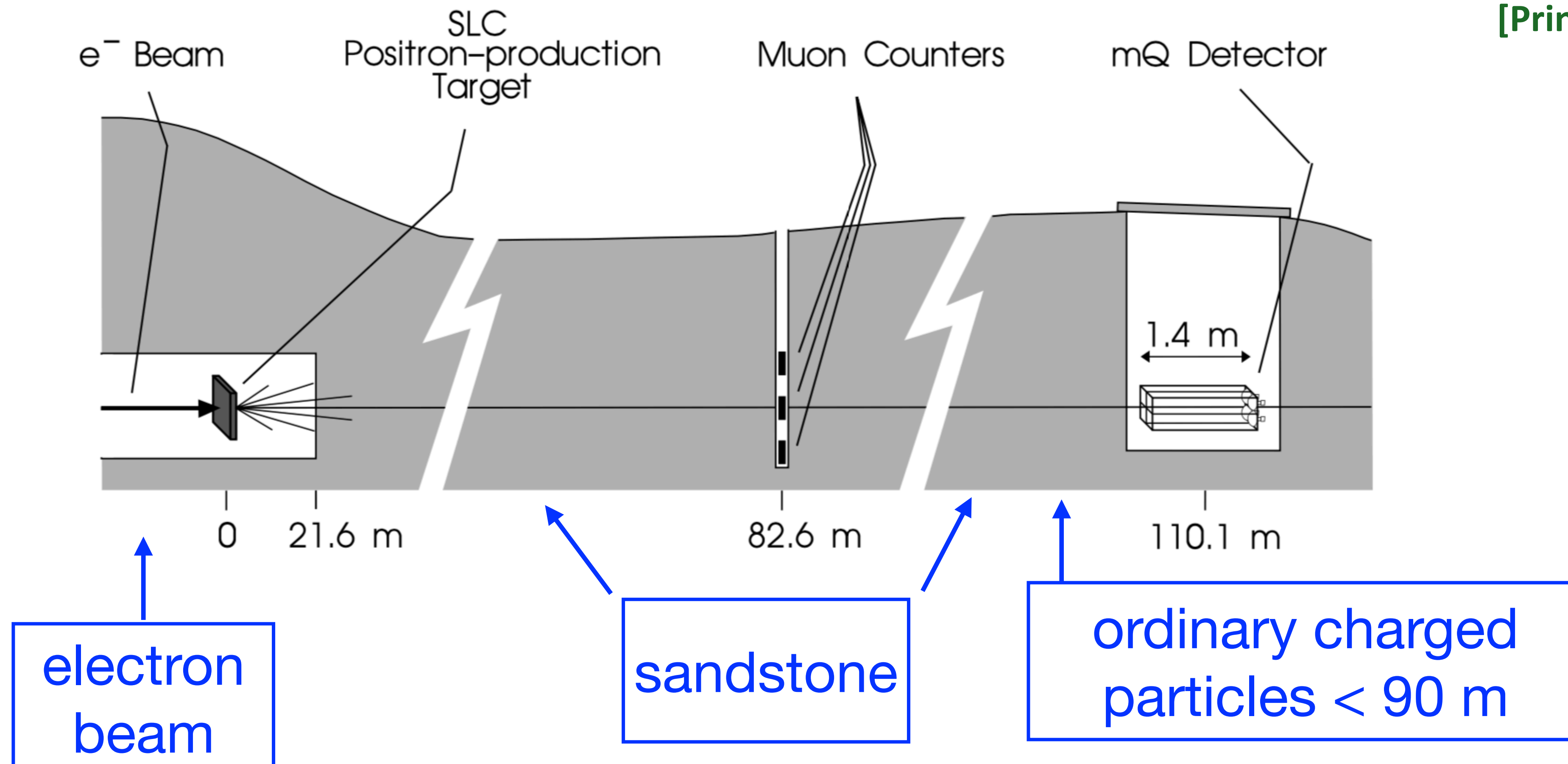
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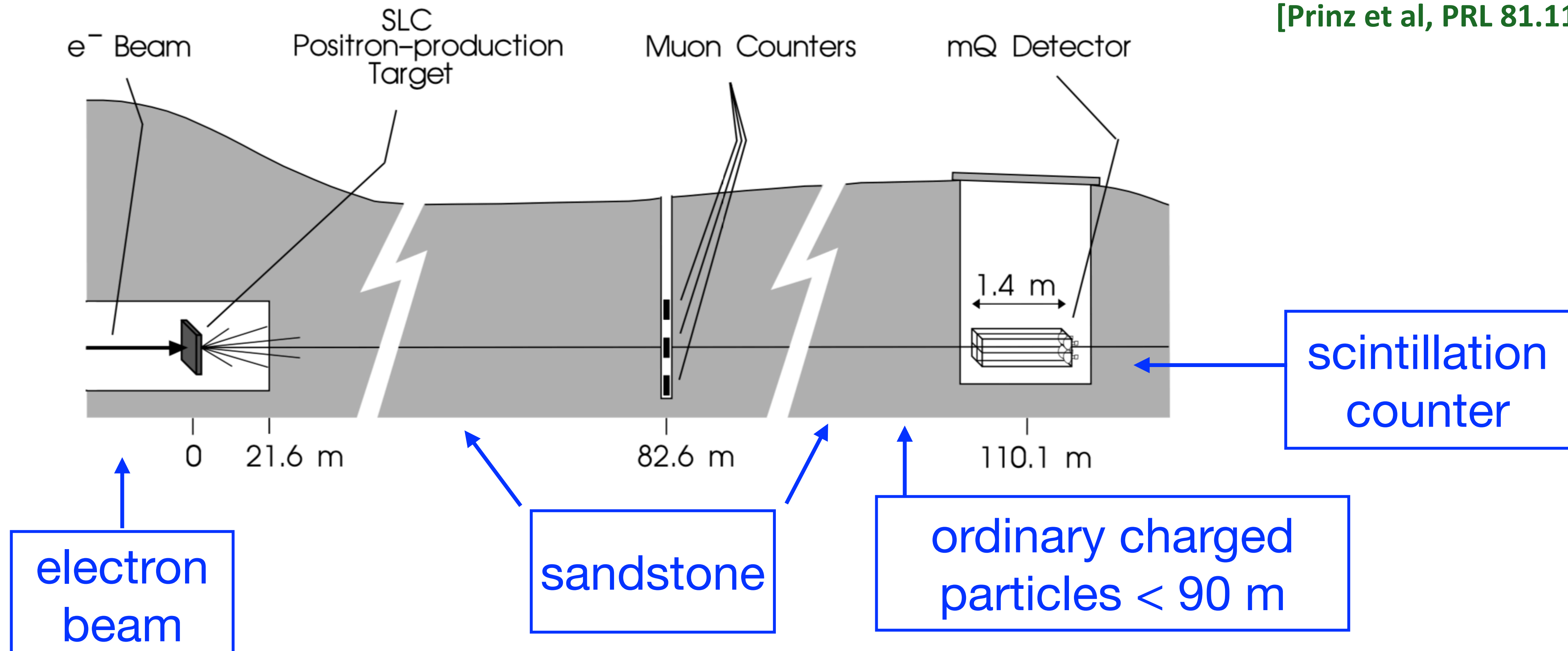
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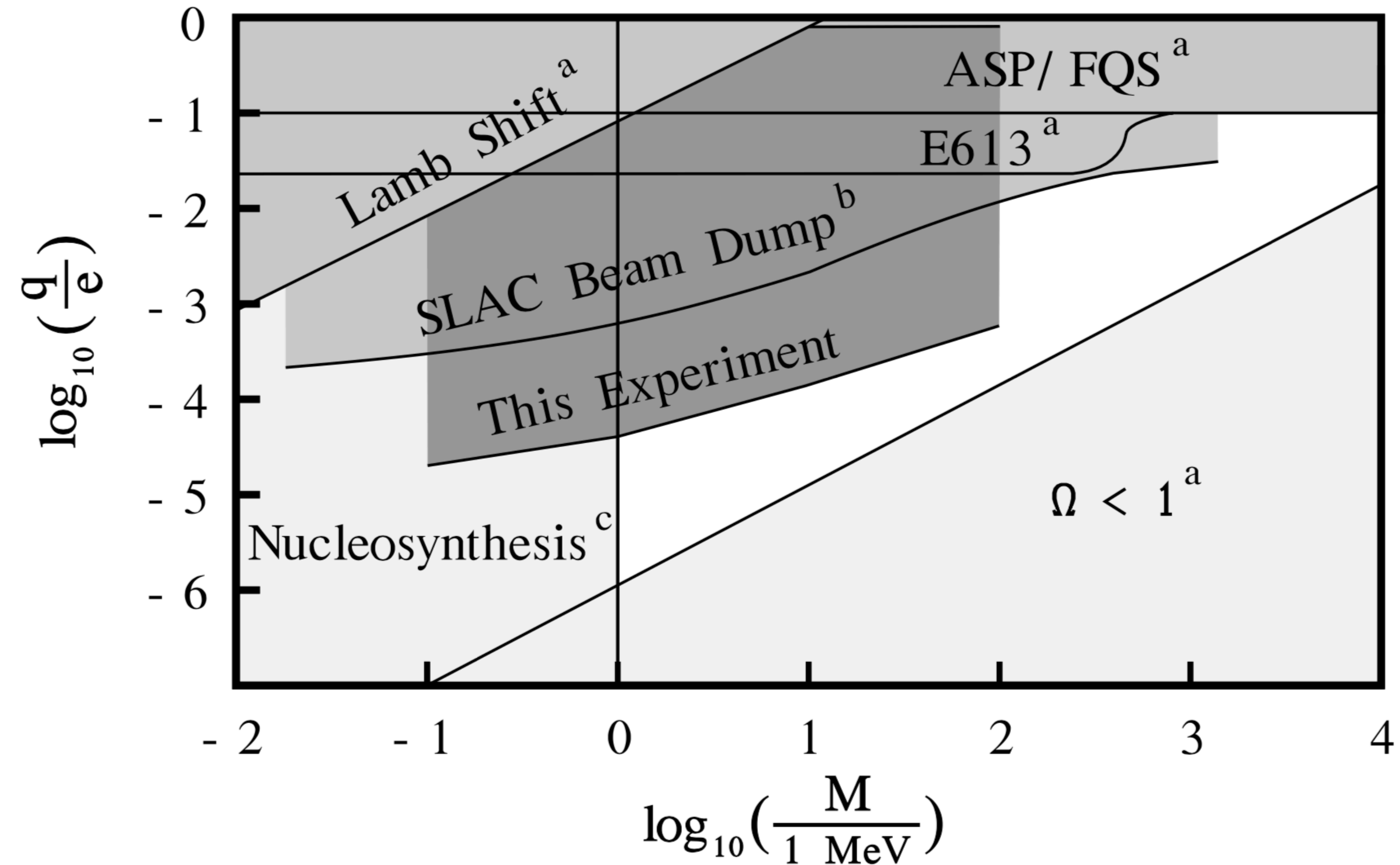
SLAC mQ: electron beam dump experiment

[Prinz et al, PRL 81.1175, 1998]



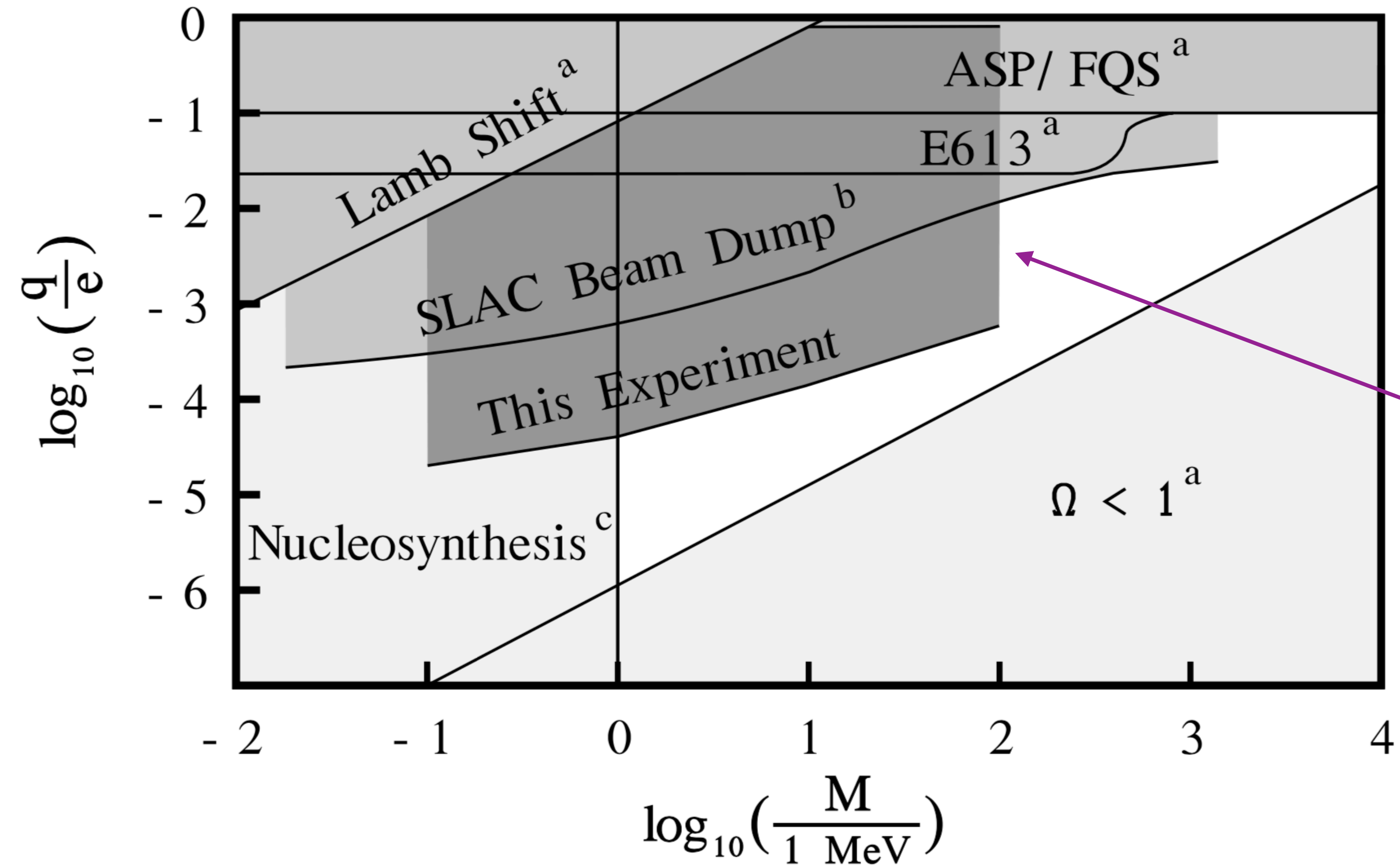
SLAC mQ constraints on millicharge

[Prinz et al, PRL 81.1175, 1998]



SLAC mQ constraints on millicharge

[Prinz et al, PRL 81.1175, 1998]

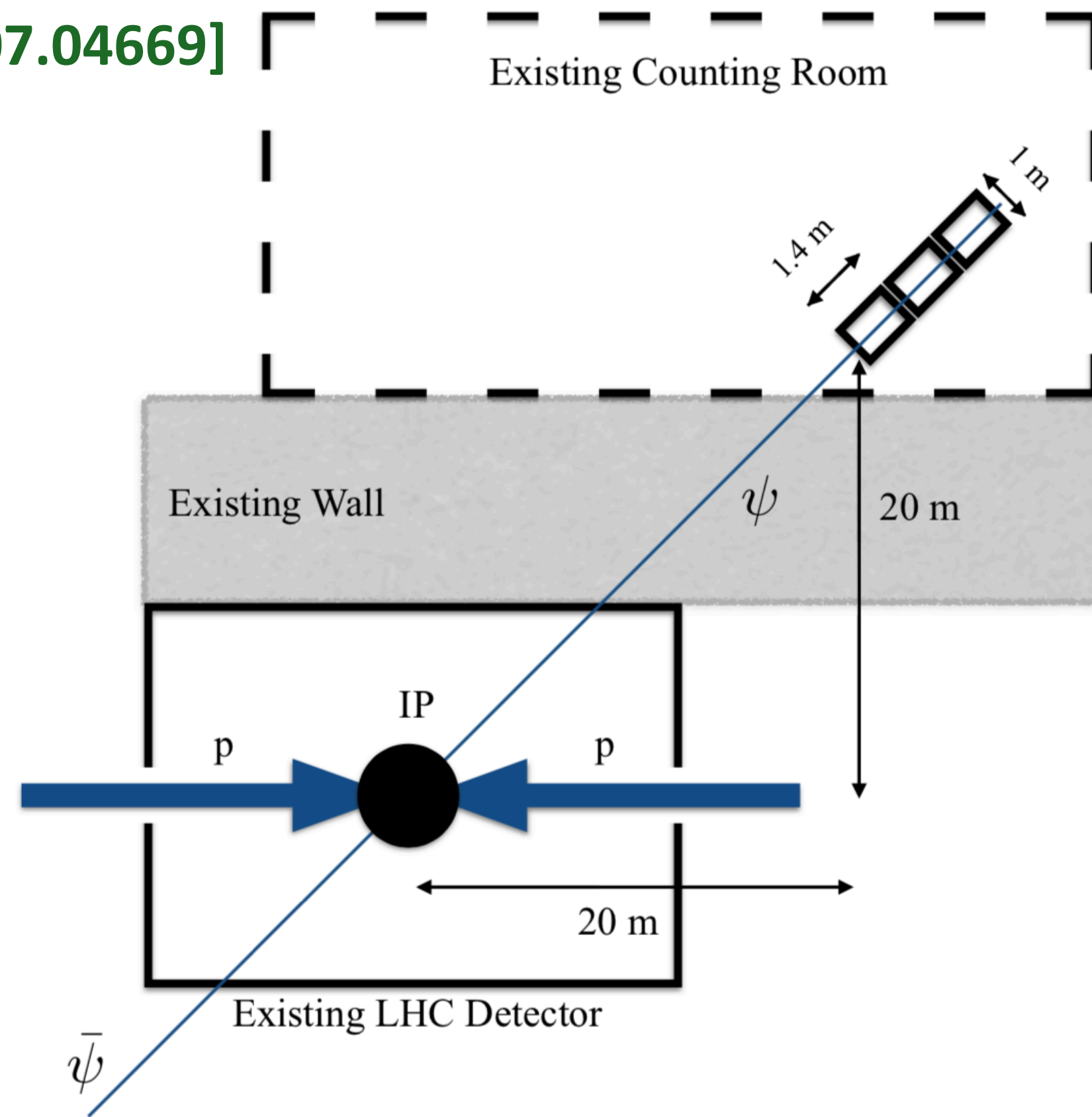


$m > 100 \text{ MeV}$
MCP yield die off

MilliQan: proposed scintillation detector @ LHC

[Haas et al., 1410.6816]

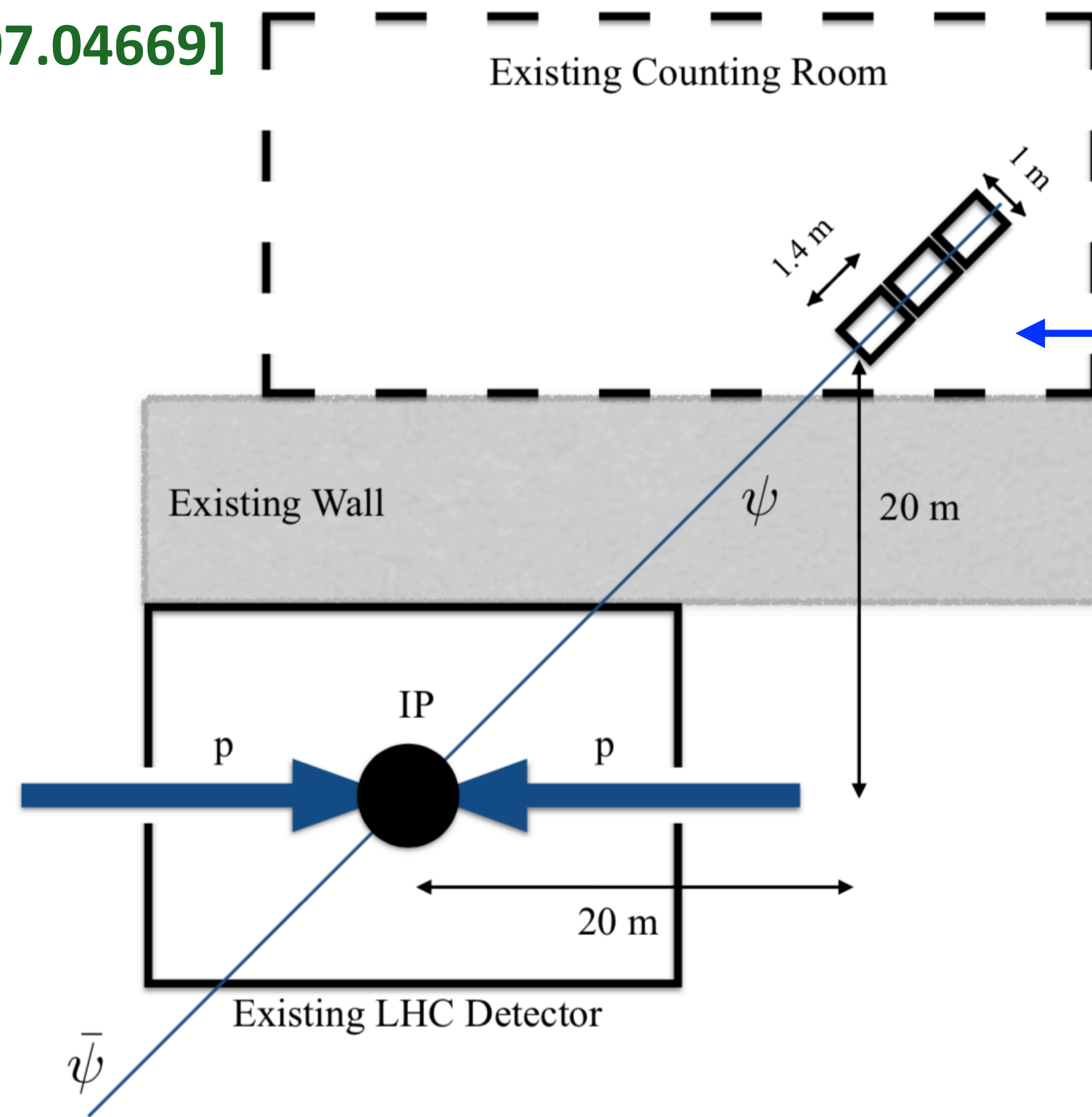
[Ball et al., 1607.04669]



MilliQan: proposed scintillation detector @ LHC

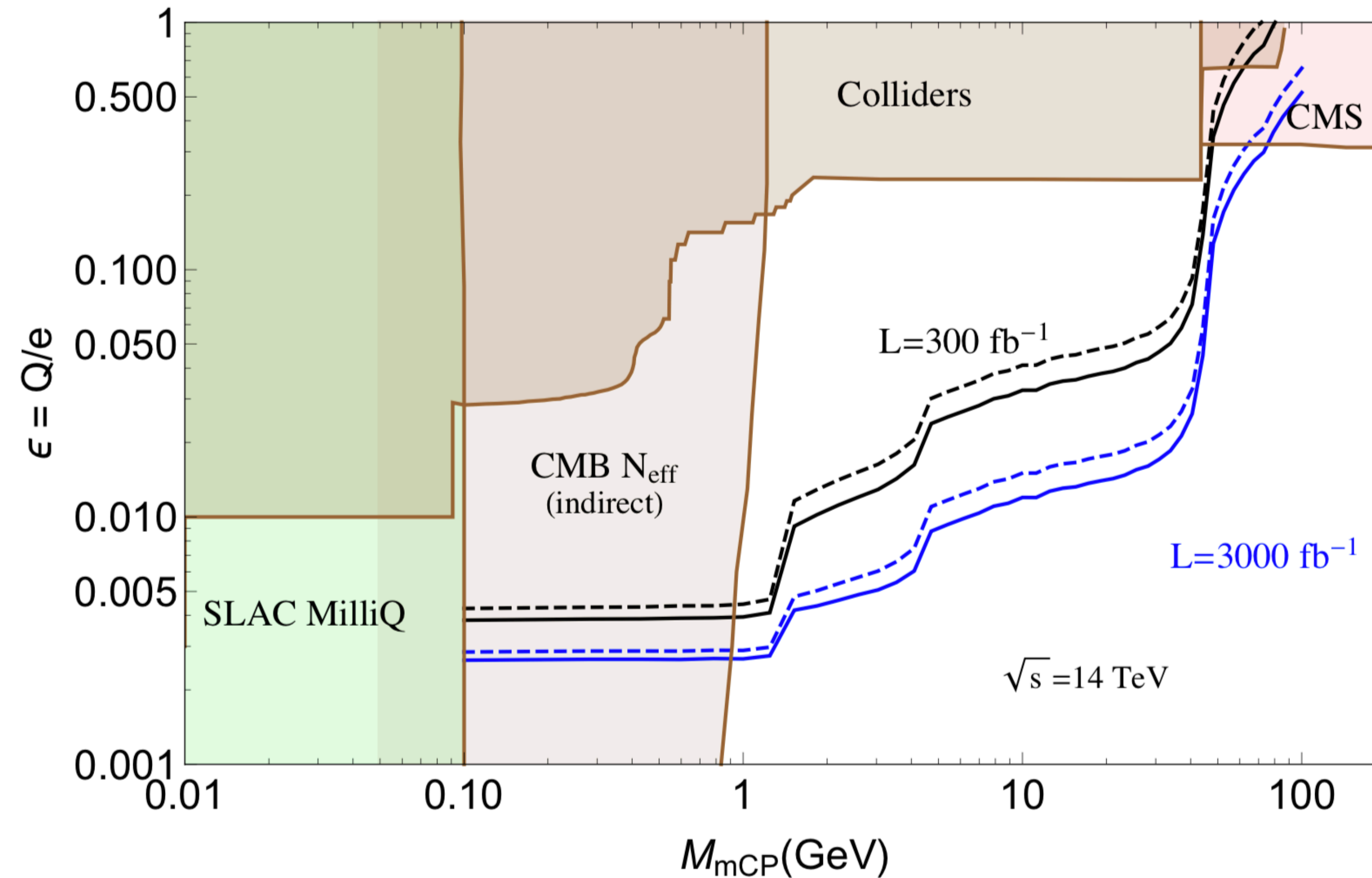
[Haas et al., 1410.6816]

[Ball et al., 1607.04669]



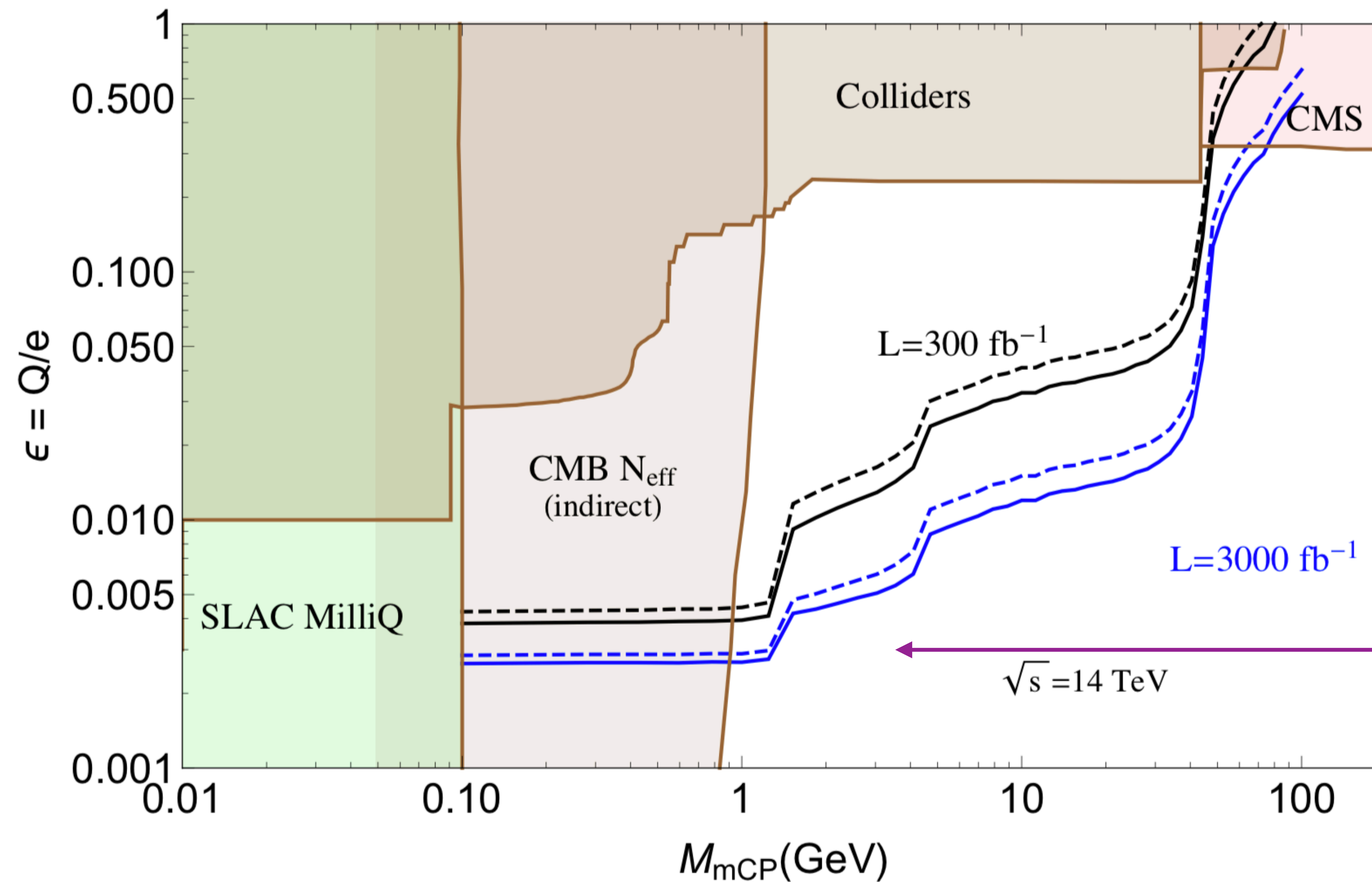
$1\text{ m} \times 1\text{ m} \times 3\text{ m}$ plastic scintillators array with 3 sections (pointing to CMS IP), each containing **400** $5\text{ cm} \times 5\text{ cm} \times 80\text{ cm}$ scintillator bars coupled to PMT. 33 m away from CMS IP.

MilliQan sensitivity on millicharged particles



[Ball et al., 1607.04669]

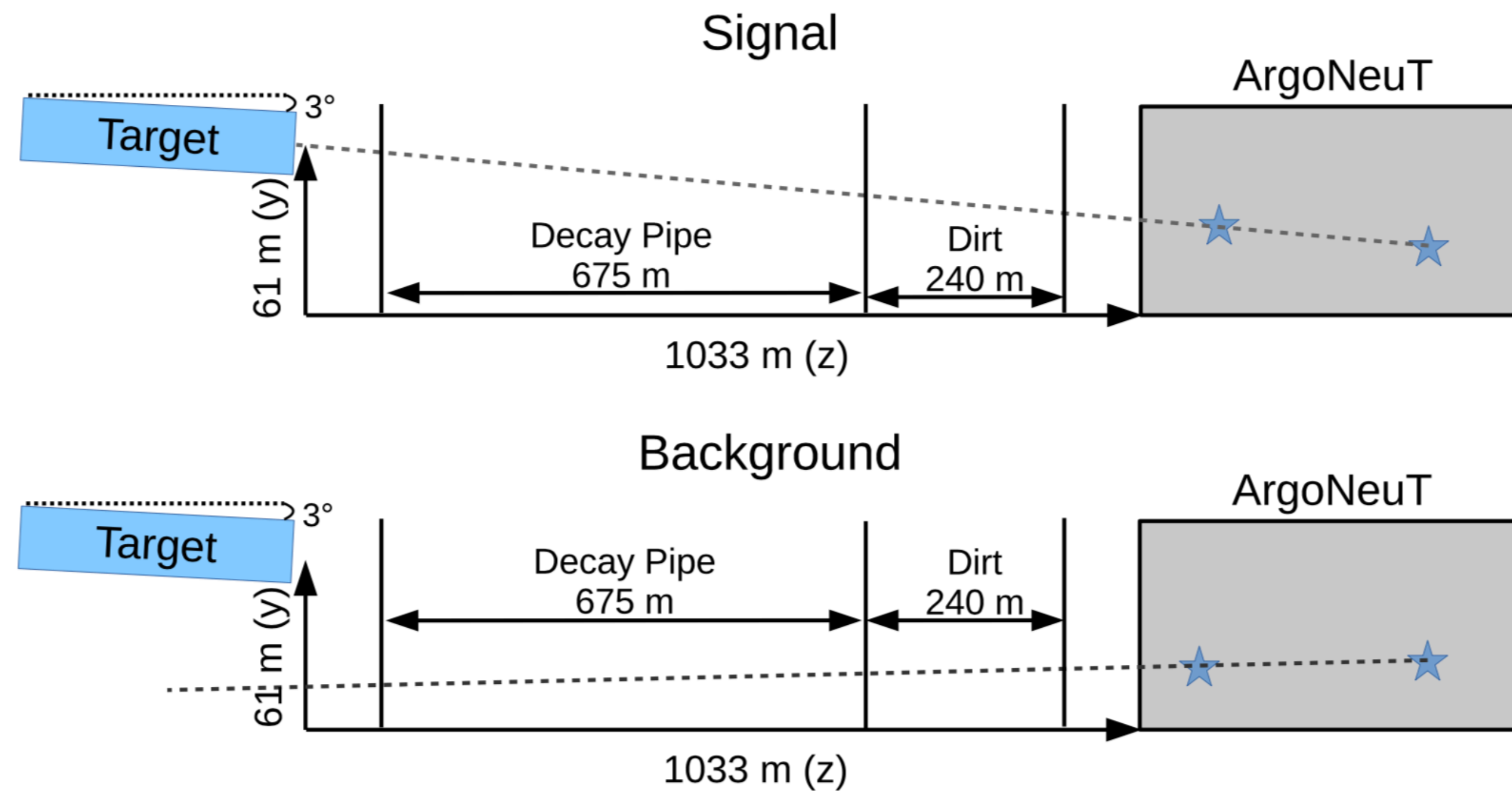
MilliQan sensitivity on millicharged particles



[Ball et al., 1607.04669]

photoelectron drops
below one when
 $\epsilon \lesssim O(10^{-3})$

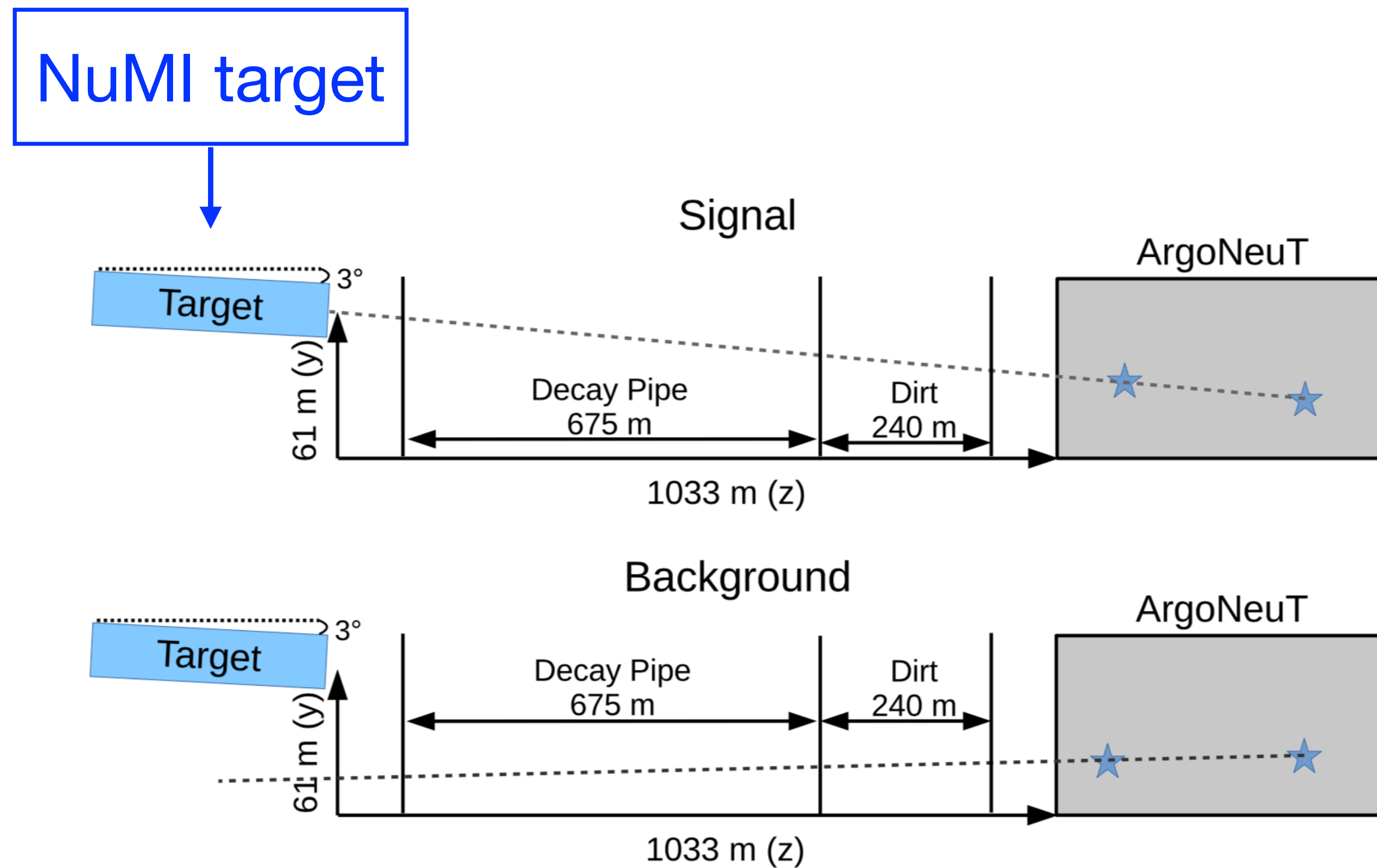
ArgoNeuT @ FermiLab: liquid argo neutrino detector



[Harnik et al., 1902.03246]

[ArgoNeuT, 1911.07996]

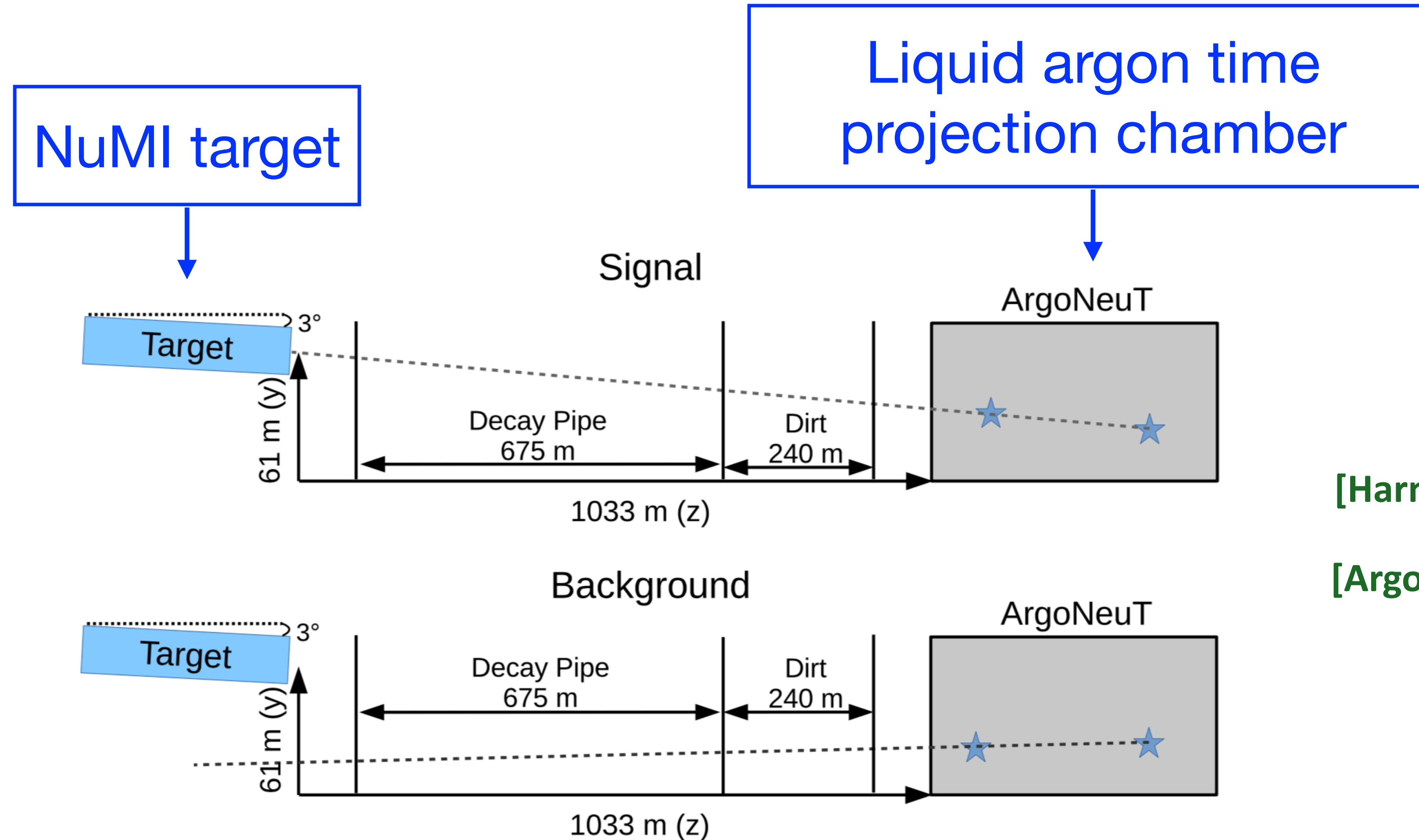
ArgoNeuT @ FermiLab: liquid argo neutrino detector



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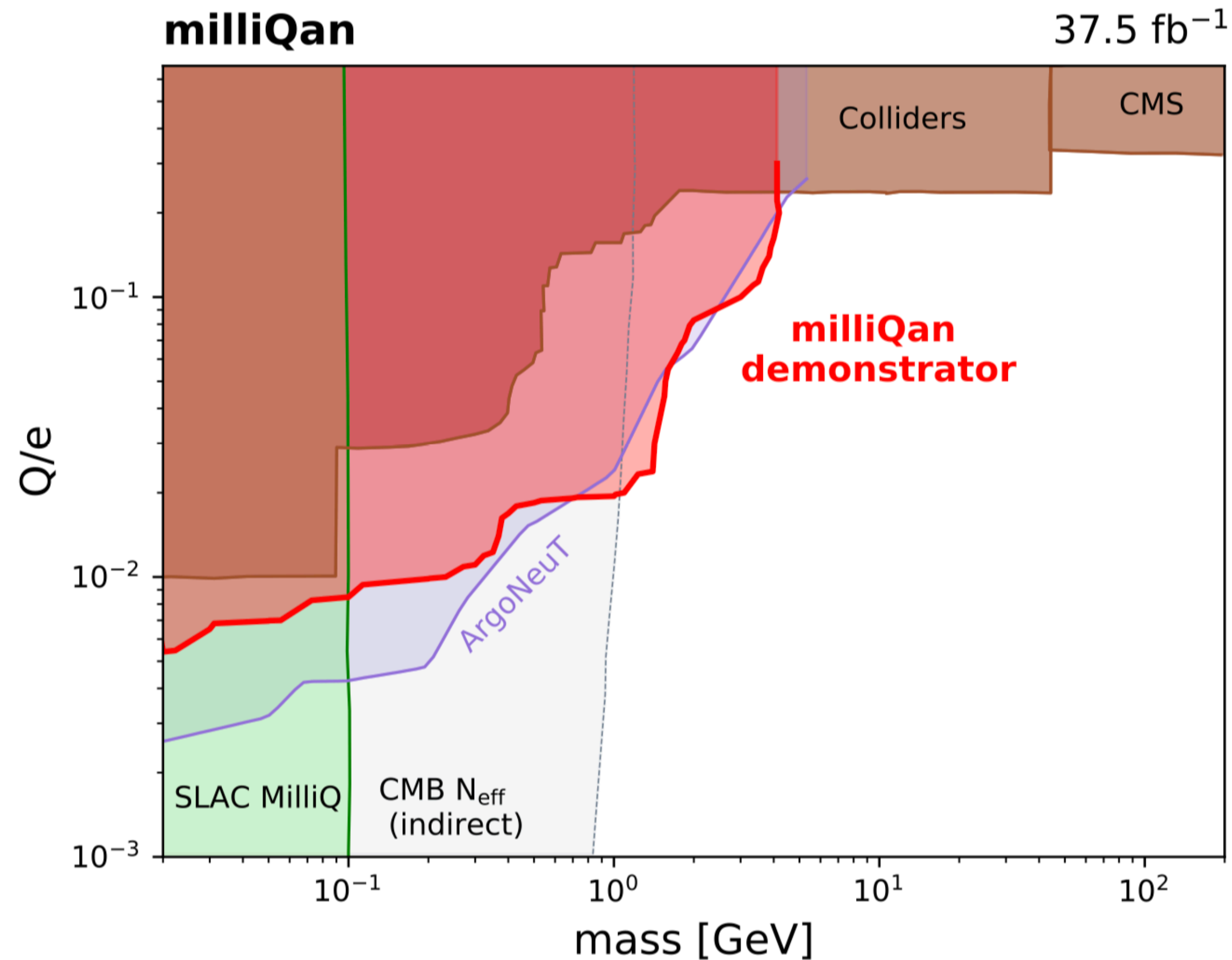
ArgoNeuT @ FermiLab: liquid argo neutrino detector



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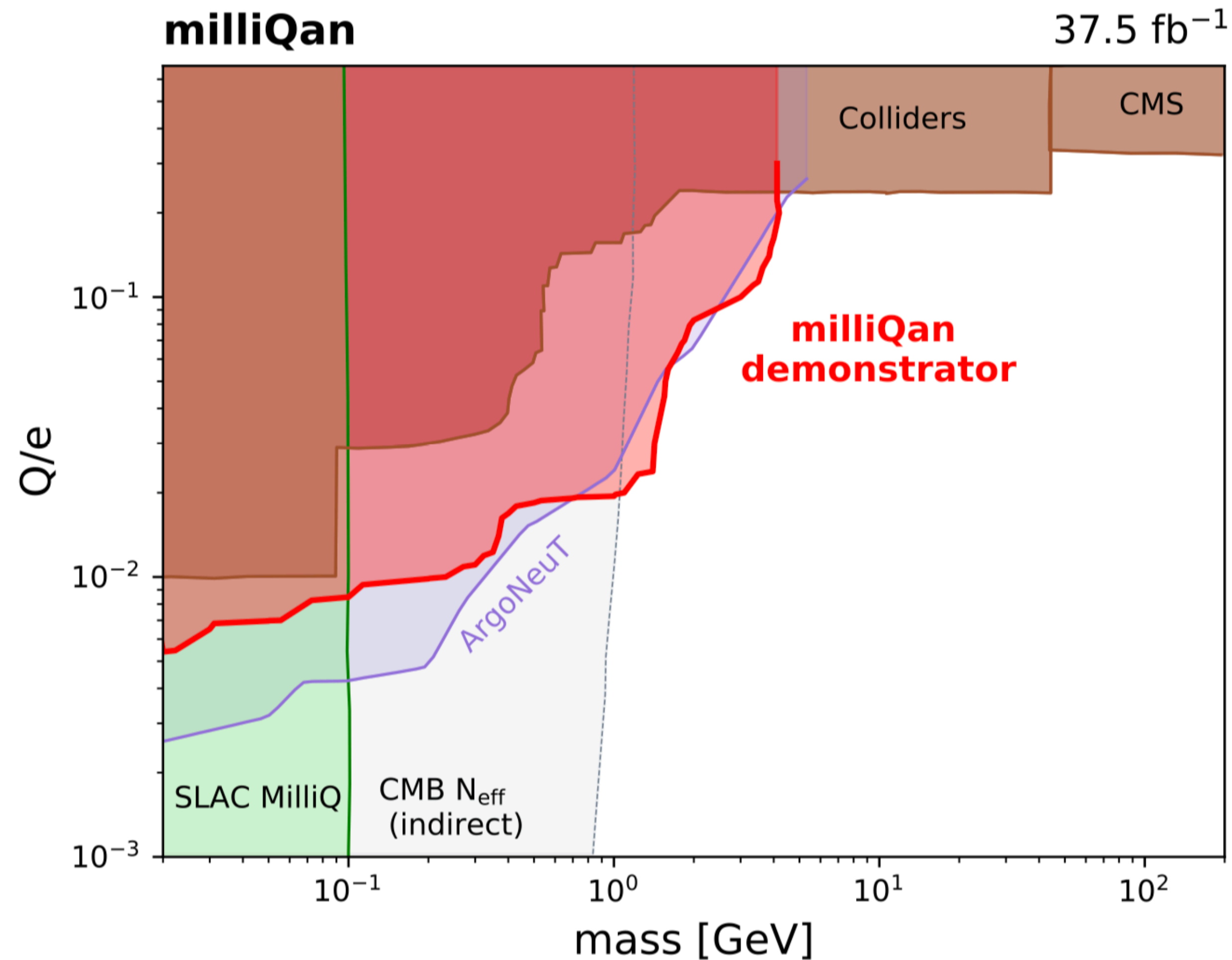
Limits from ArgoNeuT & MilliQan demonstrator (1%)



[ArgoNeuT, 1911.07996]

ArgoNeuT 10²⁰ POT

Limits from ArgoNeuT & MilliQan demonstrator (1%)



[ArgoNeuT, 1911.07996]

ArgoNeuT 10²⁰ POT

[milliQan demonstrator, 2005.06518]

1% of total detector

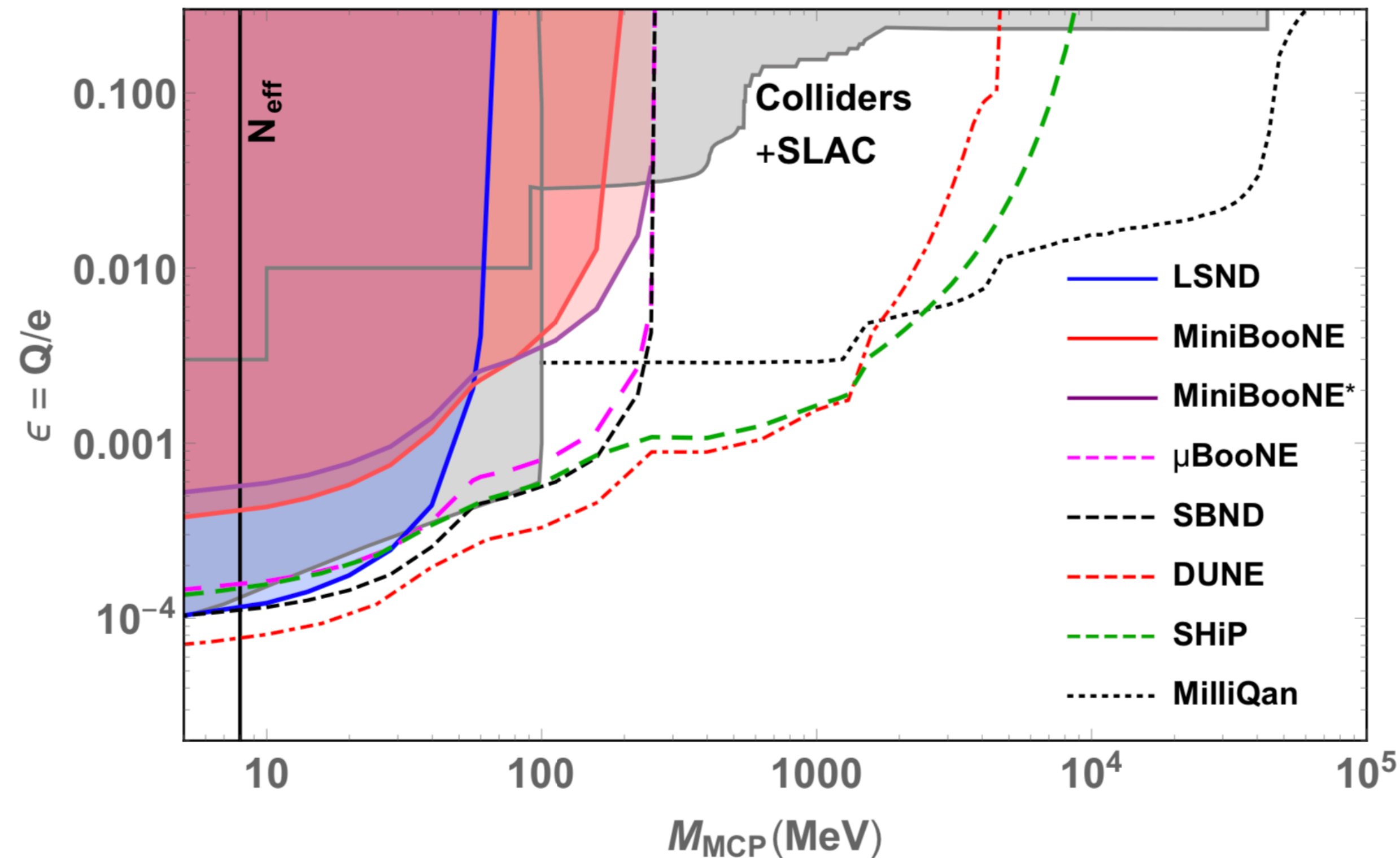
37/fb in 2018

MCP scatters w/ neutrino experiment target

MCP produced in proton fixed-target experiments



MCP scatters w/ target (electron) in the neutrino detector



[Magill et al., 1806.03310]

solid: data
dashed: projection

Some future experiments on millicharge (incomplete)

LDMX: electron fixed target

NA64: muon fixed target

FerMINI: scintillators @ proton fixed target

SUBMET: scintillators @ JPARC

neutrino experiments

DM experiments

3 electron colliders' sensitivity

[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]

Probing millicharge at electron colliders

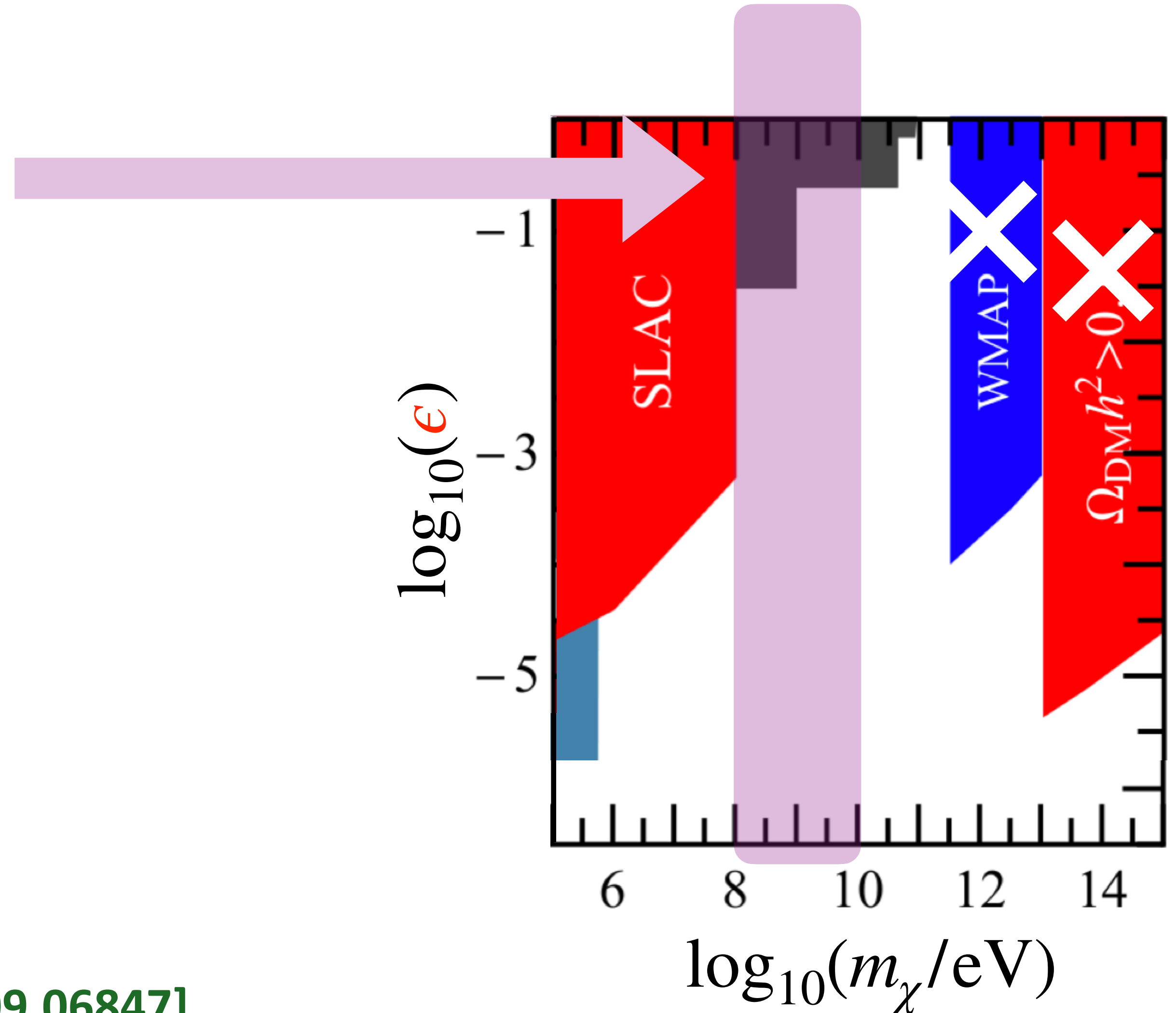
0.1-10 GeV

accessible at
electron colliders

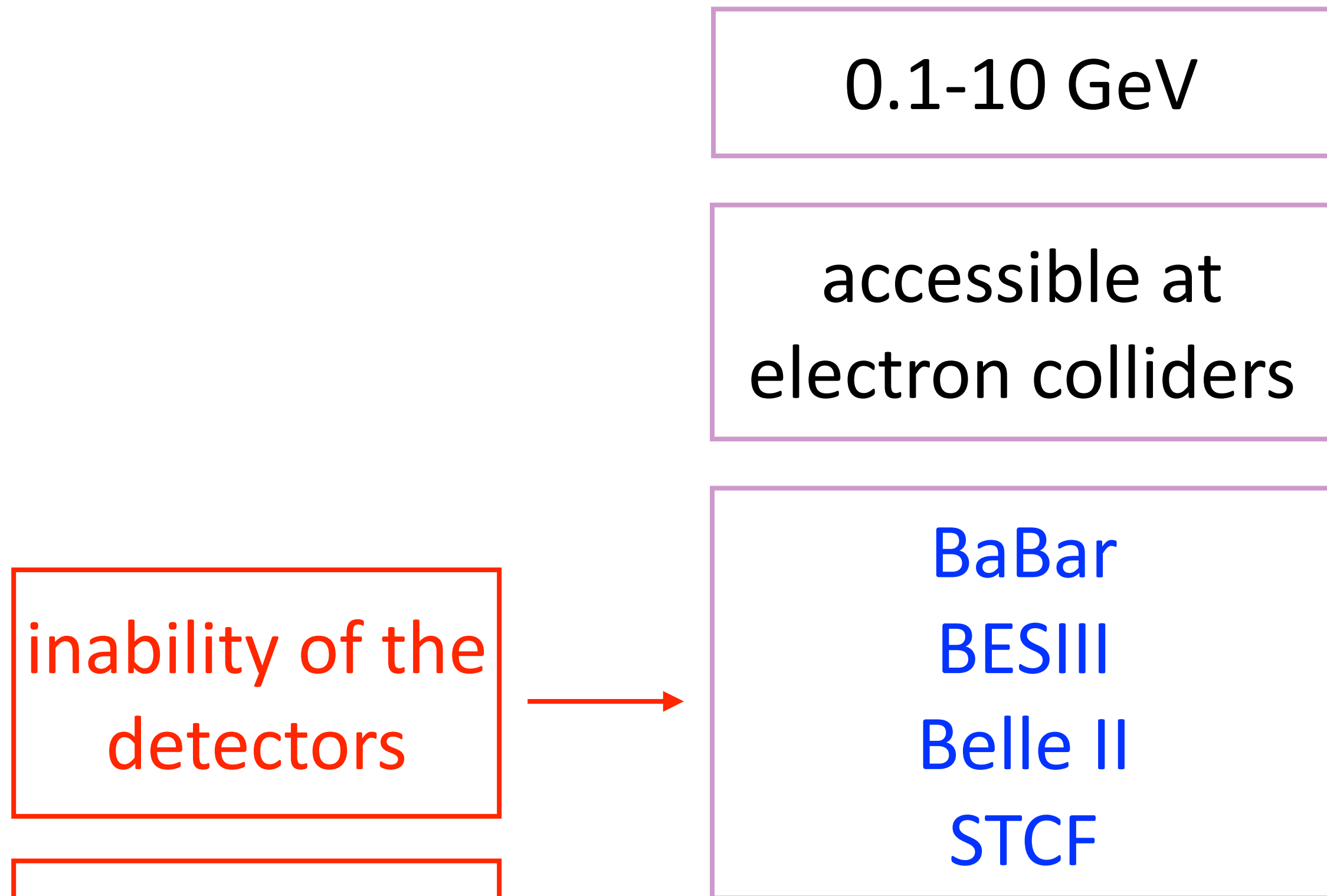
BaBar
BESIII
Belle II
STCF

[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]

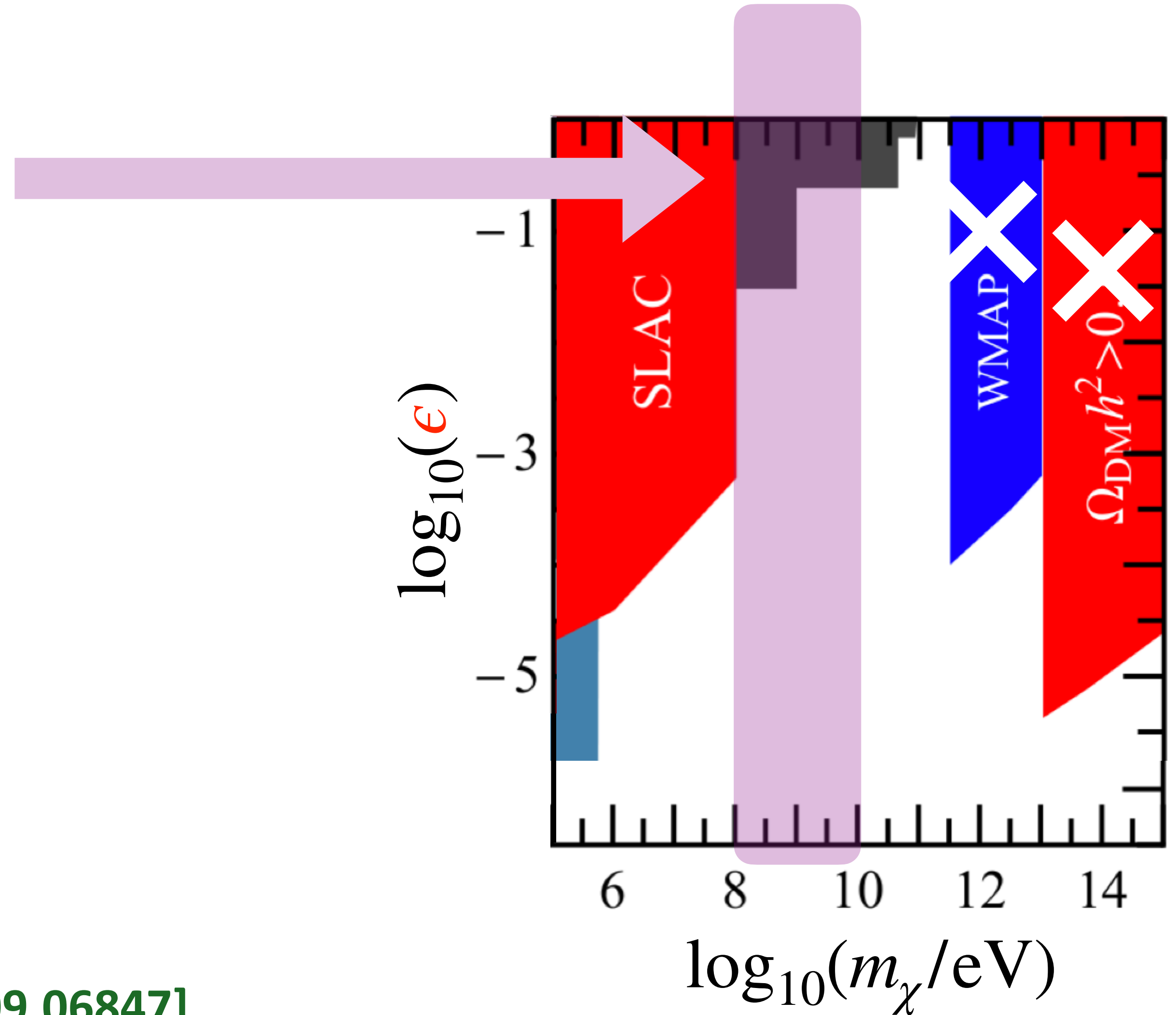


Probing millicharge at electron colliders



[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]



Process to search for millicharged particles

very small ionization
signal from millicharge



mono-photon @
electron colliders

[ZL, Zhang, 1808.00983]

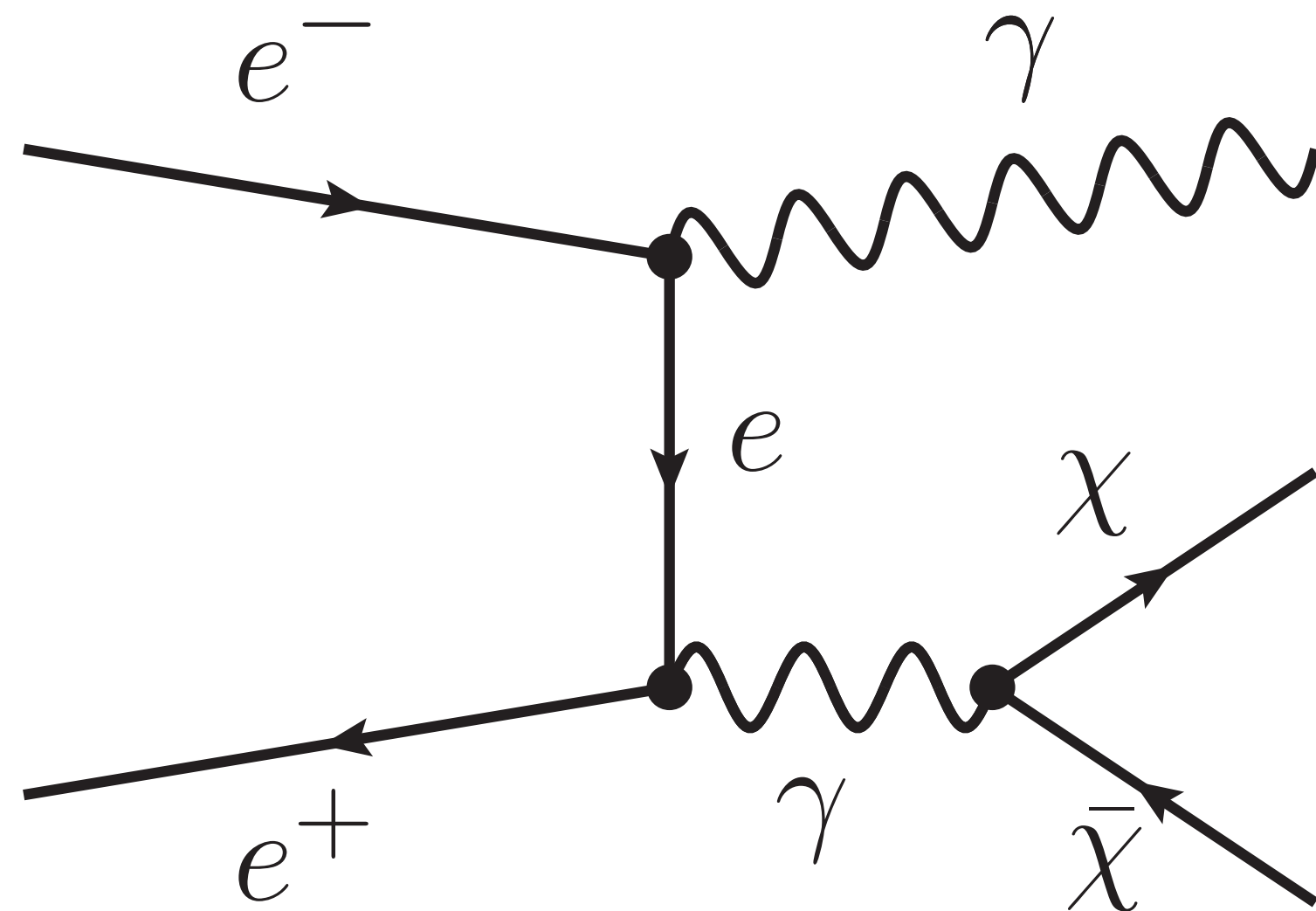
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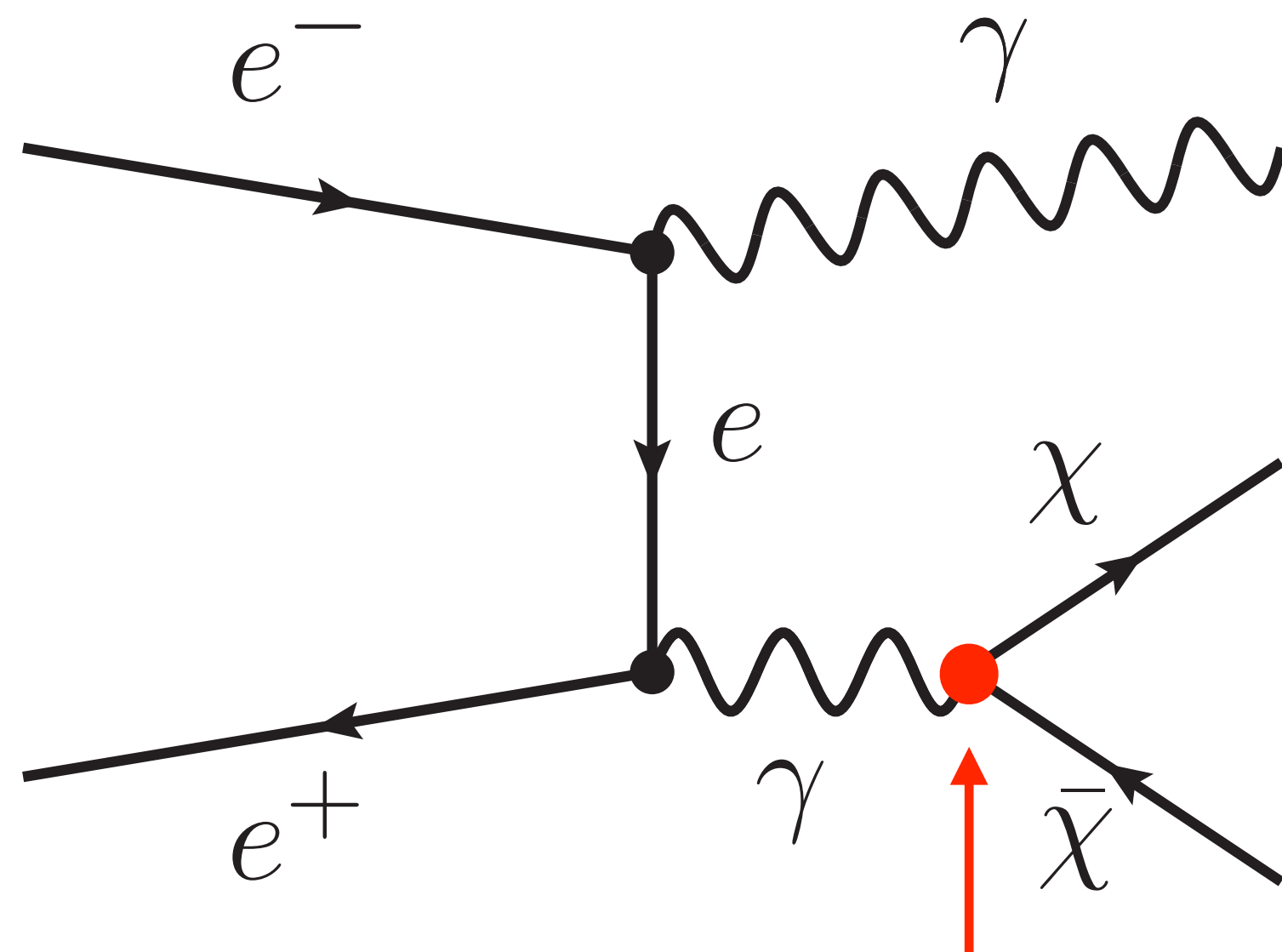
Process to search for millicharged particles

very small ionization
signal from millicharge



mono-photon @
electron colliders

[ZL, Zhang, 1808.00983]



millicharge vertex: $e \epsilon A_{\mu}^{\gamma} \bar{\chi} \gamma^{\mu} \chi$

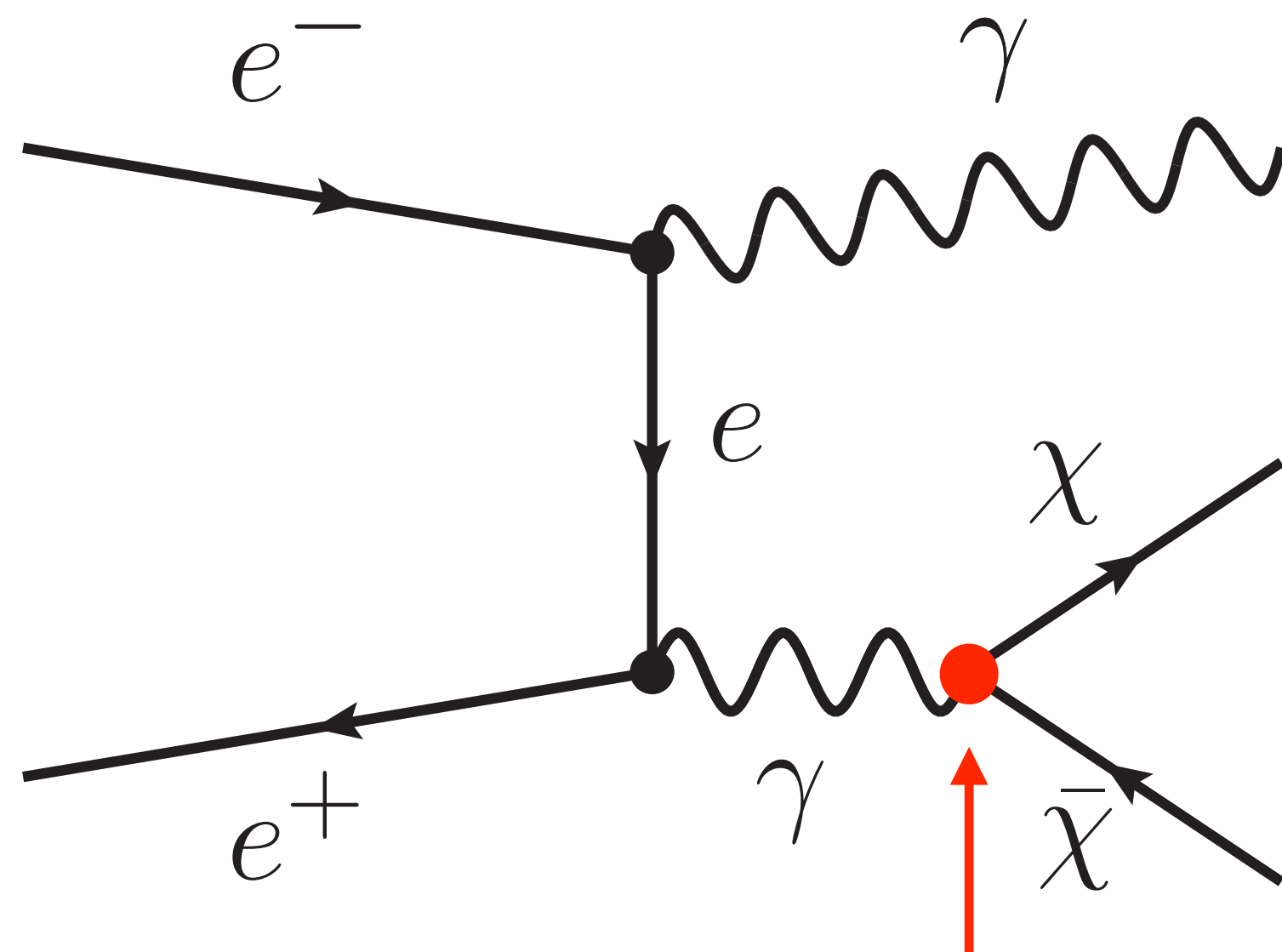
Process to search for millicharged particles

very small ionization
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mono-photon @
electron colliders

[ZL, Zhang, 1808.00983]



“invisible” at
electron colliders

millicharge vertex: $e \epsilon A_{\mu}^{\gamma} \bar{\chi} \gamma^{\mu} \chi$

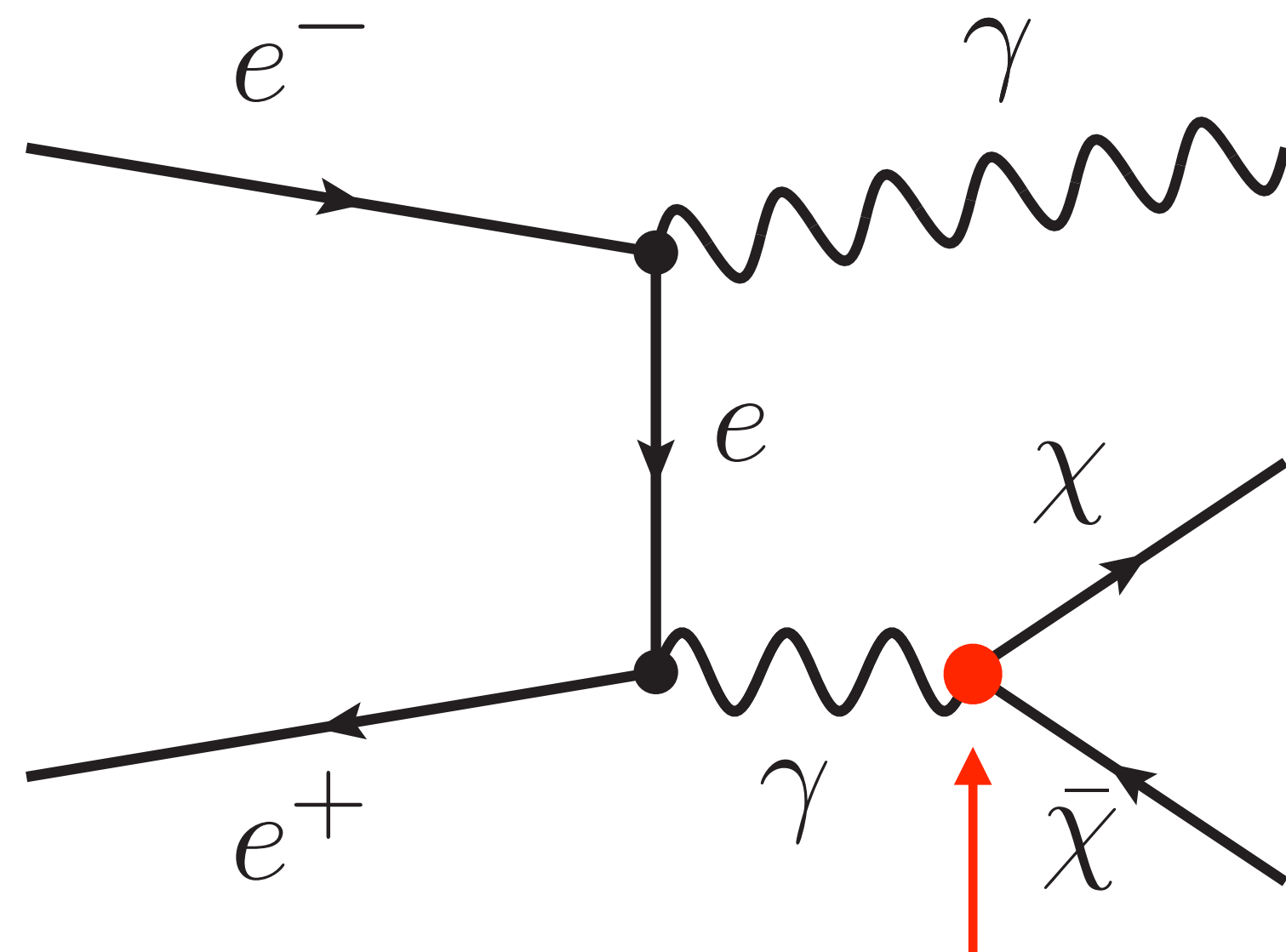
Process to search for millicharged particles

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signal from millicharge



mono-photon @
electron colliders

[ZL, Zhang, 1808.00983]



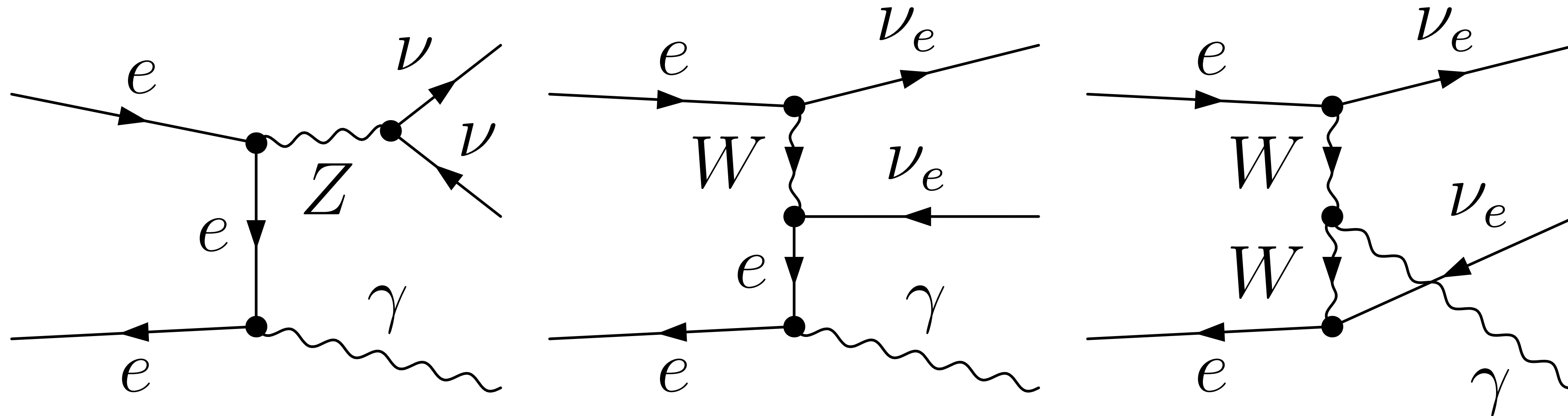
monophoton

“invisible” at
electron colliders

millicharge vertex: $e \epsilon A_{\mu}^{\gamma} \bar{\chi} \gamma^{\mu} \chi$

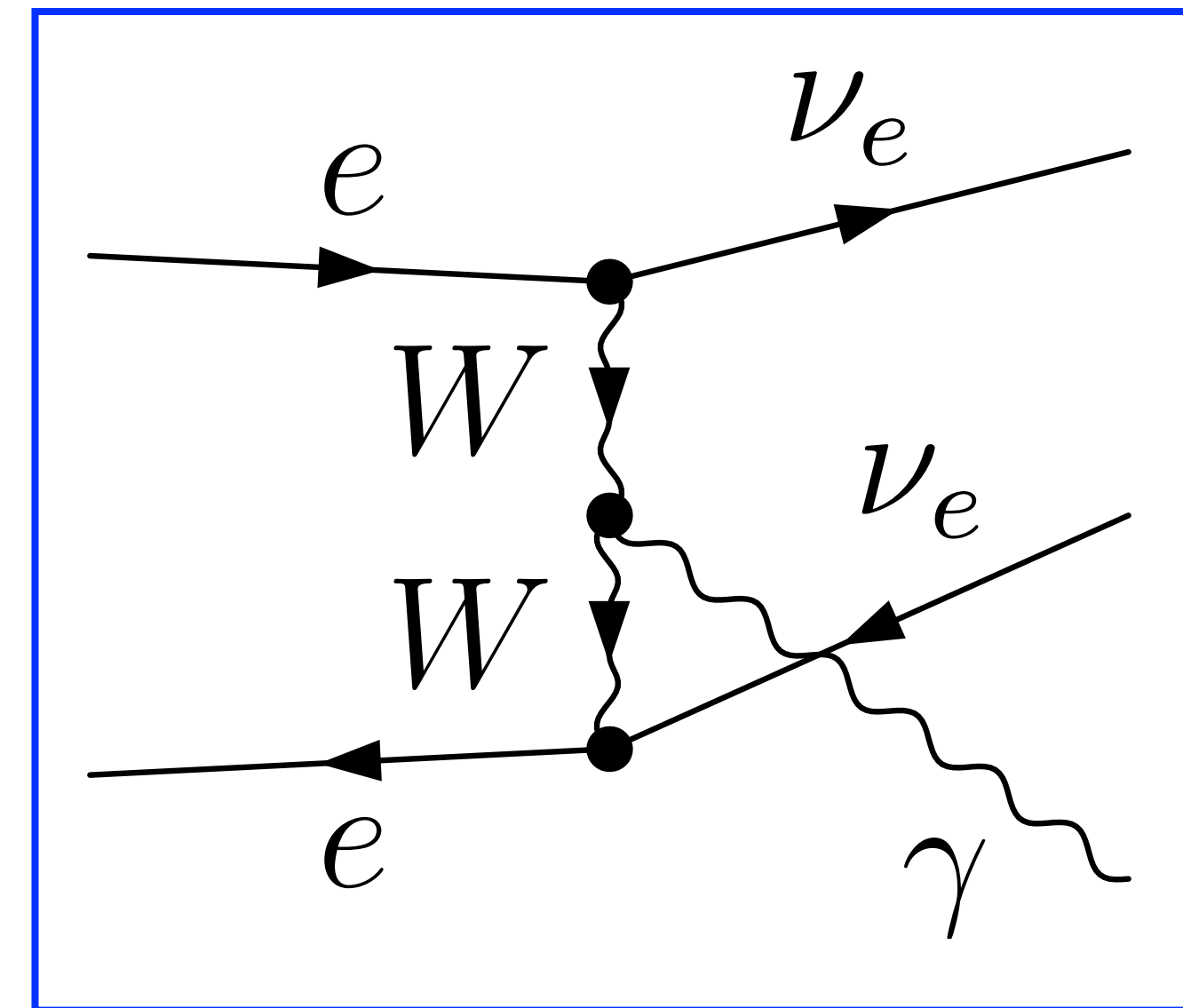
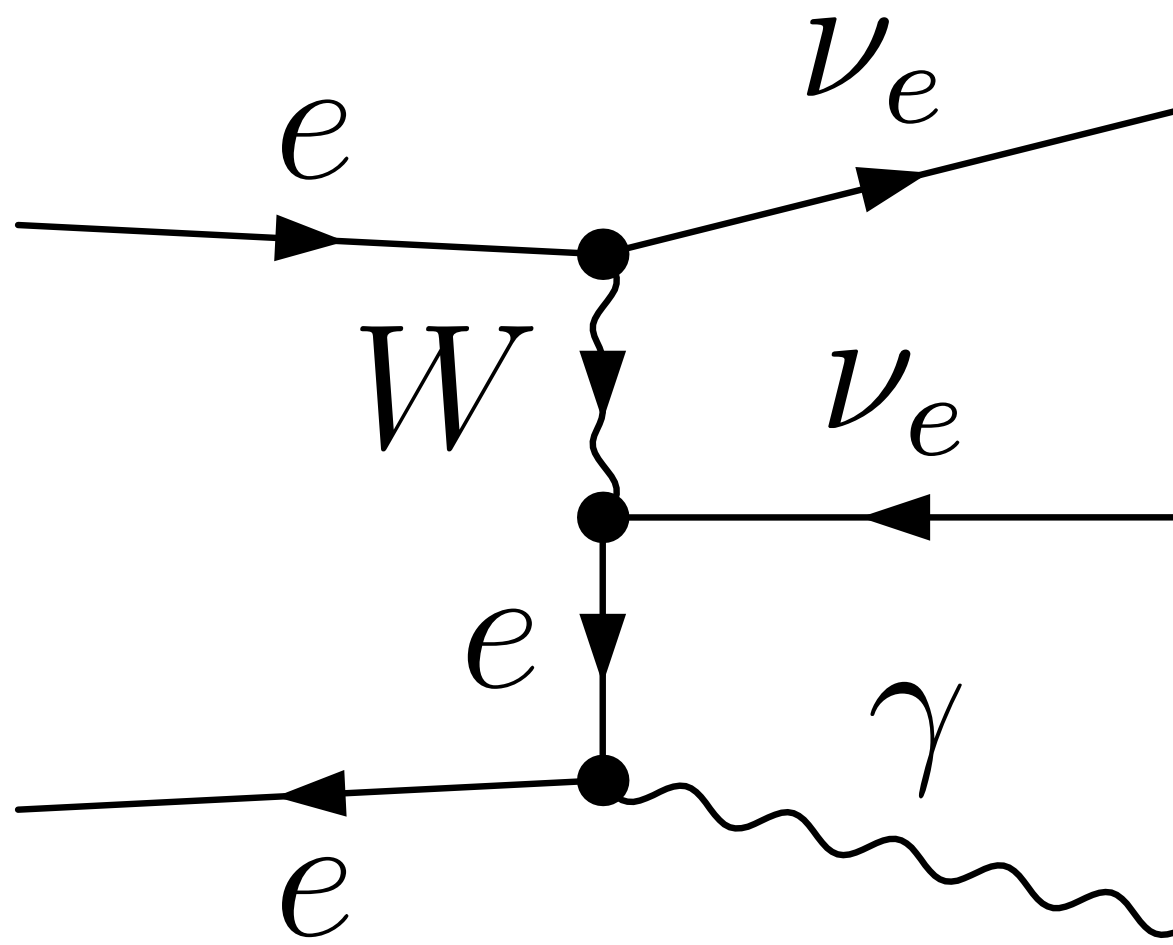
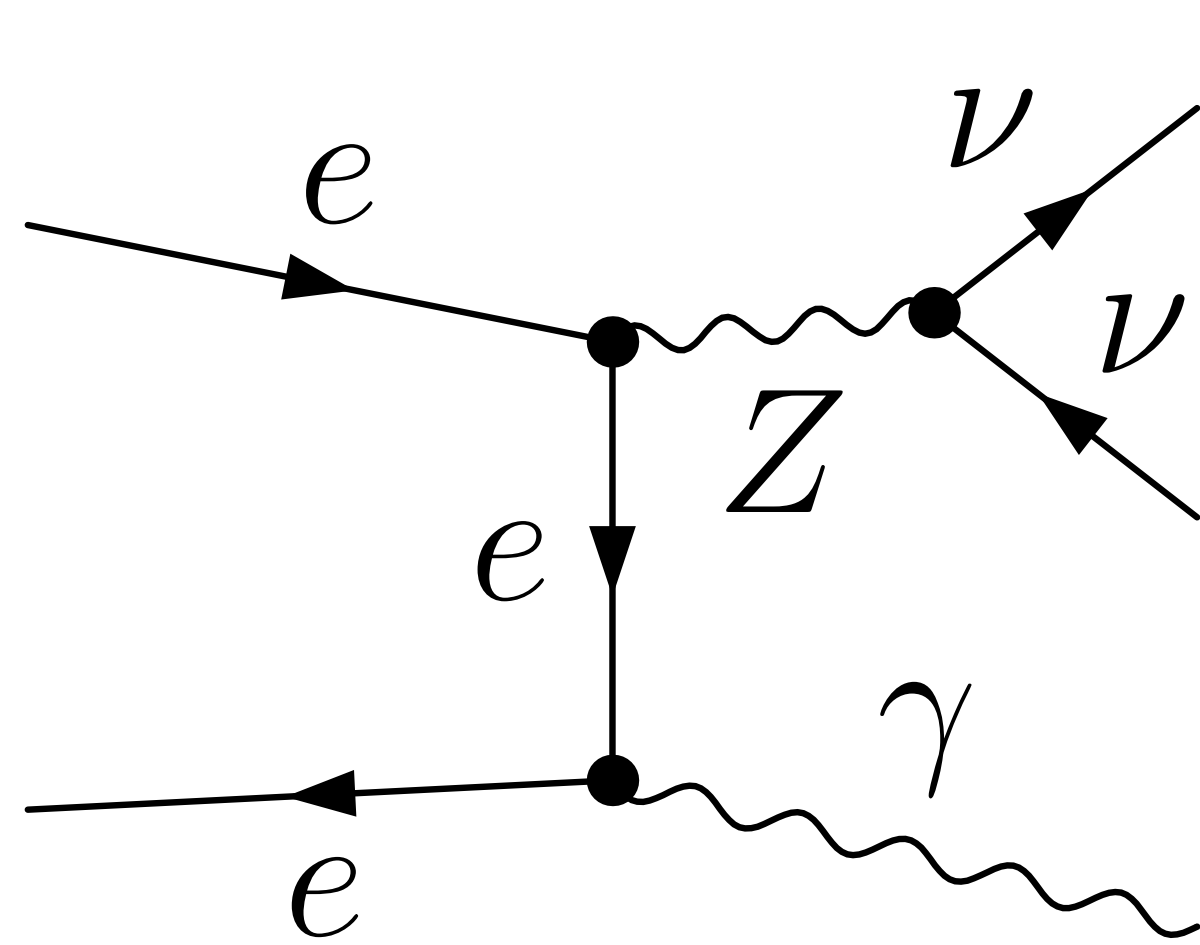
Irreducible BG (monophoton plus 2 neutrinos)

Irreducible BG: $e^+e^- \rightarrow \gamma\nu\nu$



Irreducible BG (monophoton plus 2 neutrinos)

Irreducible BG: $e^+e^- \rightarrow \gamma\nu\nu$



small

monophoton cross section @ electron colliders

millicharge process: $e^+ e^- \rightarrow \chi \chi \gamma$

[ZL, Zhang, 1808.00983]

$$\frac{d\sigma}{dE_\gamma dz_\gamma} = \frac{8\alpha^3 \varepsilon^2 (1 + 2m_\chi^2/s_\gamma) \beta_\chi}{3sE_\gamma (1 - z_\gamma^2)} \left[1 + \frac{E_\gamma^2}{s_\gamma} (1 + z_\gamma^2) \right]$$

$$z_\gamma \equiv \cos \theta_\gamma \quad s_\gamma = s - 2\sqrt{s}E_\gamma \quad \beta_\chi = (1 - 4m_\chi^2/s_\gamma)^{1/2}$$

monophoton cross section @ electron colliders

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$$z_\gamma \equiv \cos \theta_\gamma \quad s_\gamma = s - 2\sqrt{s}E_\gamma \quad \beta_\chi = (1 - 4m_\chi^2/s_\gamma)^{1/2}$$

irreducible BG: $e^+ e^- \rightarrow \gamma \nu \nu$

[Ma, Okada 1978]

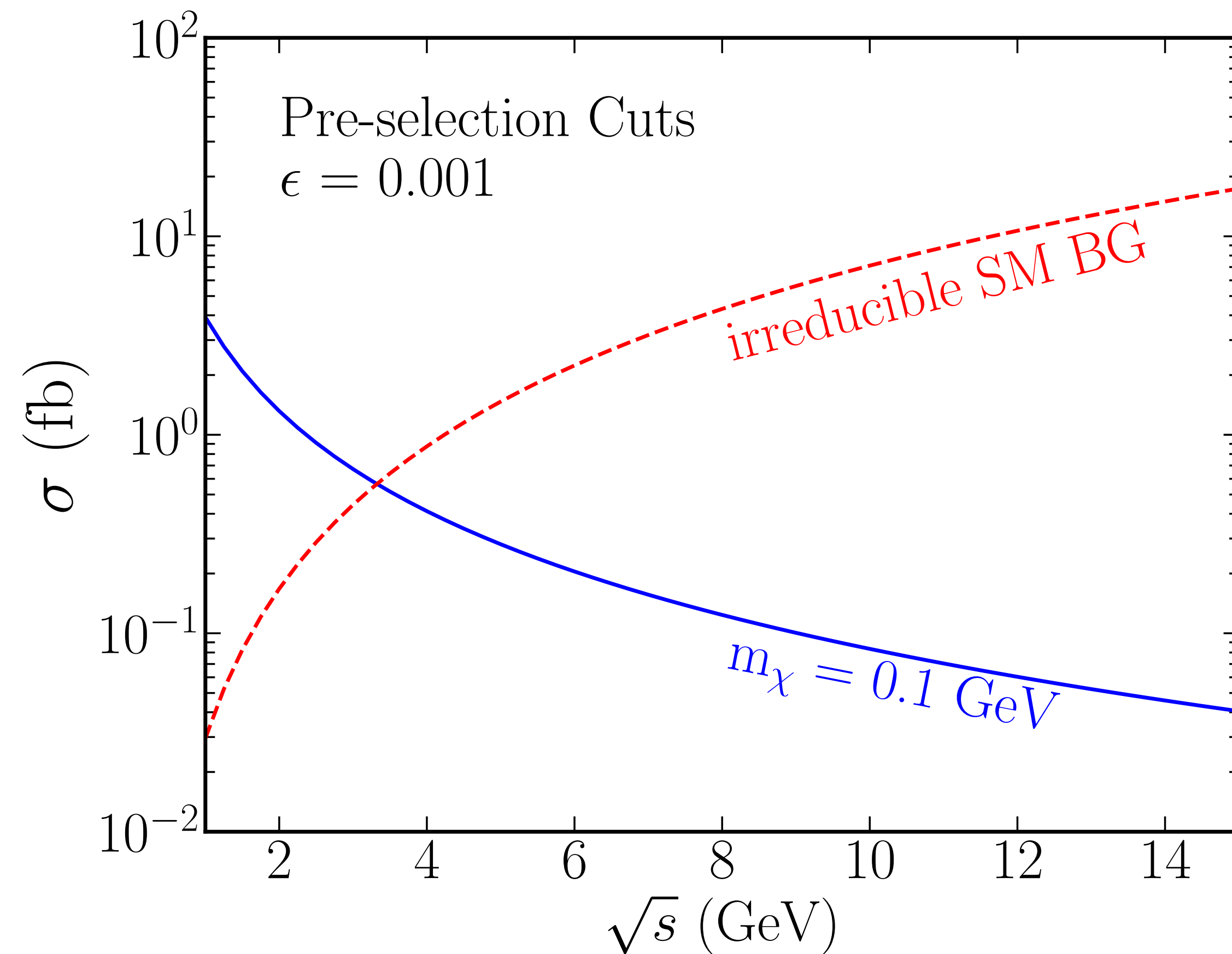
$$\frac{d\sigma}{dE_\gamma dz_\gamma} = \frac{\alpha G_F^2 s_\gamma^2}{4\pi^2 s E_\gamma (1 - z_\gamma^2)} f(s_W) \left[1 + \frac{E_\gamma^2}{s_\gamma} (1 + z_\gamma^2) \right]$$

[Gaemers + 1979]

$$s_W \equiv \sin \theta_W \quad f(s_W) = 8s_W^4 - 4s_W^2/3 + 1$$

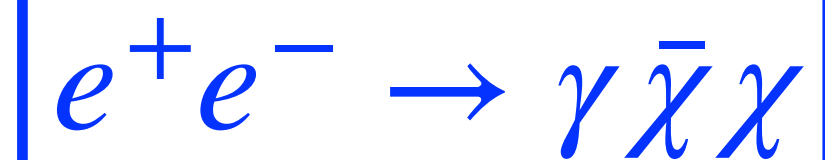
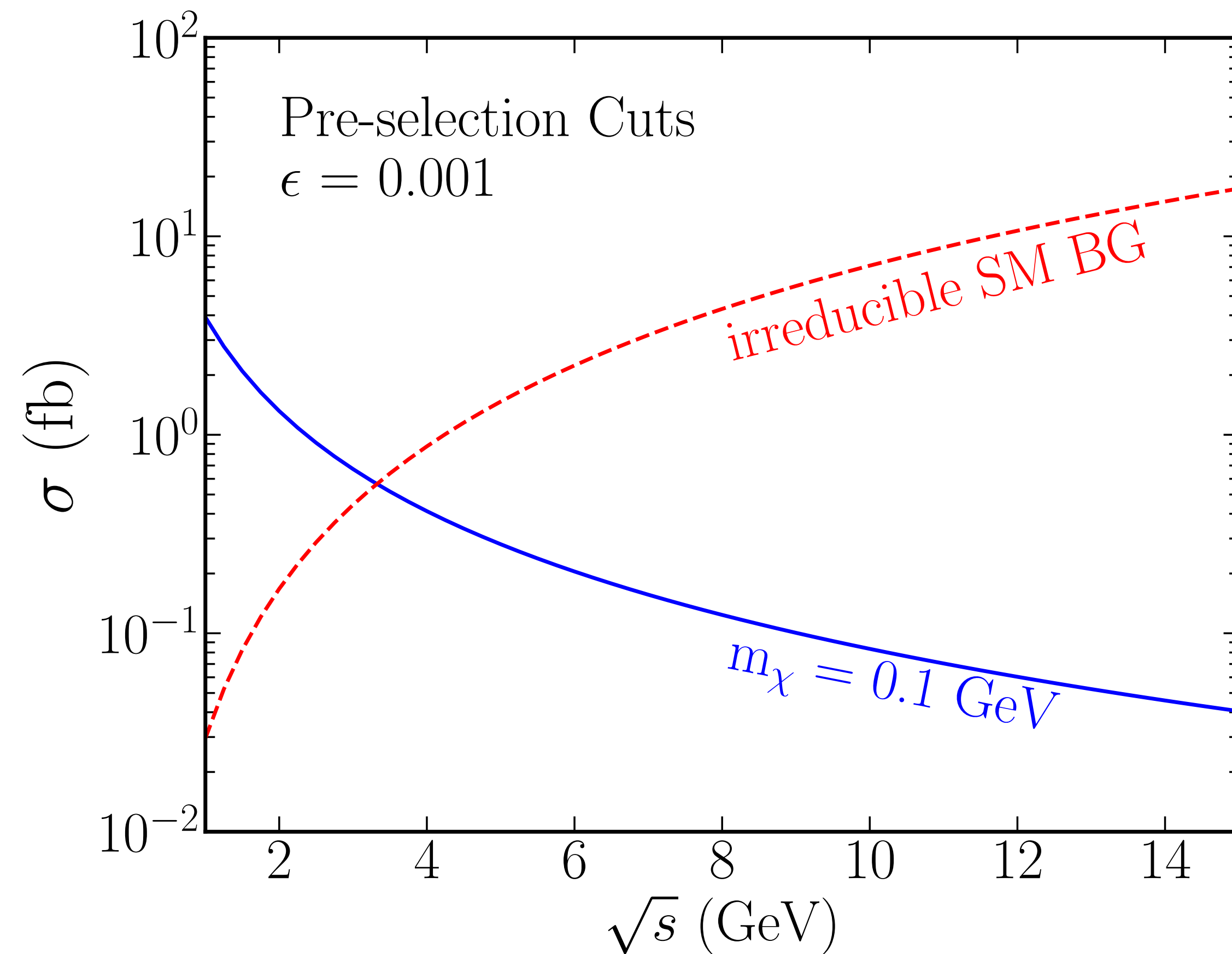
“Low” colliding energy is better to probe MCPs

if irreducible BG is the only important BG



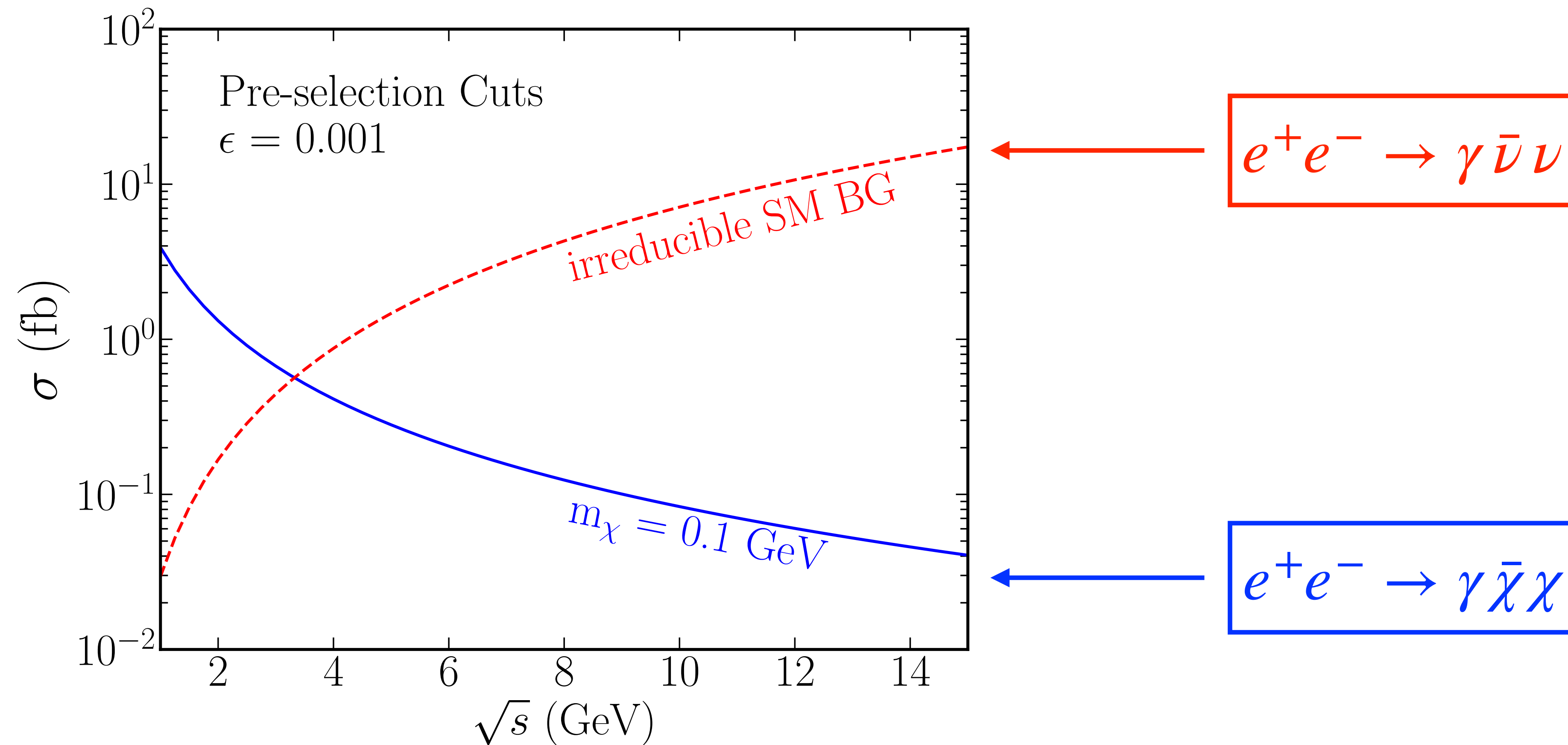
“Low” colliding energy is better to probe MCPs

if irreducible BG is the only important BG



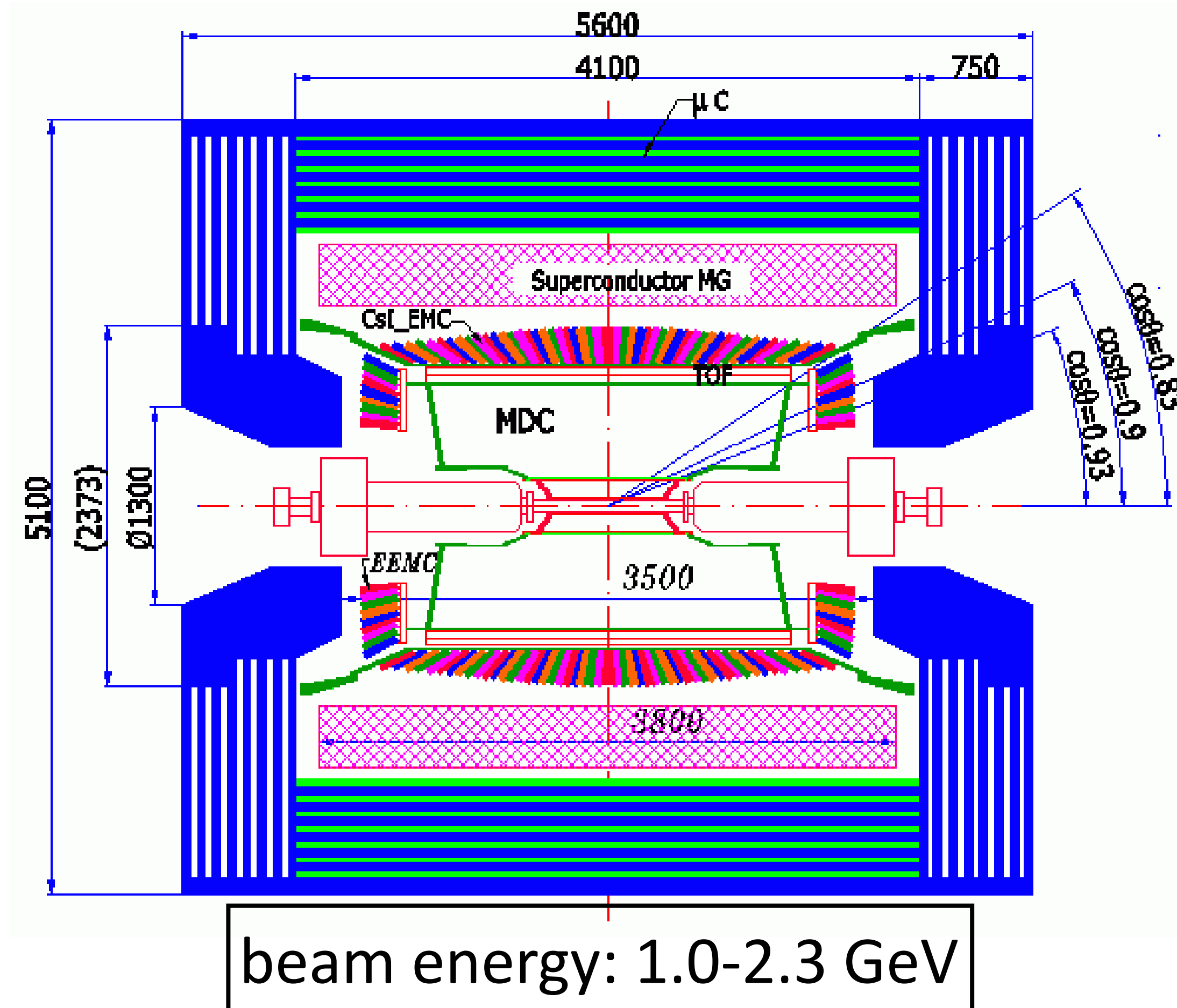
“Low” colliding energy is better to probe MCPs

if irreducible BG is the only important BG



BESIII detectors & reducible BG

[Chao, Wang et al. 0809.1869]



Main drift chamber (MDC)

$$|\cos(\Theta_Y)| < 0.93$$

Time-of-Flight (TOF)

$$|\cos(\Theta_Y)| < 0.83$$

$$0.85 < |\cos(\Theta_Y)| < 0.95$$

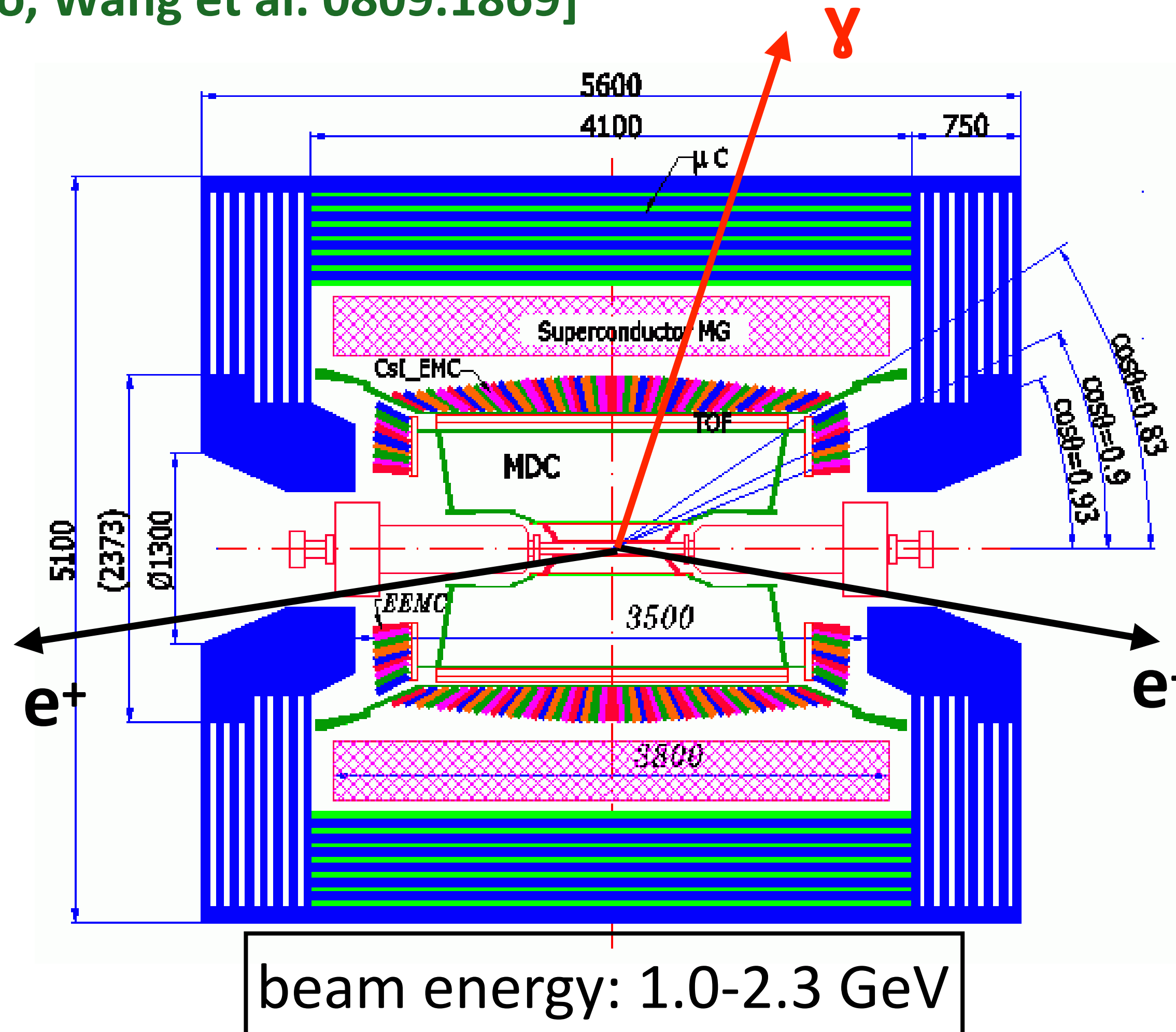
Electromagnetic calorimeter (EMC)

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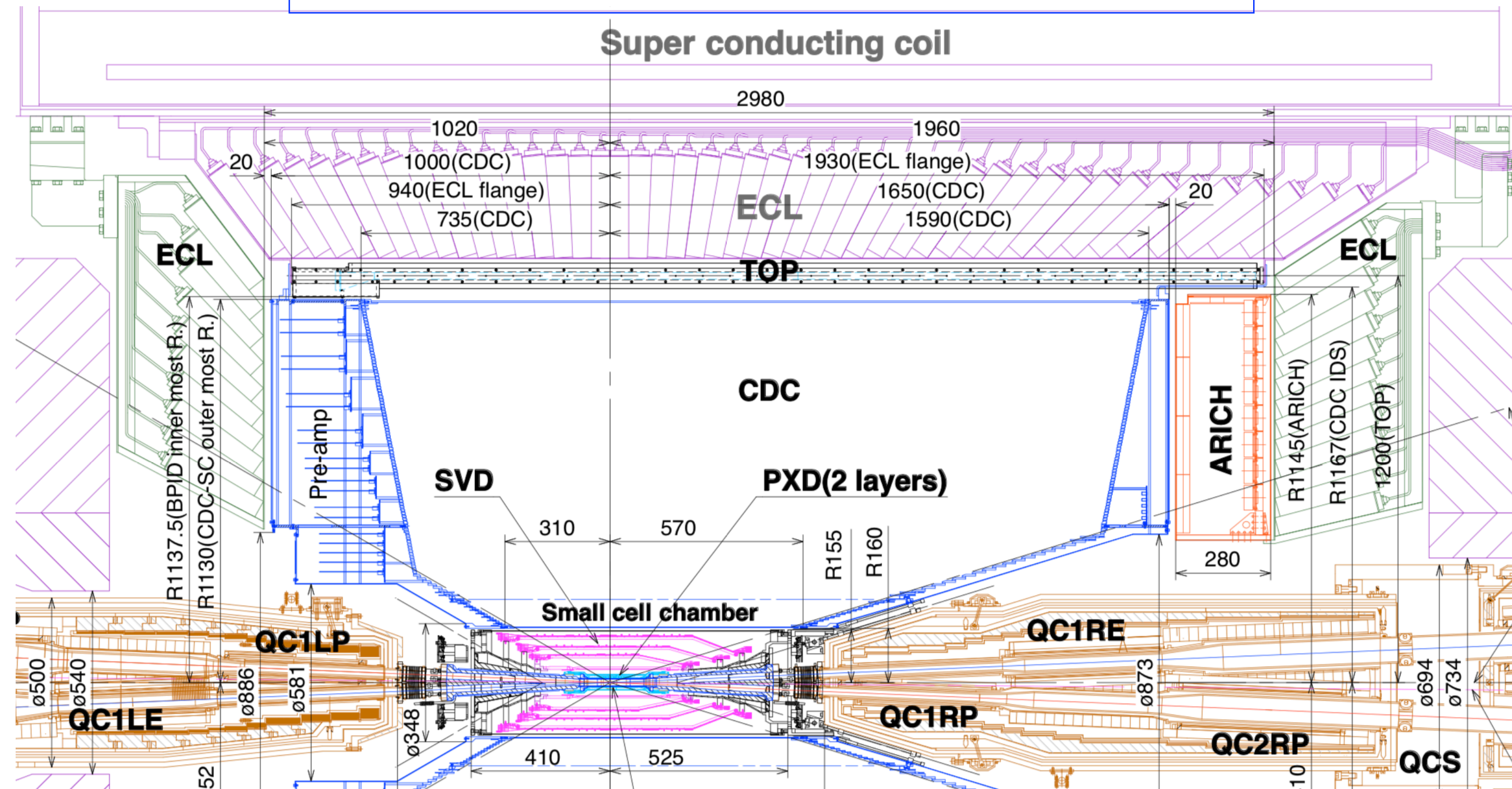
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Belle II has several uncovered angular regions

7 GeV electron collides w/ 4 GeV positron



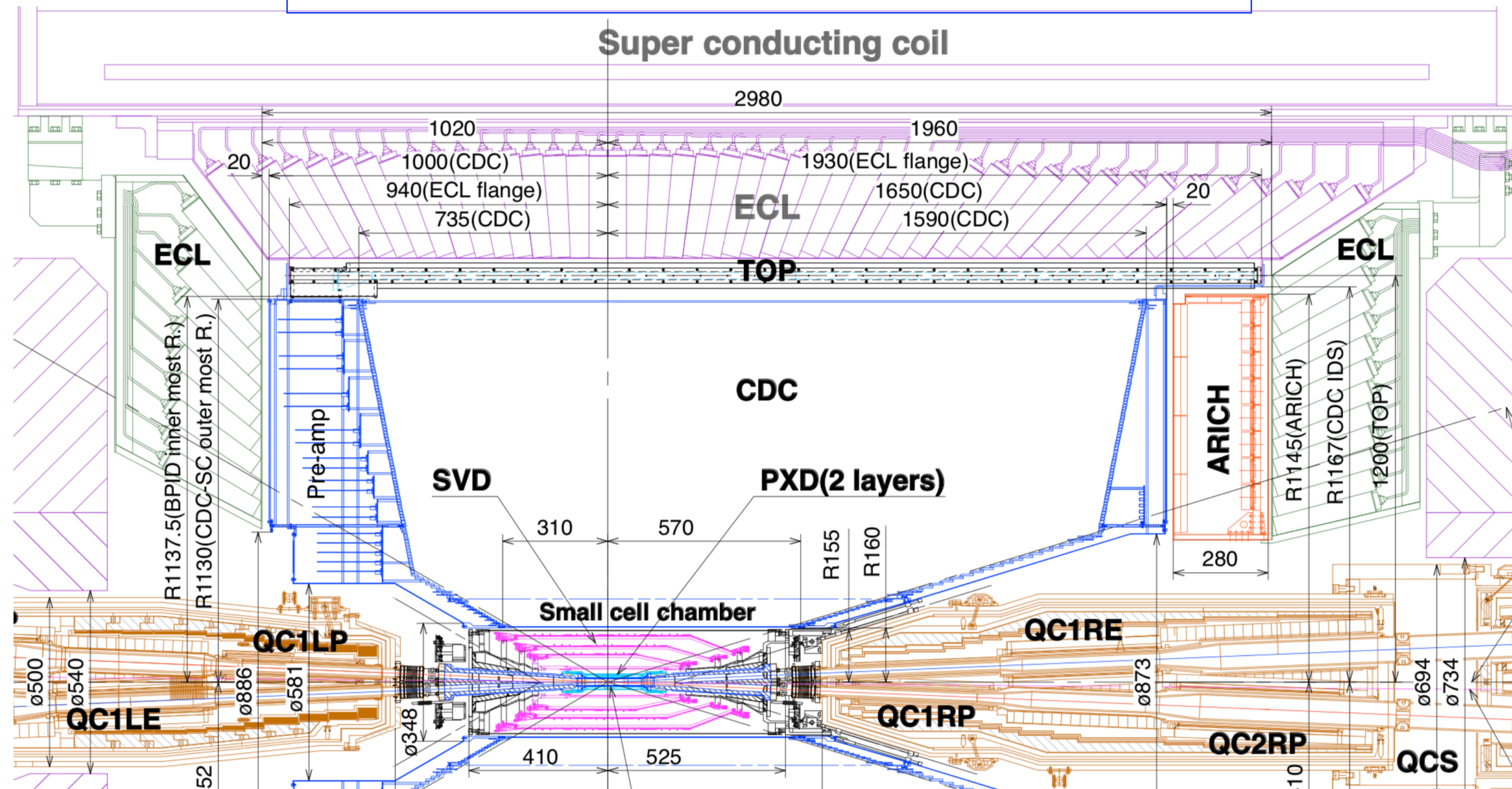
Belle II has several uncovered angular regions

7 GeV electron collides w/ 4 GeV positron

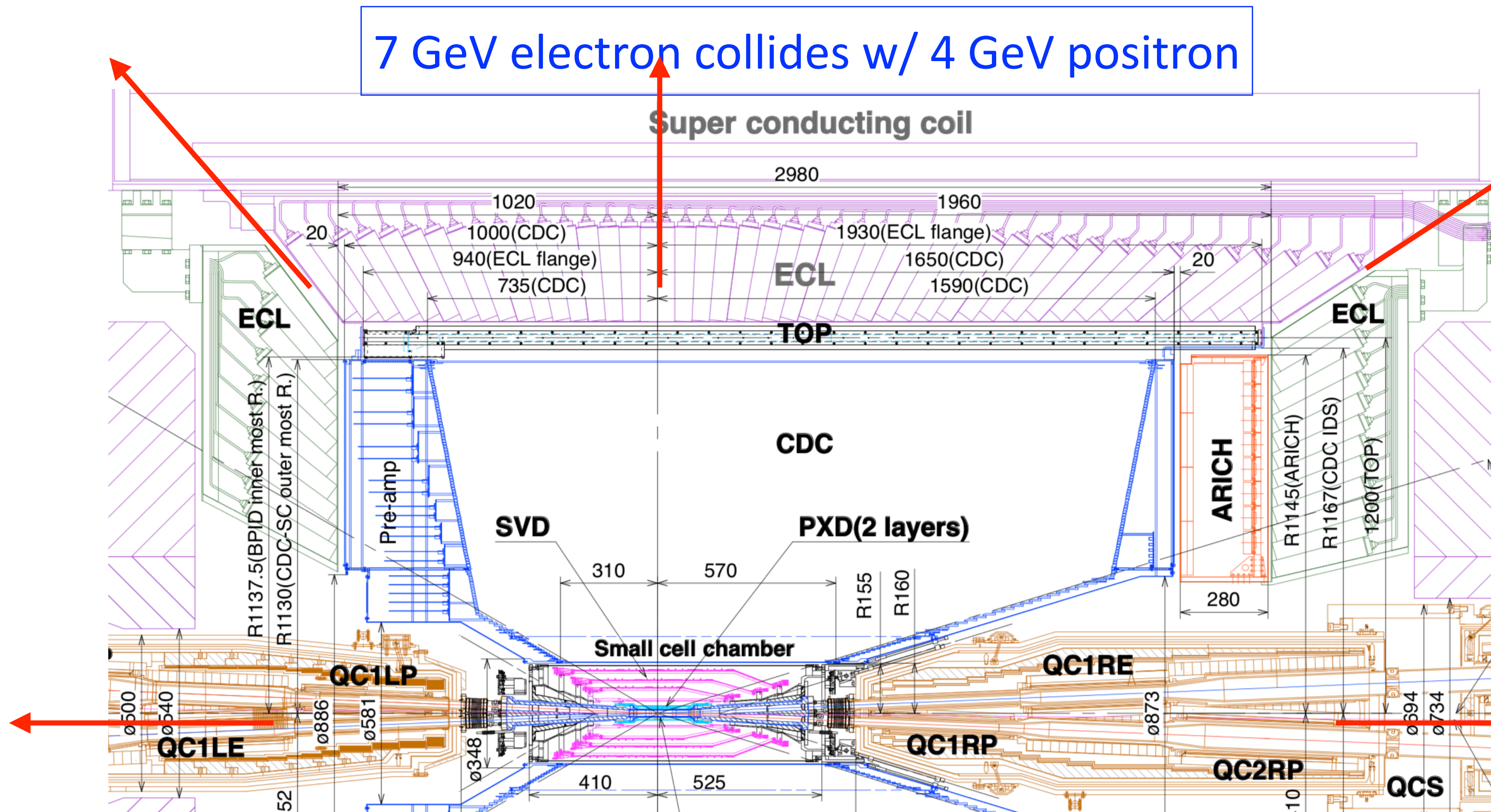
ECL angles
(lab frame)

- $12.4^\circ < \theta < 31.4^\circ$
- $32.2^\circ < \theta < 128.7^\circ$
- $130.7^\circ < \theta < 155.1^\circ$

[Belle II 1808.10567]



Belle II has several uncovered angular regions



ECL angles
(lab frame)

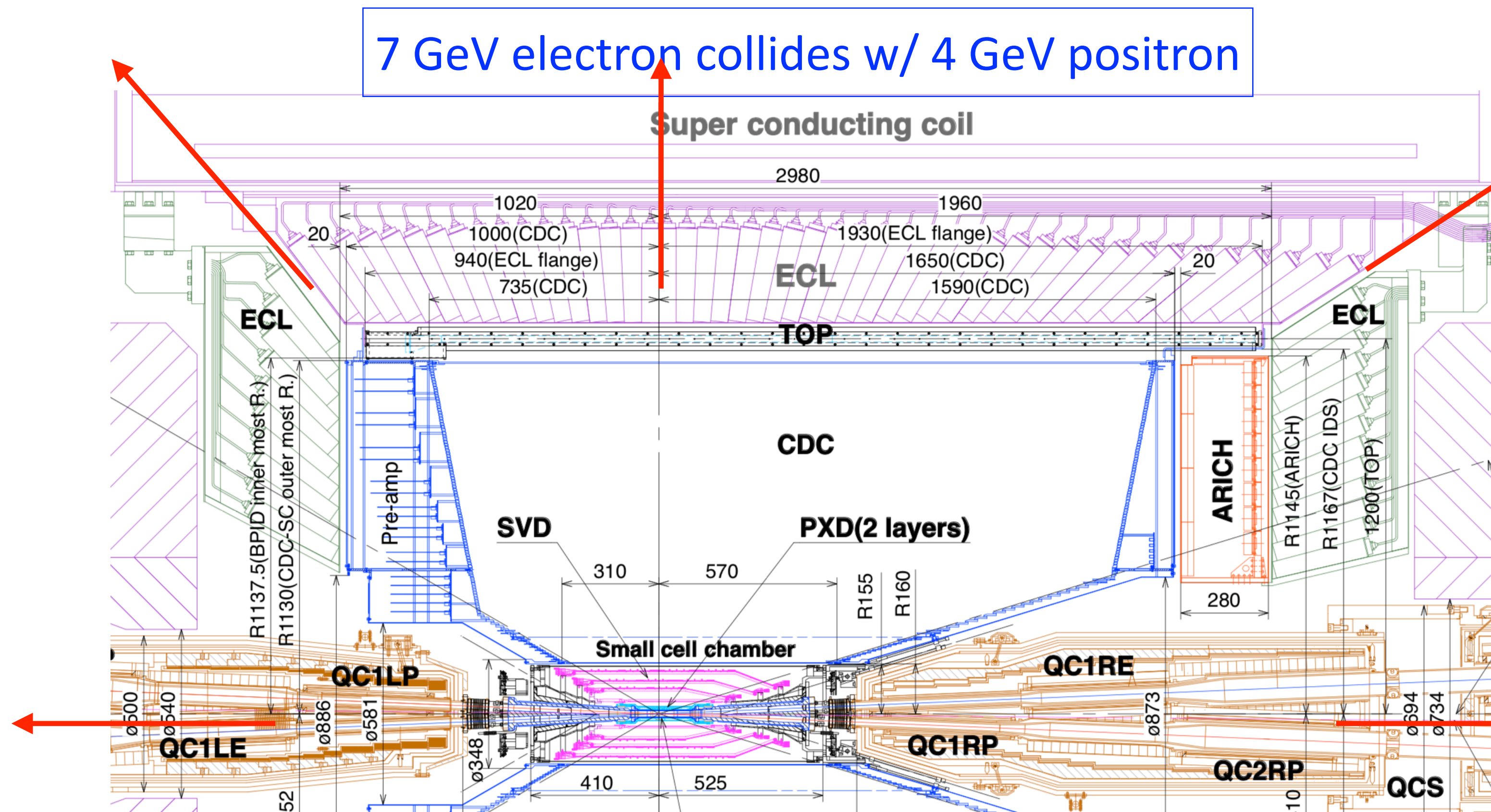
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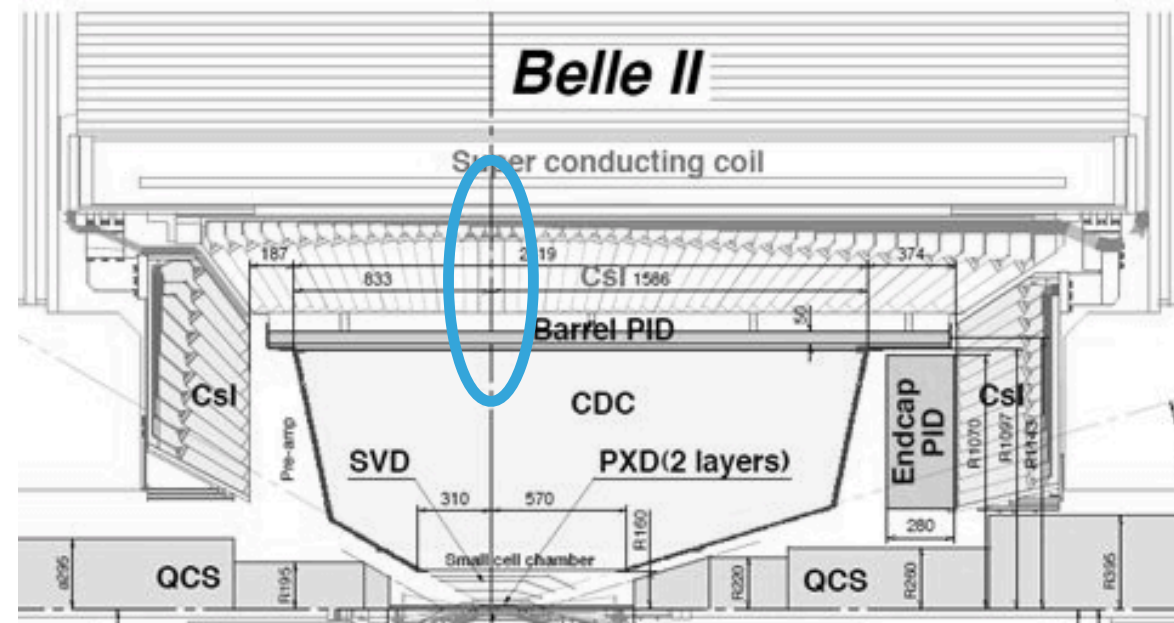
reducible BG

BG due to ECL gaps (gBG)

BG due to beam (bBG)

[taken from Torben Ferber's talk]

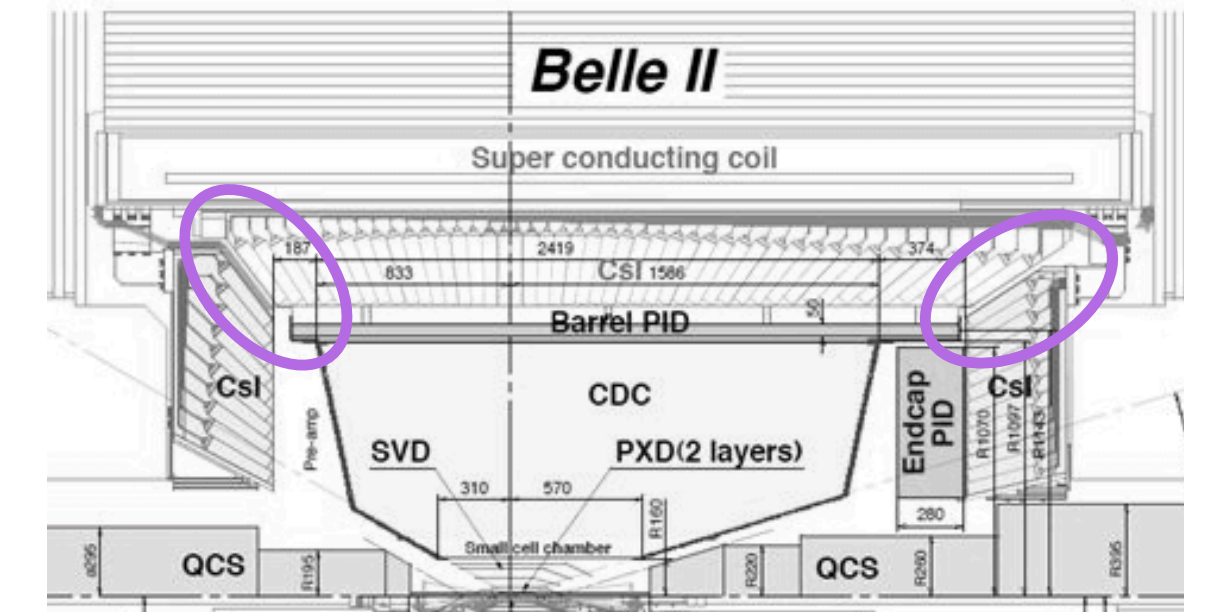
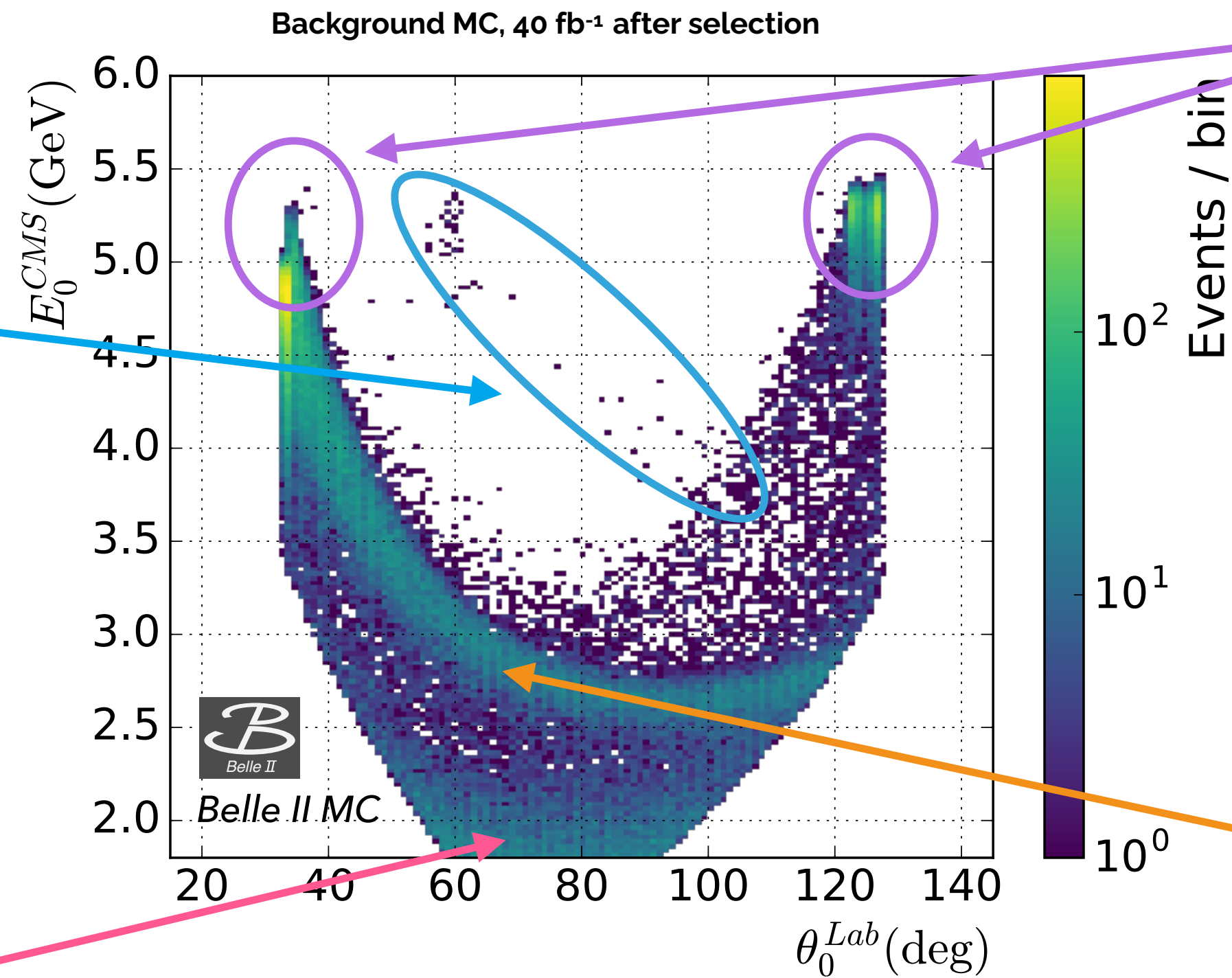
B: Invisible Dark Photon searches



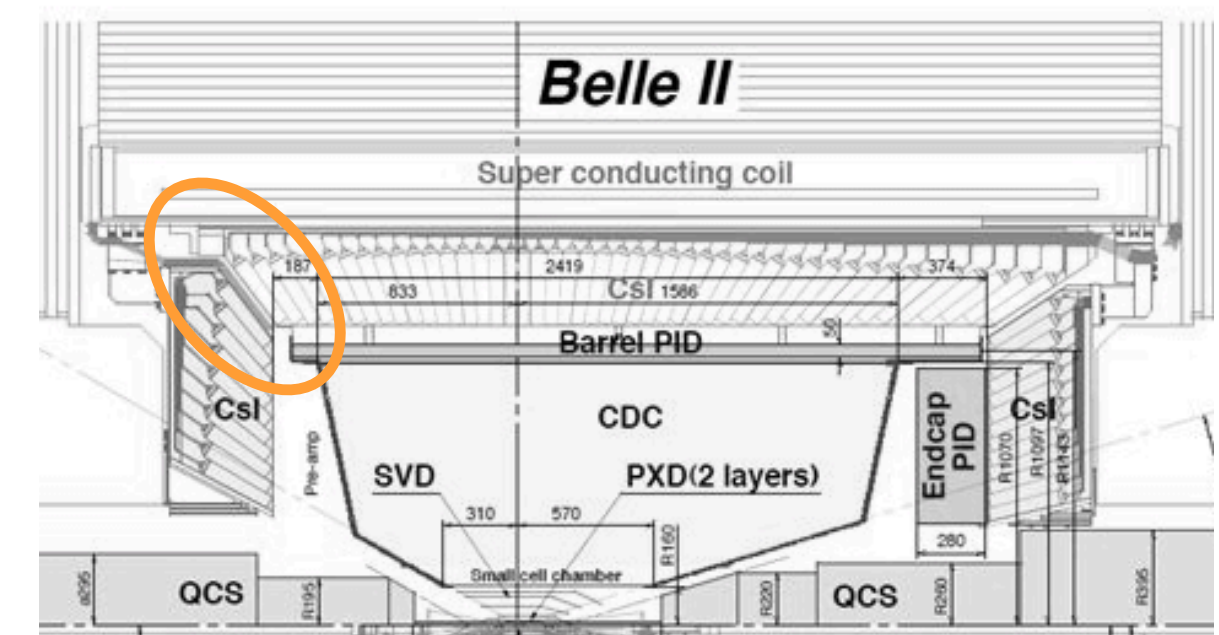
$ee \rightarrow 2\gamma$ and 3γ
 1 γ in ECL 90° gap
 1 γ out of ECL acceptance

$$E_\gamma = \frac{s - M_{A'}^2}{2\sqrt{s}}$$

$ee \rightarrow eey$
 both electrons
 out of tracking acceptance

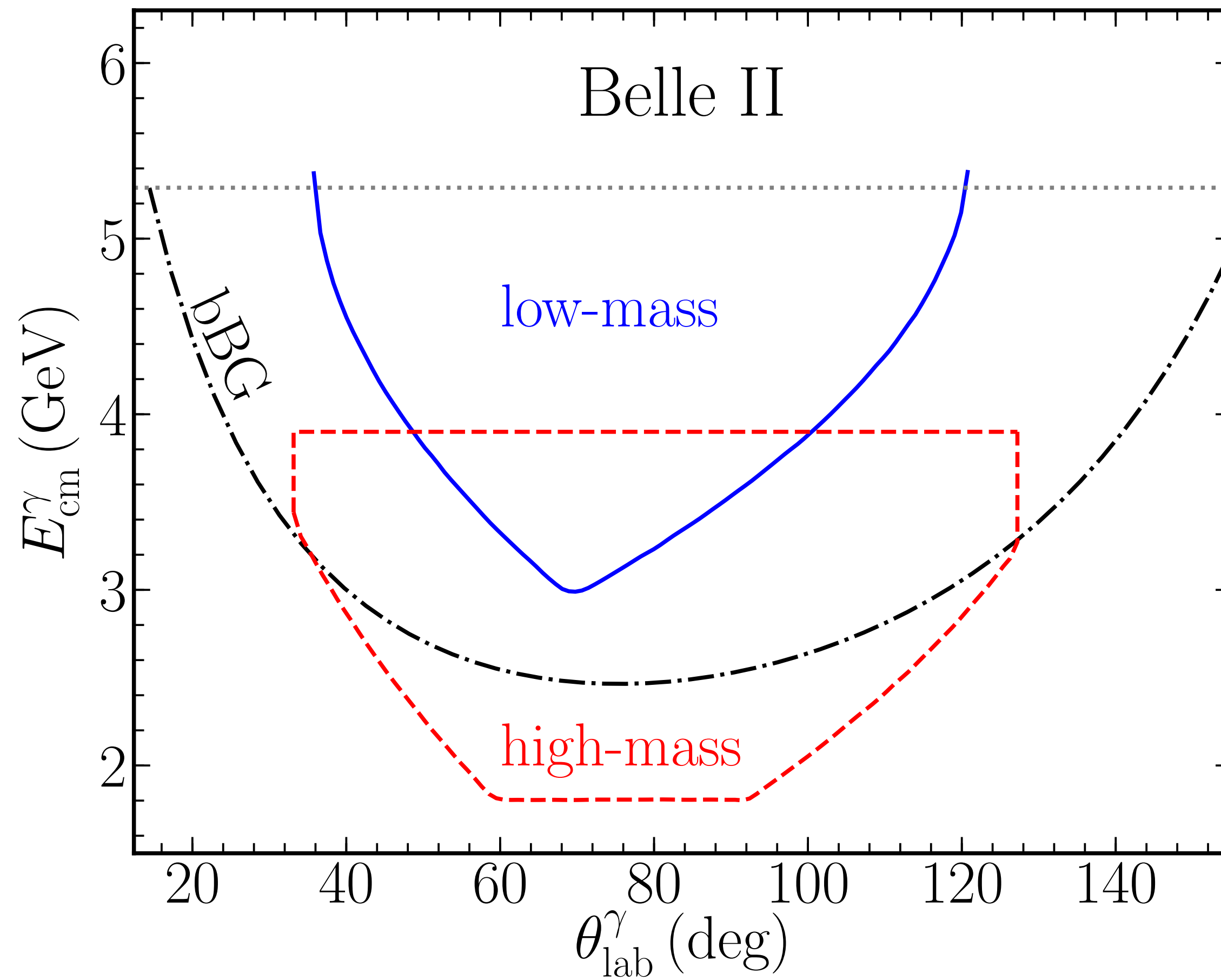


$ee \rightarrow 2\gamma$
 1 γ in ECL BWD or FWD gap



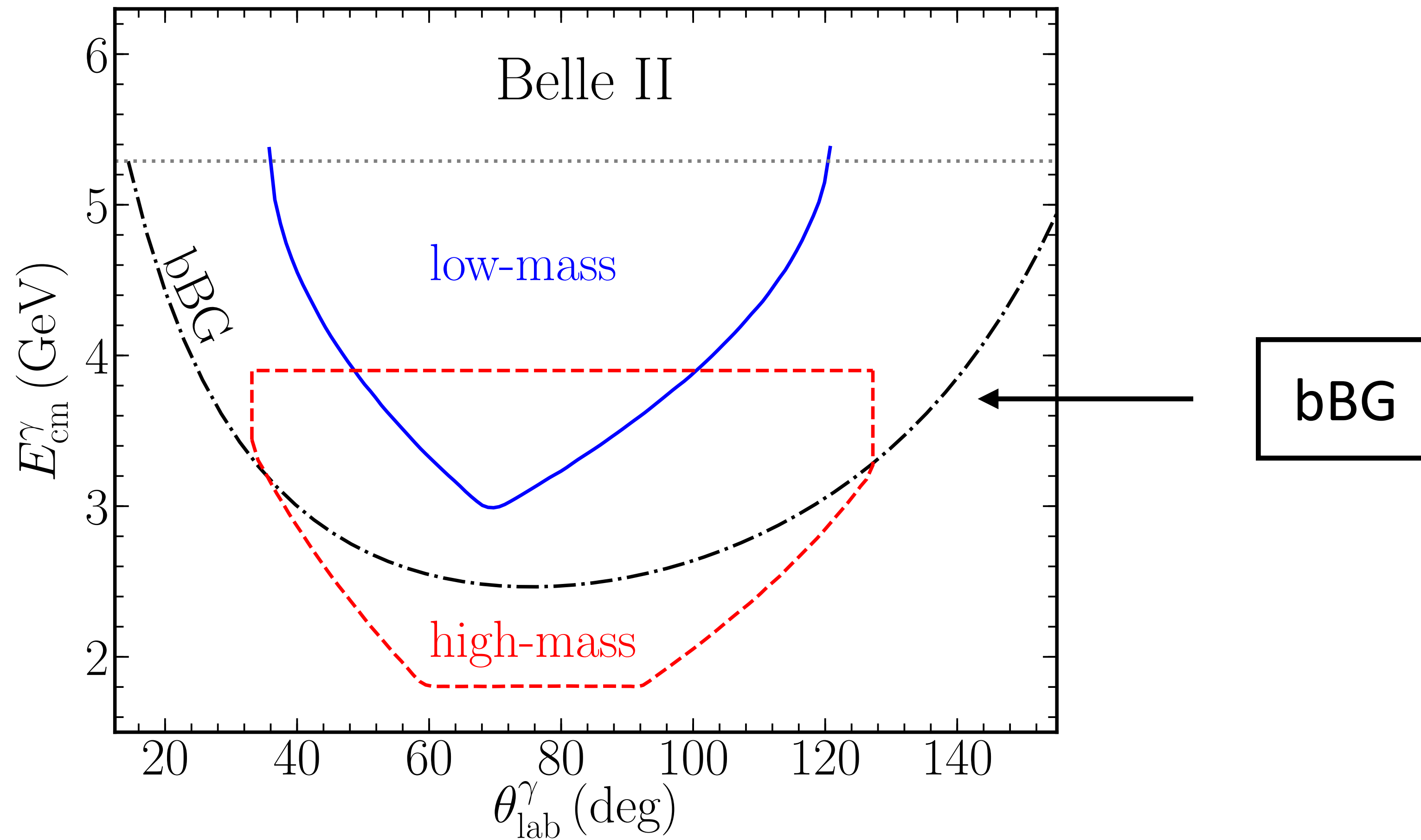
$ee \rightarrow 3\gamma$
 1 γ in ECL BWD gap
 1 γ out of ECL acceptance

Photon energy and angular cuts @ Belle II



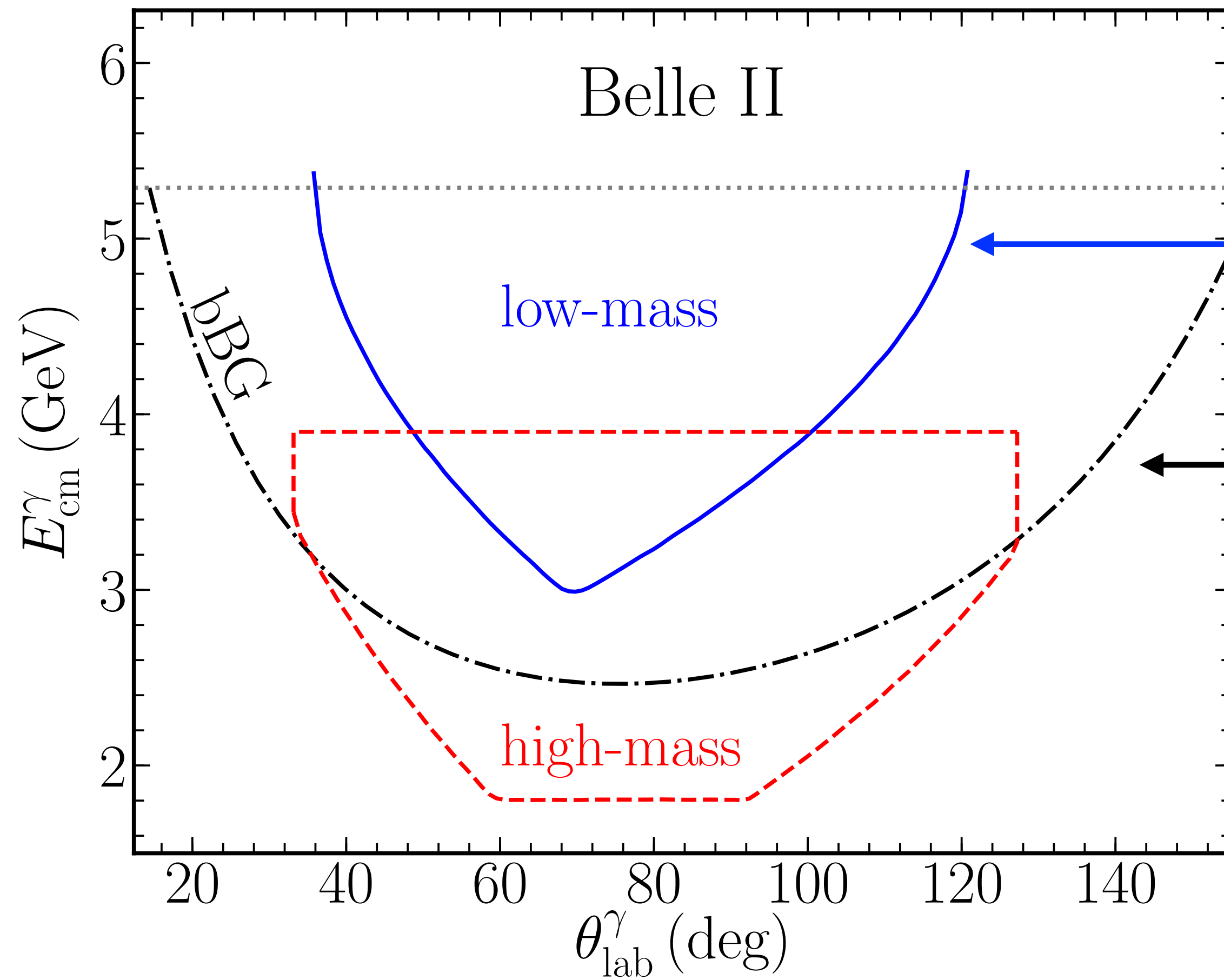
[Liang, Liu, Ma, Zhang, 1909.06847]

Photon energy and angular cuts @ Belle II



[Liang, Liu, Ma, Zhang, 1909.06847]

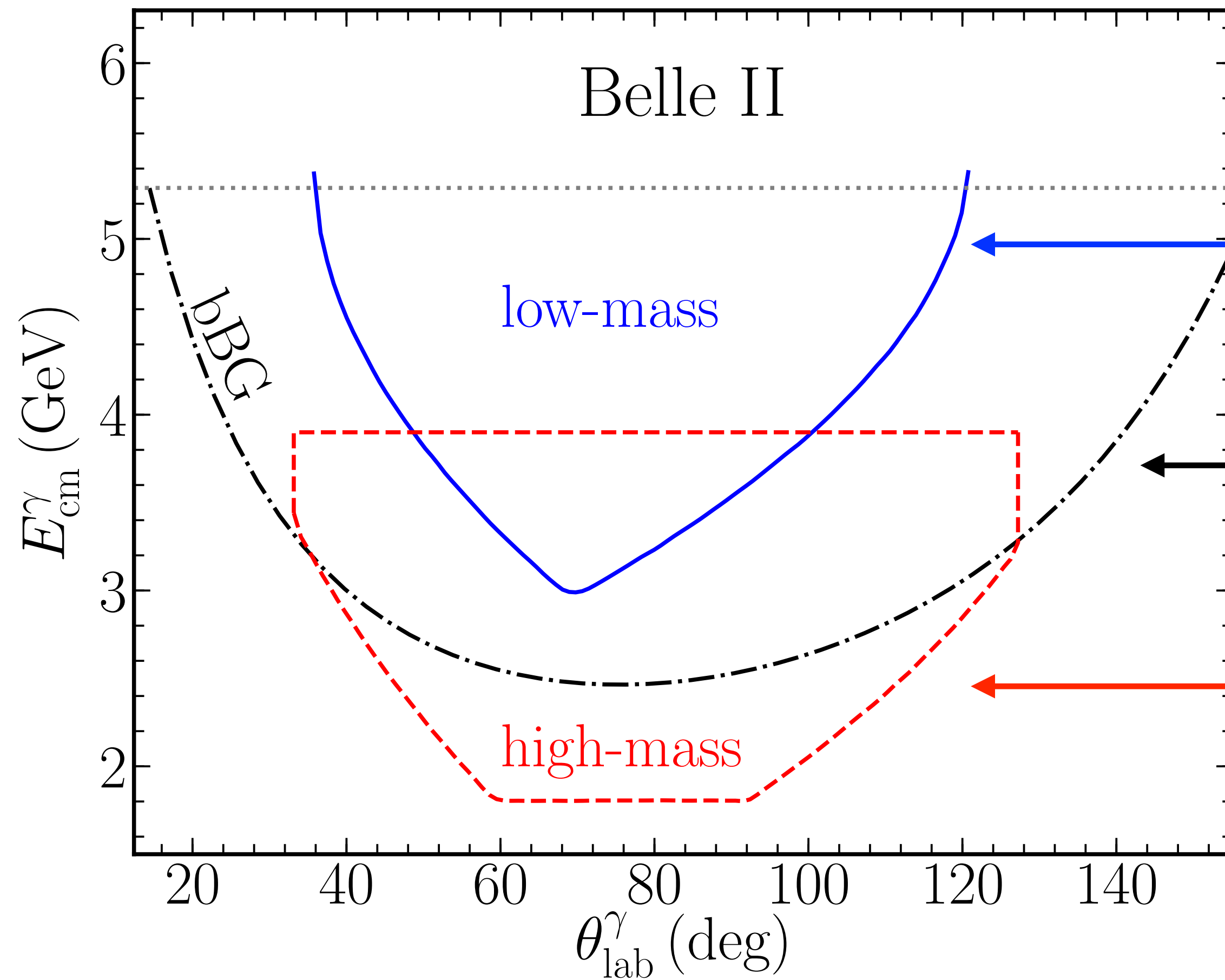
Photon energy and angular cuts @ Belle II



[Belle II 1808.10567]

[Liang, Liu, Ma, Zhang, 1909.06847]

Photon energy and angular cuts @ Belle II



low mass region

[Belle II 1808.10567]

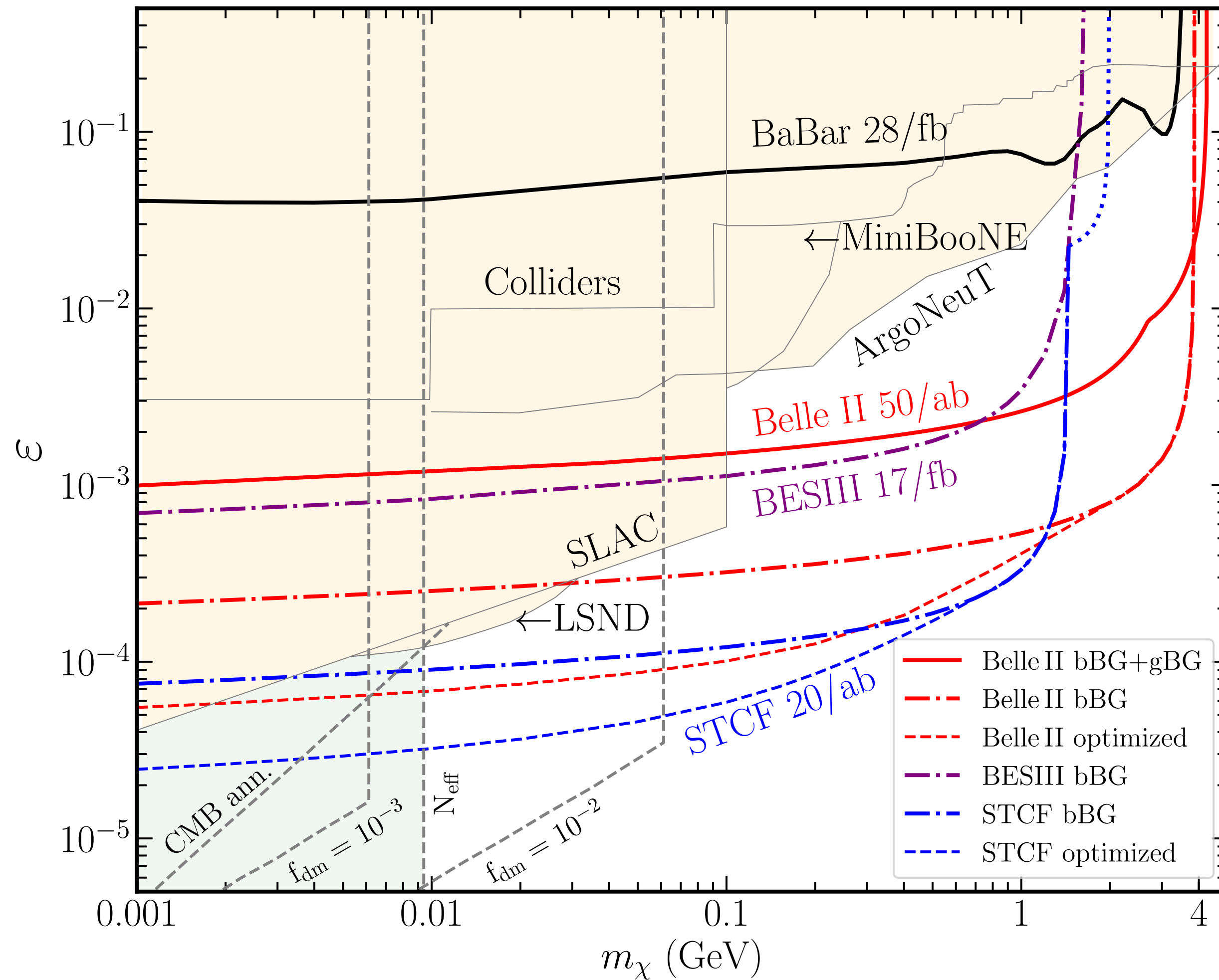
bBG

high mass region

[Belle II 1808.10567]

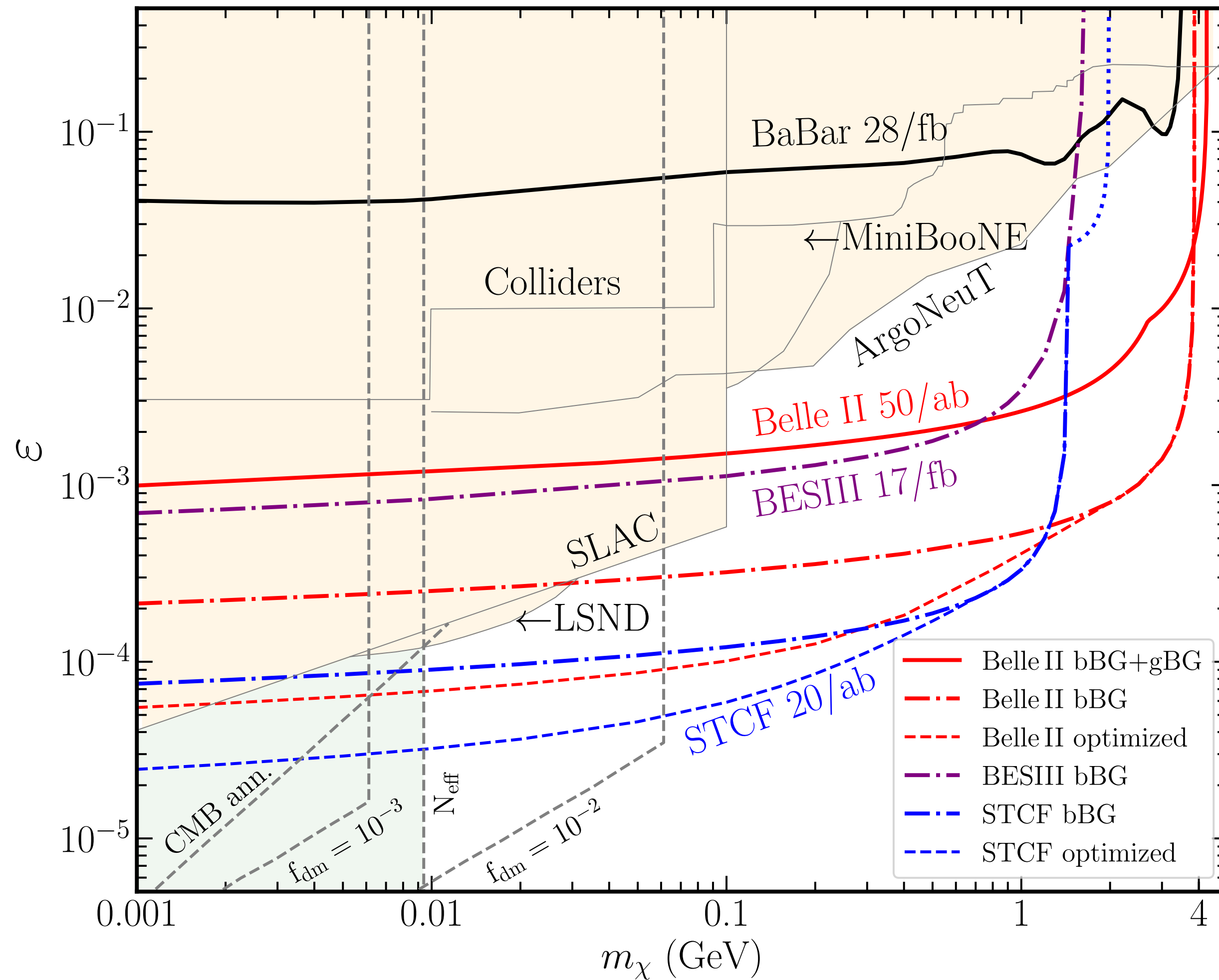
[Liang, Liu, Ma, Zhang, 1909.06847]

electron colliders probe new parameter region (95% CL)



[Liang, Liu, Ma, Zhang, 1909.06847]

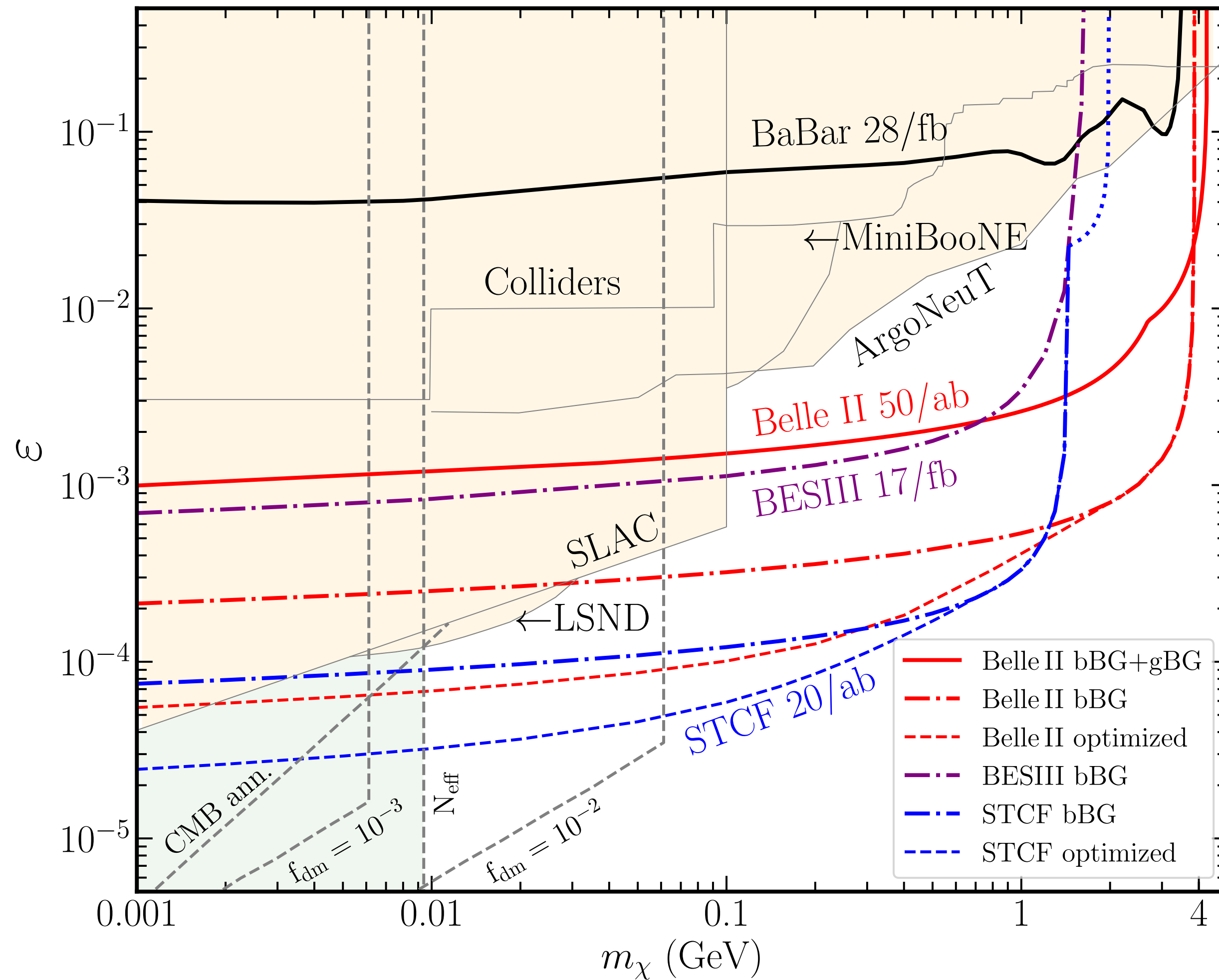
electron colliders probe new parameter region (95% CL)



← BaBar

[Liang, Liu, Ma, Zhang, 1909.06847]

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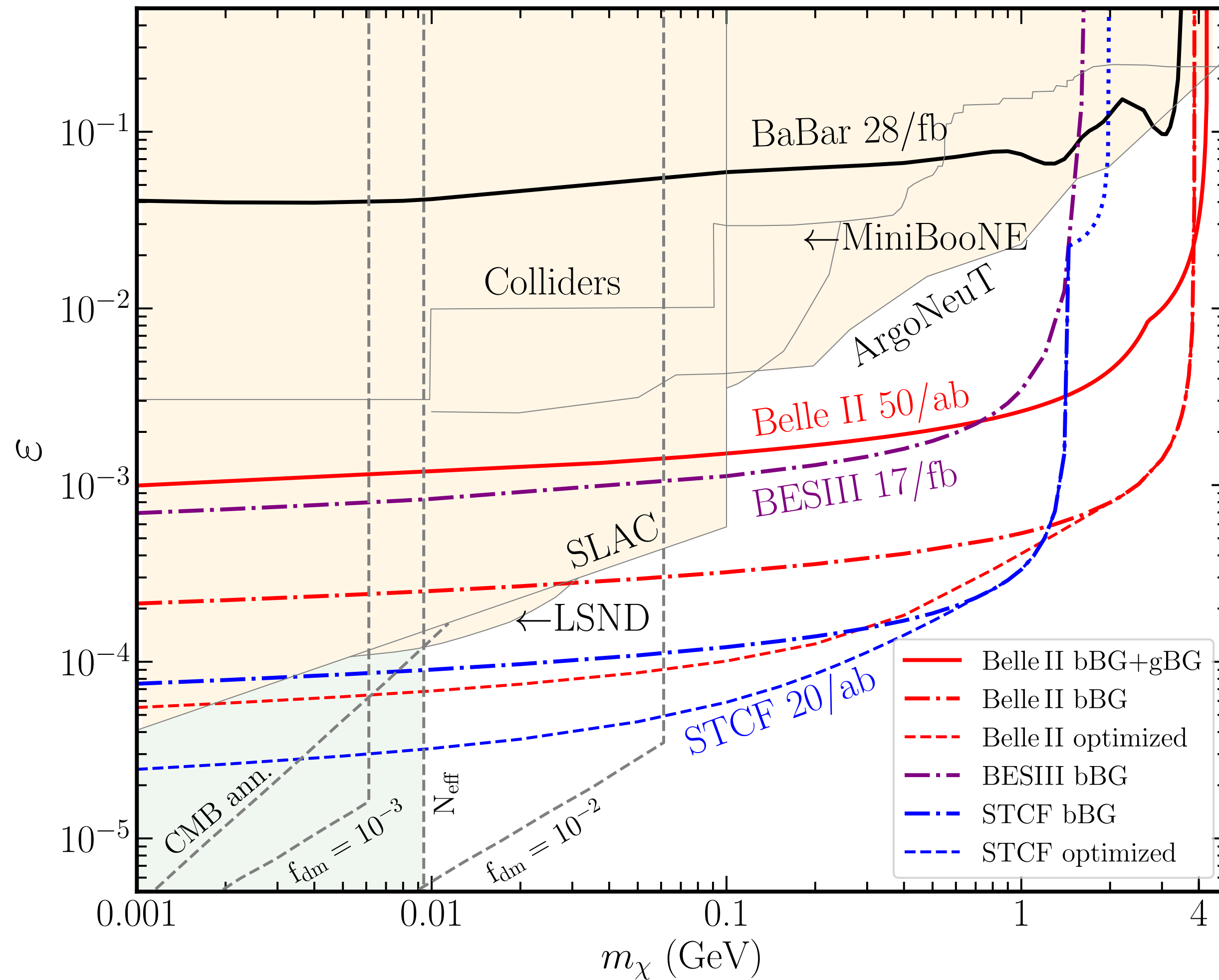


← BaBar

← BESIII

[Liang, Liu, Ma, Zhang, 1909.06847]

electron colliders probe new parameter region (95% CL)



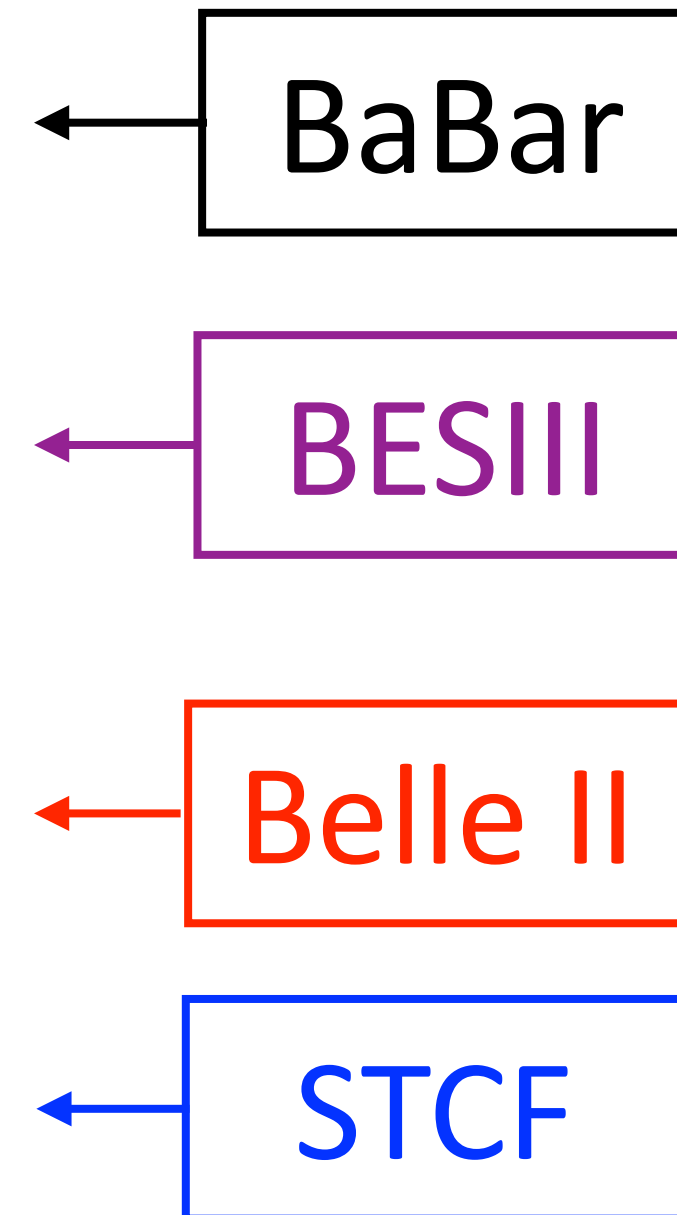
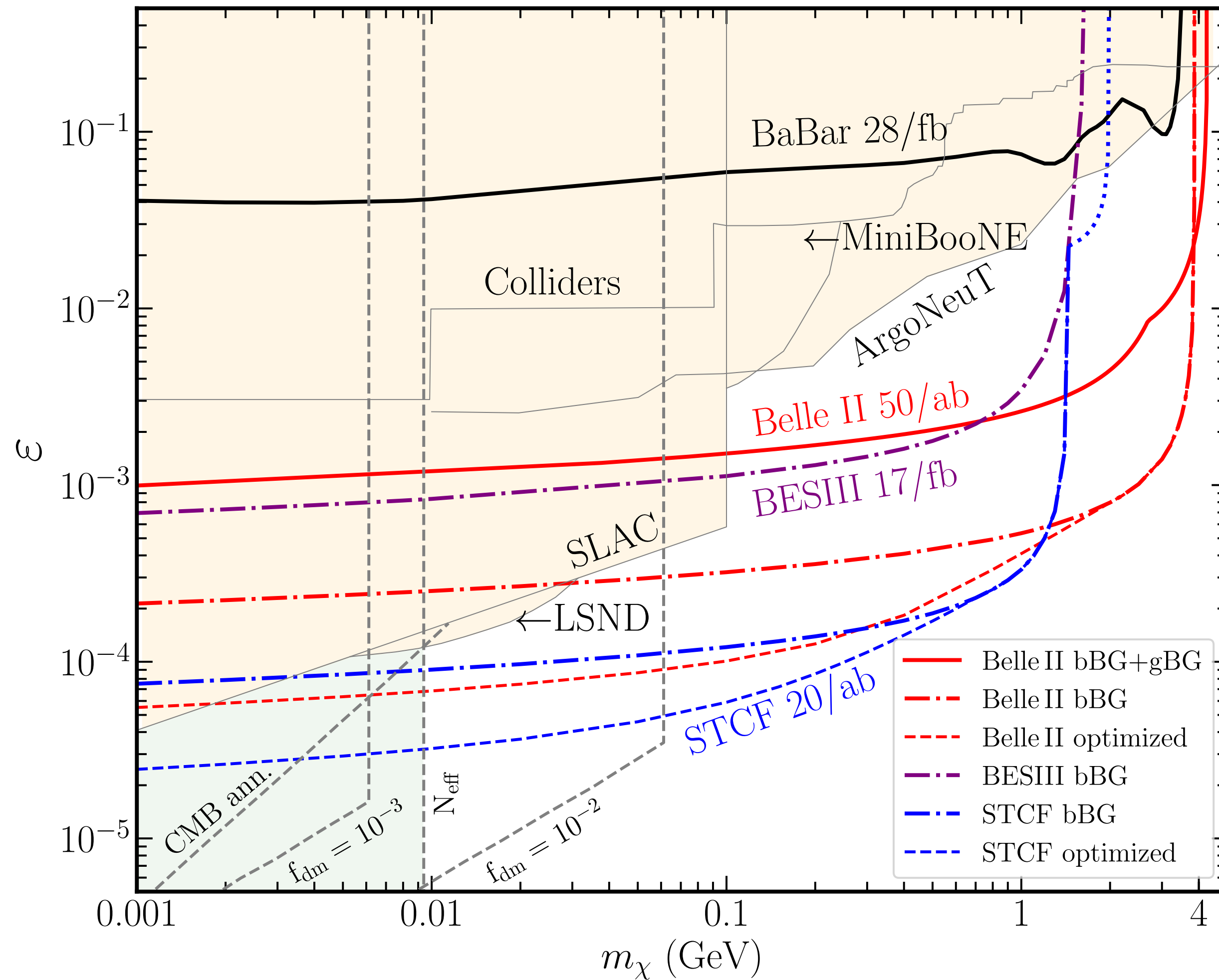
← BaBar

← BESIII

← Belle II

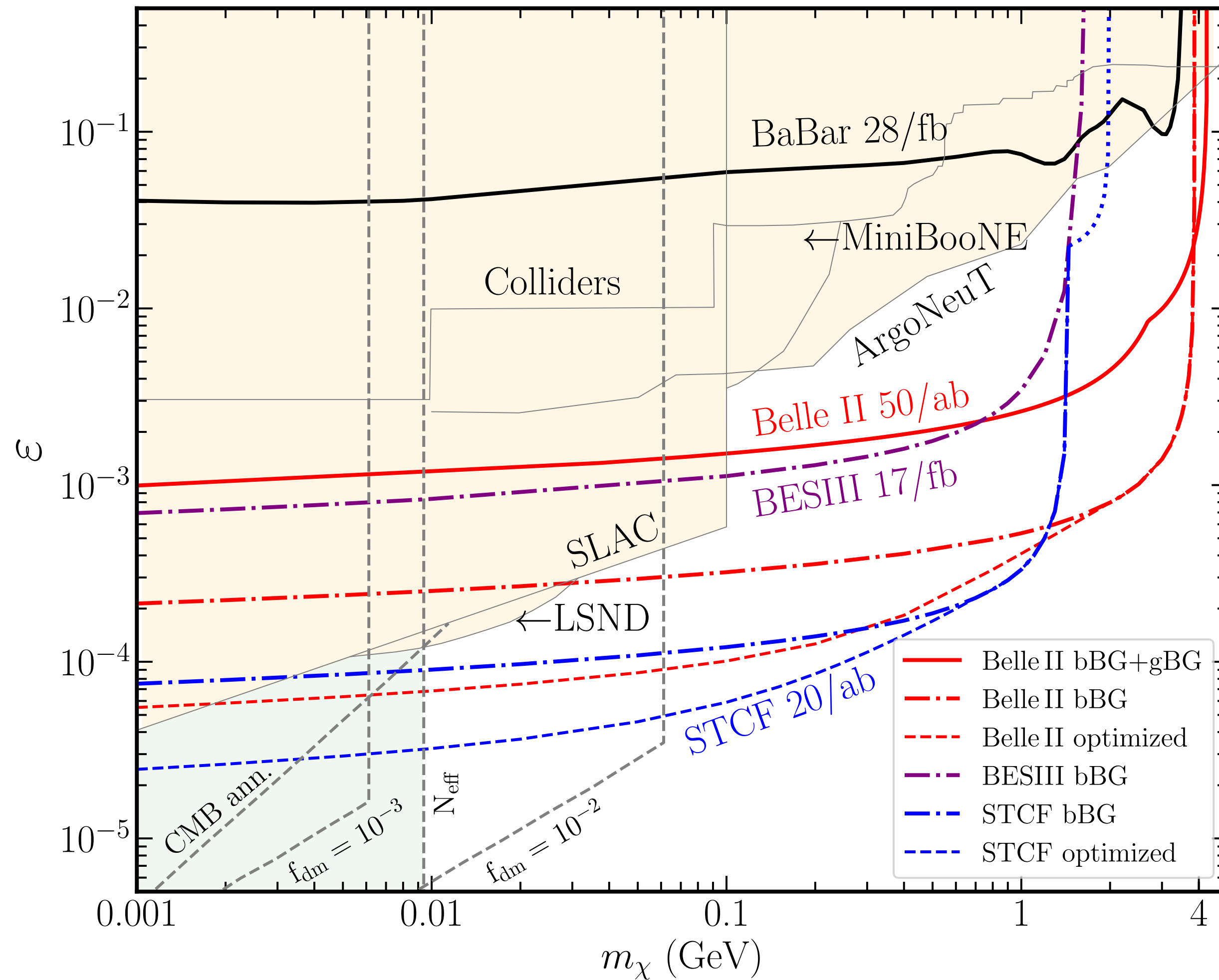
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diff BG considerations

BaBar

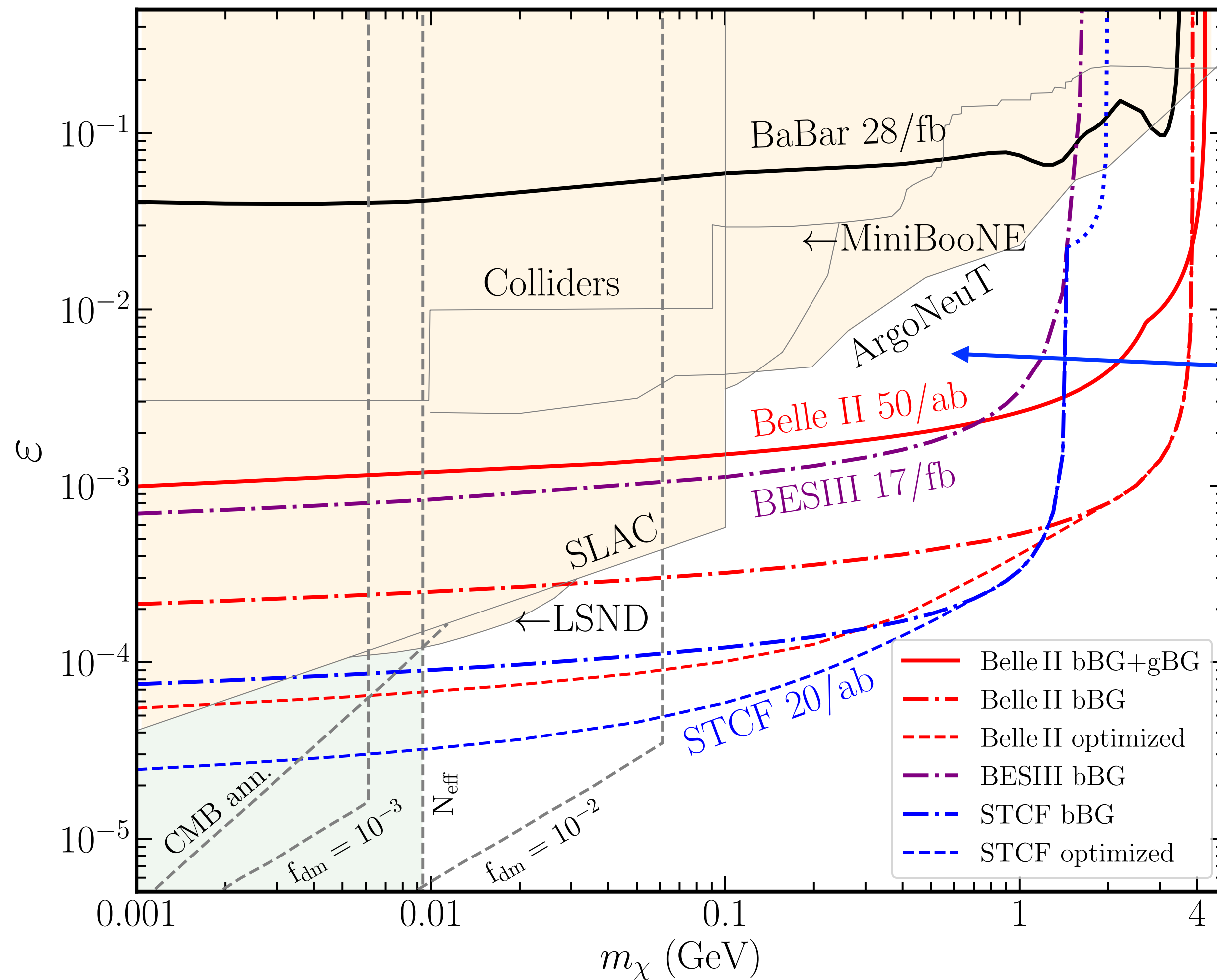
BESIII

Belle II

STCF

[Liang, Liu, Ma, Zhang, 1909.06847]

electron colliders probe new parameter region (95% CL)



diff BG considerations

BaBar

BESIII

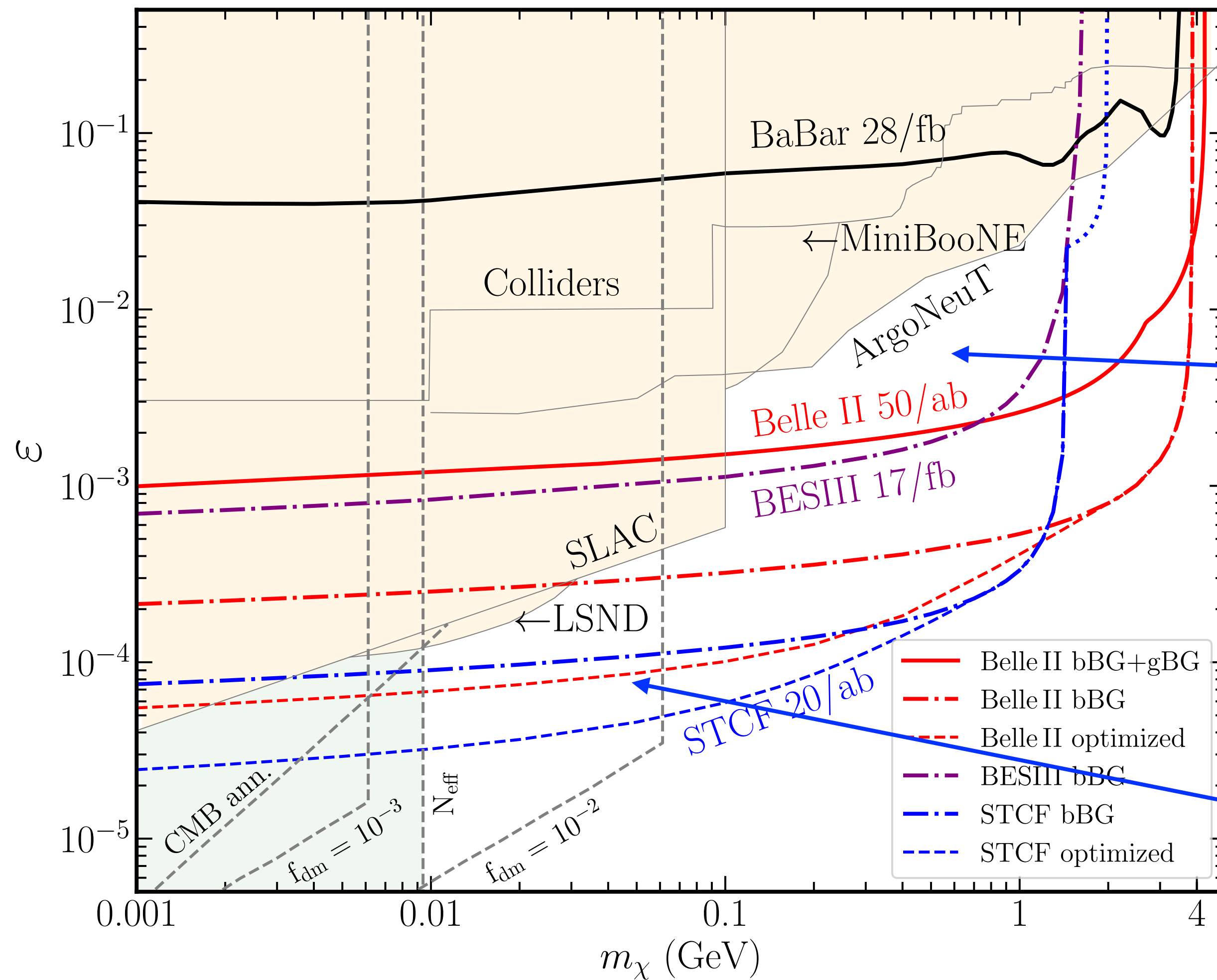
new regions: 0.1-4 GeV

Belle II

STCF

[Liang, Liu, Ma, Zhang, 1909.06847]

electron colliders probe new parameter region (95% CL)



diff BG considerations

BaBar

BESIII

new regions: 0.1-4 GeV

Belle II

STCF

$\epsilon \lesssim O(10^{-4})?$

[Liang, Liu, Ma, Zhang, 1909.06847]

Summary

Millicharged particles can appear in kinetic mixing or Stueckelberg mass mixing models

[Feldman, ZL, Nath, hep-ph/0702123, 299 cites]

A number of terrestrial experiments have been carried out or proposed to search for millicharged particles

We propose to search for millicharged particles at electron colliders, including BESIII, Belle-II and STCF, which can probe currently unexplored parameter regions: $\epsilon \lesssim O(10^{-3})$ for $100 \text{ MeV} \lesssim m \lesssim \text{several GeV}$

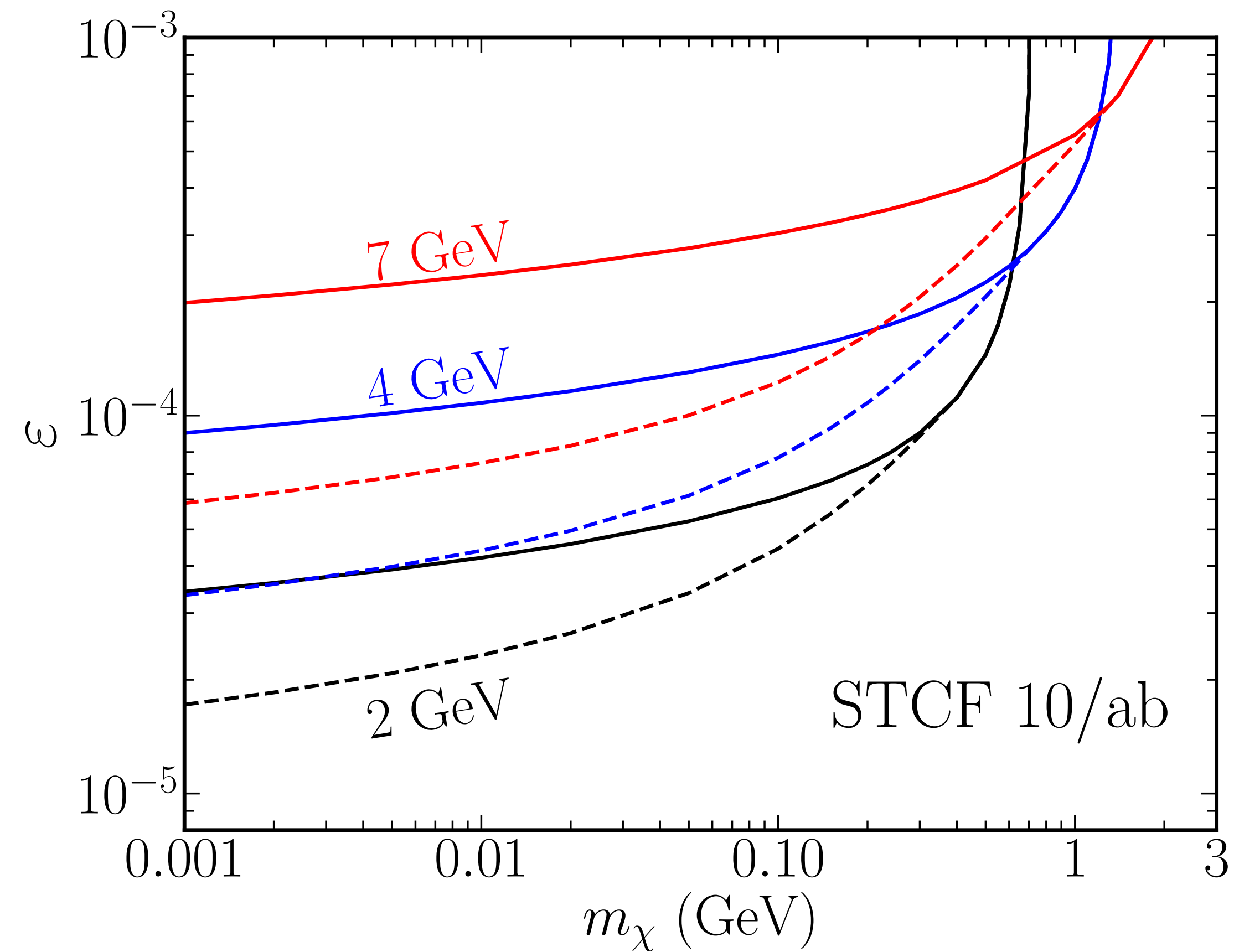
[ZL, Zhang, 1808.00983]

[Liang, ZL, Ma, Zhang, 1909.06847]

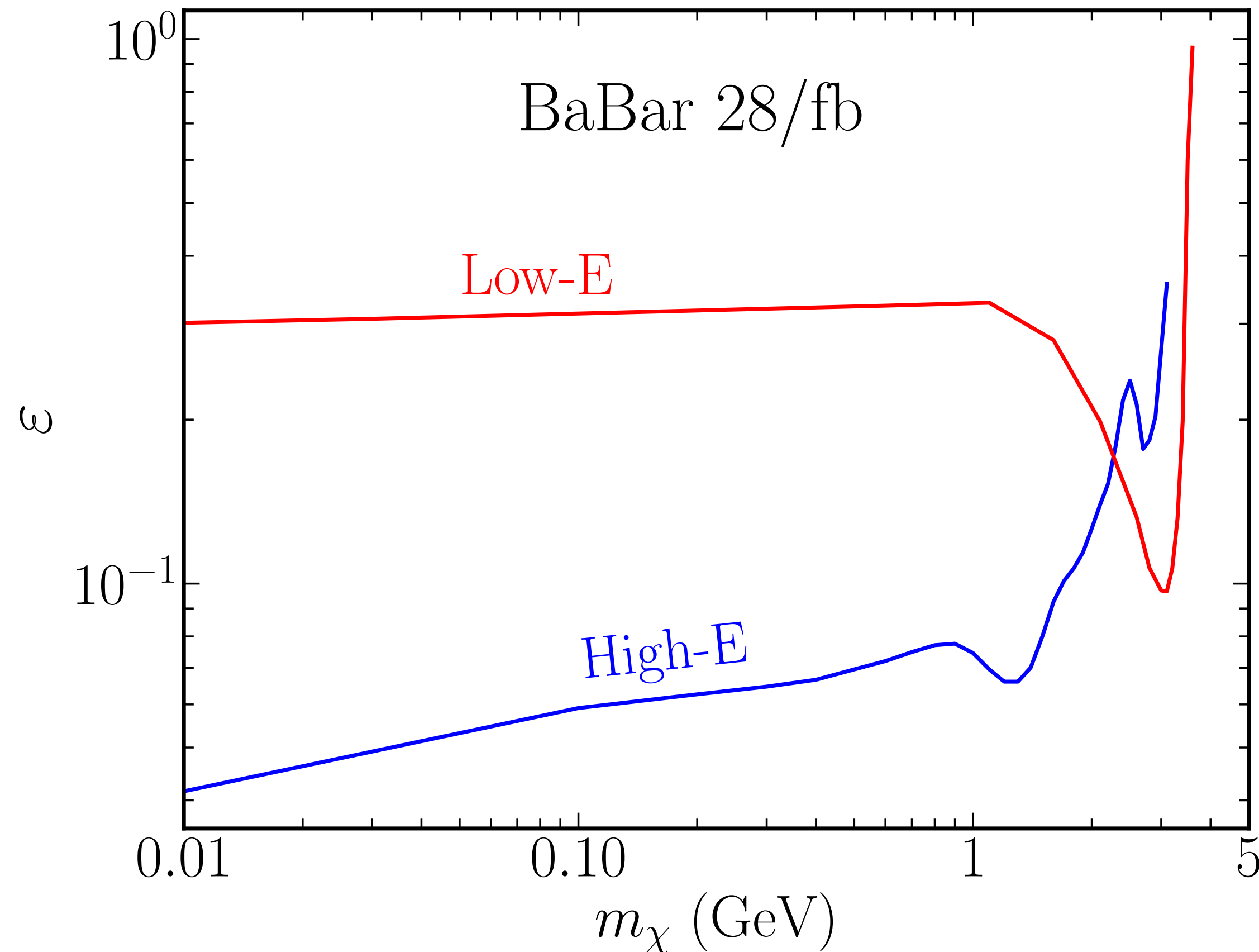
additional slides

Different STCF colliding energies

STCF low-E mode: better for low mass



BaBar sensitivity on millicharge



High-E

$$3.2 < E_\gamma^* < 5.5 \text{ GeV}$$

$$-0.31 < \cos \theta_\gamma^* < 0.6$$

Low-E

$$2.2 < E_\gamma^* < 3.7 \text{ GeV}$$

$$-0.46 < \cos \theta_\gamma^* < 0.46$$

[BaBar, 0808.0017]

high-E data has better sensitivity to light mass

Mass growth via Stueckelberg

Make massive QED gauge invariant by adding axion σ

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{m^2}{2}A_\mu^2$$
$$\Rightarrow -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{2}(mA_\mu + \partial_\mu\sigma)^2$$

invariant under gauge transformation

$$\delta A_\mu = \partial_\mu\lambda, \quad \delta\sigma = -m\lambda$$

σ : longitudinal mode of the vector boson

Stueckelberg in extra dimensions

compactification of a 5D theory on half-circle S^1/Z_2

$$\mathcal{L}_5 = -\frac{1}{4} F_{ab}(z) F^{ab}(z), \quad a, b = 0, 1, 2, 3, 5$$

$$z^a = (x^\mu, y), \quad \mu = 0, 1, 2, 3 \quad A_a = (A_\mu(z), \phi(z))$$

infinite number of massive KK modes in 4D

$$\mathcal{L}_4 = -\frac{1}{4} \sum_n F_{\mu\nu}^{(n)}(x) F^{\mu\nu(n)}(x) - \frac{1}{2} \sum_n M_n^2 \left(A_\mu^{(n)}(x) + \frac{1}{M_n} \partial_\mu \phi^{(n)}(x) \right)^2$$

Stueckelberg mass in 4D due to compactification

Stueckelberg vs Higgs

U(1) boson w/ a Higgs potential

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \left[(\partial_\mu + igA_\mu)\phi \right]^2 - \left[\mu^2\phi^*\phi + \lambda(\phi^*\phi)^2 \right]$$

Decompose the Higgs field in polar coordinates

$$\phi = \left(\frac{v+h}{\sqrt{2}} \right) e^{i\frac{\sigma}{v}} \quad v = \sqrt{\frac{-\mu^2}{\lambda}}$$

Unitary gauge $\phi^U = \frac{v+h}{\sqrt{2}}$ & $A_\mu^U = A_\mu - \frac{1}{gv}\partial_\mu\sigma$

$$\mathcal{L} = -\frac{F_U^2}{4} + \frac{(\partial_\mu h)^2}{2} + \frac{g^2}{2}(h+v)^2 A_\mu^U A^{U\mu} - \frac{\lambda}{4}(h^2 + 2hv)^2 + \frac{\lambda}{4}v^4$$

$$M_A = gv$$

$$M_h = \sqrt{2\lambda}v$$

σ disappears

decouple the Higgs particle

Take the limits $-\mu^2 \rightarrow \infty$, $\lambda \rightarrow \infty$ with $v = \sqrt{-\mu^2/\lambda}$ fixed. In this case, the Higgs field $M_h = \sqrt{2\lambda}v$ becomes infinitely heavy and decouples, whereas the gauge boson mass $M_A = gv$ remains unchanged.

Low energy effective theory

$$\mathcal{L} = -\frac{F_U^2}{4} + \frac{M_A^2}{2} A_\mu^U A^{U\mu}$$
$$A_\mu^U = A_\mu - \frac{1}{M_A} \partial_\mu \sigma$$
$$\mathcal{L} = -\frac{F_{\mu\nu}^2}{4} + \frac{1}{2} (M_A A_\mu - \partial_\mu \sigma)^2$$

The Higgs mechanism leads to the Stueckelberg mechanism.

[Allen, Bowick, Lahiri, Mod. Phys. Lett. A 6, 559, (1991)]

[Nath, arXiv:0812.0958] ⁴⁶ [Nelson, Scholtz, arXiv:1105.2812]