# Standard Model Effective Field Theory at Future Lepton Colliders

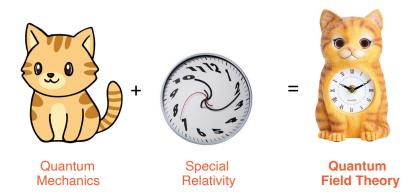
(with Machine Learning)

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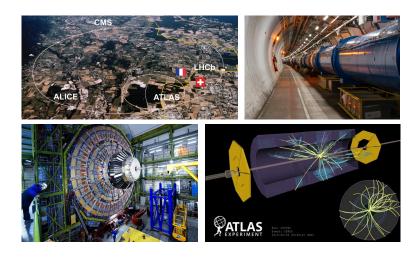
Interdisciplinary Center for Theoretical Study Peng Huanwu Center for Fundamental Theory USTC Jun 15, 2023

## What is particle physics?



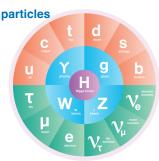
- Quantum Field Theory tells us:
  - Particles can be annihilated and created.
  - ► High energies ⇒ heavy (new) particles.

## particle physics $\approx$ collider physics



 $\blacktriangleright$  Build large colliders  $\rightarrow$  go to high energy  $\rightarrow$  discover new particles!

## The Standard Model



#### interactions



#### the Wheel

Only a few "elementary" particles.

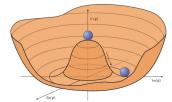
#### the Mug

The Standard Model Lagrangian is simple!

#### the "Mexican Hat"

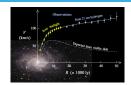
The Higgs Mechanism gives masses to the elementary particles.

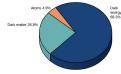
## Higgs mechanism



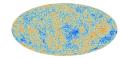
## So many things we don't know...

- What is dark matter?
- What is dark energy?
- Why are there more matter than anti-matter?
- What is the origin of neutrino masses?
- What caused the inflation (if it happened)?
- Why is the electroweak scale so much smaller than the Planck scale?
- ▶ Why is the strong CP phase  $\theta$  so small?
- Why is the CKM matrix somewhat close to 1?
- What is the theory of quantum gravity?
- **.....**









## We need experiments to find the answers!

LHC will find Supersymmetry (or something else), which has a dark matter candidate and solves the Hierarchy problem!

Higgs and nothing else?



6

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- What's next?
  - ▶ Build an even larger collider (~ 100 TeV)?
  - No guaranteed discovery!

## We need experiments to find the answers!

LHC will find Supersymmetry (or something else), which has a dark matter candidate and solves the Hierarchy problem!

Higgs and nothing else?



- What's next?
  - ▶ Build an even larger collider (~ 100 TeV)?
  - No guaranteed discovery!

■ Build large colliders → go to high energy → discover new particles!

 $\label{eq:doprec} \textbf{do precision measurements} \rightarrow \textbf{discover new physics indirectly!}$ 

- Higgs factory! (HL-LHC, or a future lepton collider)
- Standard Model Effective Field Theory (model independent approach)

#### To summarize in one sentence...



"Our future discoveries must be looked for in the sixth place of decimals."

Albert A. Michelson

## Why lepton $(e^+e^-)$ colliders?



- It's a Higgs (and Z, W, top) factory!
  - Large statistics, clean environment
    - ⇒ precision measurements!
    - ▶ On the other hand, the LHC is designed to be a "discovery machine"...
- ► Circular vs. Linear
  - ► Circular: large luminosity, reuse the tunnel for a 100 TeV hadron collider.
  - Linear: high energy (up to a few TeVs), beam polarization.

#### Muon colliders?

## Why lepton $(e^+e^-)$ colliders?

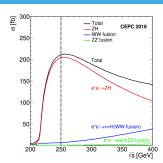
#### ▶ Higgs

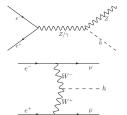
- e<sup>+</sup>e<sup>-</sup> → hZ cross section maximized at around 250 GeV
- $e^+e^- o 
  u \bar{\nu} h$  cross section increases with energy

$$\begin{array}{ll} \bullet & e^+e^- \rightarrow \bar{t}th\,,\\ & e^+e^- \rightarrow Zhh\,, e^+e^- \rightarrow \nu\bar{\nu}hh\,,\\ & \dots \end{array}$$

#### and more

- $e^+e^- \rightarrow Z \rightarrow \bar{f}f$ Z-pole
- $e^+e^- \rightarrow WW$ WW threshold and above
- $e^+e^- \rightarrow t\bar{t}$  $t\bar{t}$  threshold and above





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## The Standard Model Effective Field Theory



- $\triangleright$   $[\mathcal{L}_{sm}] \leq 4$ . Why?
  - Bad things happen when we have non-renormalizable operators!
  - Everything is fine as long as we are happy with finite precision in perturbative calculation.
- ▶ **d=5:**  $\frac{c}{\Lambda}$  *LLHH*  $\sim \frac{cv^2}{\Lambda}\nu\nu$ , Majorana neutrino mass.
- Assuming Baryon and Lepton numbers are conserved,

$$\mathcal{L}_{ ext{SMEFT}} = \mathcal{L}_{ ext{SM}} + \sum_{i} rac{c_{i}^{(6)}}{\Lambda^{2}} \mathcal{O}_{i}^{(6)} + \sum_{j} rac{c_{j}^{(8)}}{\Lambda^{4}} \mathcal{O}_{j}^{(8)} + \cdots.$$

▶ If  $\Lambda \gg v$ , E, then SM + dimension-6 operators are sufficient to parameterize the physics around the electroweak scale.

## The Standard Model Effective Field Theory

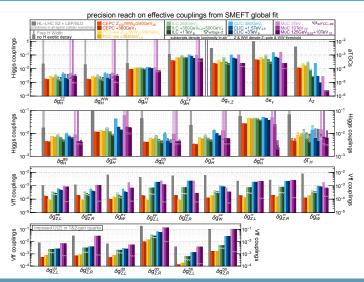


		$X^2$		$\varphi^4$ and $\varphi^4 D^2$		ψ <sup>2</sup> φ <sup>3</sup>		(LL)(LL)		(RR)(RR)		(LL)(RR)
	Qc	$f^{ABC}G^{Ac}G^{Bc}G^{Cc}$	$Q_{\nu}$	$(\varphi^{\dagger}\varphi)^3$	Que	$(\varphi^{\dagger}\varphi)(I_{\rho^{\mu}}\varphi)$	Qu	$(\bar{l}_i \gamma_i I_r)(\bar{l}_i \gamma^\mu l_i)$	$Q_{ee}$	$(\tilde{e}_{\mu}\gamma_{\mu}e_{\nu})(\tilde{e}_{\nu}\gamma^{\mu}e_{\nu})$	$Q_{lc}$	$(\tilde{l}_j\gamma_\mu l_\nu)(\tilde{e}_i\gamma^\mu e_i)$
	Q <sub>0</sub>	fasc Gar Gar Ger	Quo	$(\varphi^{\dagger}\varphi)\Box(\varphi^{\dagger}\varphi)$	Que	(u'u)(q,u,0)	$Q_{qq}^{(1)}$	$(q_{i}\gamma_{i}q_{i})(q_{i}\gamma^{\mu}q_{i})$	Que	$(\theta_g \gamma_\mu v_\nu)(\theta_e \gamma^\mu v_e)$	$Q_{\mathrm{he}}$	$(\tilde{l}_{p}\gamma_{p}\tilde{l}_{r})(\hat{u}_{a}\gamma^{\mu}u_{t})$
	Qu	gDKWI-WJeWKe	Qua	$(\varphi^{\dagger}D^{\mu}\varphi)^{*}(\varphi^{\dagger}D_{\mu}\varphi)$	Qu	$(\varphi^{\dagger}\varphi)(q_{\rho}d_{\nu}\varphi)$	$Q_{ii}^{(0)}$	$(q_\mu\gamma_\mu\tau^Iq_\nu)(q_\nu\gamma^\mu\tau^Iq_\nu)$	$Q_M$	$(\bar{d}_y \gamma_\mu d_r)(\bar{d}_z \gamma^\mu d_l)$	$Q_{kl}$	$(\tilde{l}_{\mu}\gamma_{\nu}l_{\nu})(\tilde{d}_{\nu}\gamma^{\mu}d_{\ell})$
	$Q_{\overline{W}}$	$e^{IJK}\widetilde{W}^{I_1}W^{J_2}W^{K_2}$					$Q_{i_0}^{(1)}$	$(l_p \gamma_p I_r)(\bar{a}_1 \gamma^\mu a_1)$	$Q_{cs}$	$(\tilde{\epsilon}_{\mu}\gamma_{\mu}\epsilon_{\nu})(\tilde{a}_{\mu}\gamma^{\mu}u_{\ell})$	$Q_{\rm pc}$	$(\bar{q}_j\gamma_{j\ell}q_r)(\bar{e}_j\gamma^\mu e_l)$
	X <sup>2</sup> o <sup>2</sup>		⊕2X <i>ϕ</i>		62G2D		$Q_{iq}^{(3)}$	$(\bar{l}_{p}\gamma_{p}\tau^{I}l_{r})(\bar{q}_{r}\gamma^{\mu}\tau^{I}q_{r})$	$Q_{cd}$	$(\bar{e}_y \gamma_y e_r)(\bar{d}_z \gamma^a d_t)$	$Q_{qu}^{(1)}$	$(q_i\gamma_iq_r)(s_i\gamma^\mu u_t)$
	9,0	Ø 0 € € € € € € € € € € € € € € € € € €	Qav	$(I_{\nu}\sigma^{\mu\nu}e_{\nu})\tau^{J}\psi W_{\nu\nu}^{I}$	$Q_{a}^{(0)}$	(011 D. 01 (L. +1)			$Q_{ud}^{(1)}$	$(\bar{u}_{\mu}\gamma_{\mu}u_{\nu})(\bar{d}_{z}\gamma^{\mu}d_{z})$	$Q_{\eta n}^{(k)}$	$(q_s\gamma_sT^Aq_r)(\pi_s\gamma^sT^A\pi_t)$
	Q,0	\$  \tilde \	Qua	$(l_0\sigma^{\mu\nu}c_r)\varphi B_{\mu\nu}$	Q(2)	$(\varphi^{I}i\vec{D}_{i}^{I}\varphi)(\vec{l}_{i}\tau^{I}\gamma^{\mu}l_{\nu})$			$Q_{ud}^{(0)}$	$(\bar{u}_s\gamma_sT^Au_r)(\bar{d}_s\gamma^\mu T^Ad_t)$	$Q_{q\ell}^{(1)}$	(40,00)(d,1*d)
	Q <sub>qW</sub>	$\varphi^i \varphi^i W^i_{\mu} W^{i\mu\nu}$	Que	$(q_0 \cdots q_r) \varphi B_{pr}$ $(q_0 \cdots q_r) \varphi G_{rr}^A$	0	$(\phi^{ij} \overrightarrow{D}_{\mu} \phi)(q_{i} \gamma^{\mu} q_{i})$ $(\phi^{ij} \overrightarrow{D}_{\mu} \phi)(q_{i} \gamma^{\mu} q_{i})$					$Q_{s\ell}^{(n)}$	$(\bar{q}_i\gamma_iT^Aq_i)(\bar{d}_i\gamma^\mu T^Ad_i)$
+		SOW WIN	Que	(\$100 m) 1 3 W.	Q(1) Q(1)	$(\varphi^{\eta}D_{\mu}\varphi)(e_{\mu}\gamma^{\mu}e_{\nu})$ $(\varphi^{\eta}D_{\mu}\varphi)(\bar{q}_{\nu}\gamma^{\mu}q_{\nu})$		(RL) and $(LR)(LR)$		B-vio		
	$Q_{\sqrt{W}}$						Qiete	$(\tilde{t}_{i}^{j}c_{r})(\tilde{d}_{r}q_{i}^{j})$	$Q_{dec}$	$\varepsilon^{a_jb_j}\varepsilon_{jk}\left[(d_g^a)\right]$		
	$Q_{\rho S}$	$\varphi^{\dagger}\varphi B_{\mu\nu}B^{\mu\nu}$	$Q_{uS}$	$(q_p \sigma^{\mu\nu} u_r) \overline{\varphi} B_{\mu\nu}$	$Q_{qq}^{(3)}$	$(\varphi^I i \overset{\circ}{D}_{\mu}^I \varphi)(q_{\nu} \tau^I \gamma^{\mu} q_{\nu})$	$Q_{\rm quot}^{(1)}$	$(\bar{q}_{\mu}^{i}u_{\nu})e_{jk}(\bar{q}_{\mu}^{k}d_{\ell})$	$Q_{qq}$	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_{p}^{\alpha j})\right]$		
	$Q_{\mu \bar{\nu}}$	$\varphi^{\dagger}\varphi\bar{B}_{\mu\nu}B^{\mu\nu}$	Qac	$(\tilde{q}_{\mu}\sigma^{\mu\nu}T^Ad_{\sigma})\varphiG^A_{\mu\nu}$	$Q_{\varphi a}$	$(\varphi^{\dagger}i \tilde{D}_{\mu} \varphi)(\bar{u}_{\rho} \gamma^{\mu} u_{\tau})$	$Q_{\rm popt}^{(t)}$	$(q_j^i T^{ij} u_r) v_{jk} (q_s^k T^{ij} d_t)$	$Q_{\rm ess}^{(1)}$	$x^{\alpha\beta\gamma}x_{jk}x_{nm}[(q_p^{\alpha}$		
	$Q_{\varphi WB}$	$\varphi^{\dagger}\tau^{\dagger}\varphiW_{\mu\nu}^{\dagger}B^{\mu\nu}$	Qav	$(q_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\rm vd}$	$(\varphi^{\dagger}i\overrightarrow{D}_{\mu}\varphi)(\overrightarrow{d}_{p}\gamma^{\mu}d_{r})$	$Q_{\rm legs}^{(1)}$	$(l_j^i c_r) c_{jk} (\hat{q}_s^k u_t)$	$Q_{\rm est}^{\rm IS}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{\dagger}\varepsilon)_{jk}(\tau^{\dagger}\varepsilon)_{em}$		
	$Q_{\sqrt{K}B}$	$\varphi^{\dagger}\tau^{I}\varphi\widetilde{W}_{\mu\nu}^{I}B^{\mu\nu}$	$Q_{e0}$	$(\bar{q}_j \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\mu\nu\ell}$	$i(\hat{\varphi}^{\dagger}D_{\mu}\varphi)(\hat{u}_{\mu}\gamma^{\mu}d_{\tau})$	$Q_{loqu}^{(2)}$	$(\bar{\ell}_{\mu}^{i}\sigma_{j\alpha}e_{\nu})e_{jk}(\bar{q}_{\alpha}^{k}\sigma^{\mu\nu}u_{k})$	$Q_{\ell m}$	$\varepsilon^{\alpha\beta\gamma} \left[ (d^{\alpha}_{\mu})^{3} \right]$	$Cu_s^s$	$[(u_i^*)^T C c_i]$

- Write down all possible (non-redundant) dimension-6 operators ...
- 59 operators (76 parameters) for 1 generation, or 2499 parameters for 3 generations. [arXiv:1008.4884] Grzadkowski, Iskrzyński, Misiak, Rosiek, [arXiv:1312.2014] Alonso, Jenkins, Manohar, Trott.
- ▶ A **full global fit** with all measurements to all operator coefficients?
  - ▶ We usually only need to deal with a subset of them, e.g. ~ 20-30 parameters for Higgs and electroweak measurements.
- Do a global fit and present the results with some fancy bar plots!

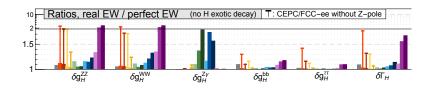
## Higgs + EW, Results from the Snowmass 2021 (2022) study

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonido



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## Impacts of (lack of) the Z-pole run



- Without good Z-pole measurements, the <u>eeZh</u> contact interaction may have a significant impact on the Higgs coupling determination.
- Current (LEP) Z-pole measurements are not good enough for CEPC/FCC-ee Higgs measurements!
  - A future Z-pole run is important!



► Linear colliders suffer less from the lack of a Z-pole run. (Win Win!)

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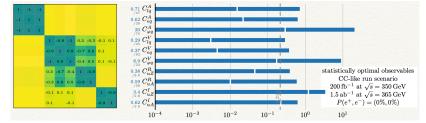
#### Probing Top operators with $e^-e^+ \rightarrow t\bar{t}$

[arXiv:1807.02121] Durieux, Perelló, Vos, Zhang

$$\begin{array}{lll} O_{\varphi q}^{1} \equiv \frac{y_{t}^{2}}{2} & \bar{q}\gamma^{\mu}q & \varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi, & O_{uG} \equiv y_{t}g_{s} & \bar{q}T^{A}\sigma^{\mu\nu}u & \epsilon\varphi^{*}G_{\mu\nu}^{A}, \\ O_{\varphi q}^{3} \equiv \frac{y_{t}^{2}}{2} & \bar{q}\tau^{I}\gamma^{\mu}q & \varphi^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}\varphi, & O_{uW} \equiv y_{t}g_{W} & \bar{q}\tau^{I}\sigma^{\mu\nu}u & \epsilon\varphi^{*}W_{\mu\nu}^{I}, \\ O_{\varphi u} \equiv \frac{y_{t}^{2}}{2} & \bar{u}\gamma^{\mu}u & \varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi, & O_{dW} \equiv y_{t}g_{W} & \bar{q}\tau^{I}\sigma^{\mu\nu}d & \epsilon\varphi^{*}W_{\mu\nu}^{I}, \\ O_{\varphi ud} \equiv \frac{y_{t}^{2}}{2} & \bar{u}\gamma^{\mu}d & \varphi^{T}\epsilon iD_{\mu}\varphi, & O_{uB} \equiv y_{t}g_{Y} & \bar{q}\sigma^{\mu\nu}u & \epsilon\varphi^{*}B_{\mu\nu}, \end{array}$$

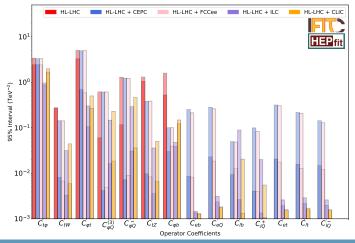
$$\begin{split} O_{lq}^1 &\equiv \frac{1}{2} \ \, \bar{q} \gamma_{\mu} q \quad \bar{l} \gamma^{\mu} l, \\ O_{lq}^3 &\equiv \frac{1}{2} \, \bar{q} \tau^I \gamma_{\mu} q \quad \bar{l} \tau^I \gamma^{\mu} l, \\ O_{lu} &\equiv \frac{1}{2} \ \, \bar{u} \gamma_{\mu} u \quad \bar{l} \gamma^{\mu} l, \\ O_{eq} &\equiv \frac{1}{2} \ \, \bar{q} \gamma_{\mu} q \quad \bar{e} \gamma^{\mu} e, \\ O_{eu} &\equiv \frac{1}{2} \ \, \bar{u} \gamma_{\mu} u \quad \bar{e} \gamma^{\mu} e, \end{split}$$

- Also need to include top dipole interactions and eett contact interactions!
- Hard to resolve the top couplings from 4f interactions with just the 365 GeV run.
  - Can't really separate  $e^+e^- \rightarrow Z/\gamma \rightarrow t\bar{t}$  from  $e^+e^- \rightarrow Z' \rightarrow t\bar{t}$ .
  - Is that a big deal?



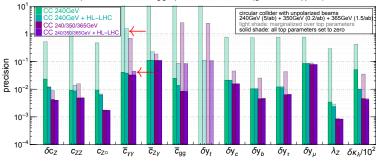
## Results from the recent snowmass study

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou

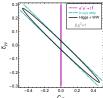


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- $O_{tB}=(\bar{Q}\sigma^{\mu\nu}t)\ \tilde{\varphi}B_{\mu\nu}+h.c.$  is not very well constrained at the LHC, and it generates dipole interactions that contributes to the  $h\gamma\gamma$  vertex.
- ▶ Deviations in  $h\gamma\gamma$  coupling ⇒ run at  $\sim 365 \, \text{GeV}$  to confirm?



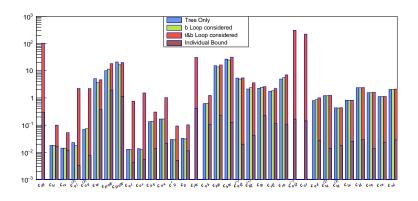
## Top operators in loops (current EW processes)

[2205.05655] Y. Liu, Y. Wang, C. Zhang, L. Zhang, JG

	Experiment	Observables					
Low Energy	CHARM/CDHS/ CCFR/NuTeV/ APV/QWEAK/ PVDIS	Effective Couplings					
		Total decay width $\Gamma_Z$					
		Hadronic cross-section $\sigma_{had}$ Ratio of decay width $R_f$ Forward-Backward Asymmetry $A_{FB}^f$					
Z-pole	LEP/SLC						
		Polarized Asymmetry $A_f$					
	LHC/Tourstron/	Total decay width $\Gamma_W$					
W-pole	LHC/Tevatron/ LEP/SLC	$W$ branching ratios $Br(W \rightarrow lv_l)$					
	LEI / SLC	Mass of W Boson $M_W$					
		Hadronic cross-section $\sigma_{had}$					
ee  o qq	LEP/TRISTAN	Ratio of cross-section $R_f$					
		Forward-Backward Asymmetry for $b/c$ $A_{FB}^{f}$					
	LEP	cross-section $\sigma_f$					
ee  ightarrow ll		Forward-Backward Asymmetry $A_{FB}^{f}$					
		Differential cross-section $\frac{d\sigma_f}{d\cos\theta}$					
$ee \rightarrow WW$	LEP	cross-section $\sigma_{WW}$					
ee → w w	LEF	Differential cross-section $\frac{d\sigma_{WW}}{d\cos\theta}$					

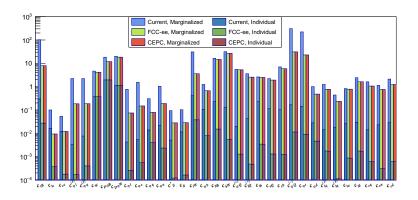
- Top operators (1-loop) + EW operators (tree, including bottom dipole operators)
- $e^+e^- \rightarrow f\bar{f}$  at different energies,  $e^+e^- \rightarrow WW$ .

## Top operators in loops (current EW processes)



Good sensitivities, but too many parameters for a global fit...

## Top operators in loops (future EW processes)



- Good sensitivities, but too many parameters for a global fit...
- ▶ It shows the importance of directly measuring  $e^+e^- \rightarrow t\bar{t}$ .

## Machine learning in SMEFT analyses

Machine learning is not physics!



past

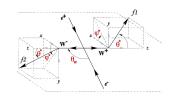


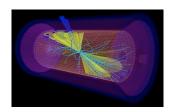
now

- ► Current work with Shengdu Chai (柴声都), Lingfeng Li (李凌风) on  $e^+e^- \to WW$ .
- ▶ Current work with Yifan Fei (费昳帆), Tong Shen (沈同) and Kerun Yu (余柯润) on  $e^+e^- \to t\bar{t}$ .

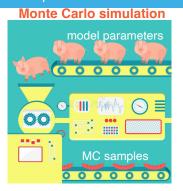
## Why Machine learning?

- In many cases, the new physics contributions are sensitive to the differential distributions.
  - ▶  $e^+e^- \rightarrow WW \rightarrow 4f \Rightarrow 5$  angles
  - $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+\bar{b}W^- \rightarrow 6f$ \$\Rightarrow\$ 9 angles
  - How to extract information from the differential distribution?
  - If we have the full knowledge of  $\frac{d\sigma}{d\Omega}$   $\Rightarrow$  matrix-element method, optimal observables...
- ► The ideal  $\frac{d\sigma}{d\Omega}$  we can calculate is not the  $\frac{d\sigma}{d\Omega}$  that we actually measure!
  - detector acceptance, measurement uncertainties, ISR/beamstrahlung ...
  - In practice we only have MC samples, not analytic expressions, for  $\frac{d\sigma}{d\Omega}$ .





#### The "inverse problem"





- Forward: From model parameters we can calculate the ideal dσ/dΩ, simulate complicated effects and produce MC samples.
- Inverse: From data / MC samples, how do we know the model parameters?
- ▶ With Neural Network we can (in principle) reconstruct  $\frac{d\sigma}{d\Omega}$  (or likelihood ratios) from MC samples.

## A rough sketch

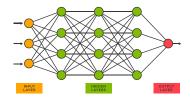
- ▶ We have a theory (SMEFT) that gives a differential cross section  $\frac{d\sigma}{d\Omega}$  which is a function of the parameters of interest c (Wilson coefficients).
  - For simplicity, let's ignore the total rate and focus on  $\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \equiv p(\mathbf{x}|\mathbf{c})$ , *i.e.* it's a probability density function of the observables  $\mathbf{x}$ .
  - ▶ Define the likelihood function  $\mathcal{L}(\mathbf{c}|\mathbf{x}) \equiv p(\mathbf{x}|\mathbf{c})$ . For a sample of N events, maximizing the joint likelihood  $\prod_{i=1}^{N} \mathcal{L}(\mathbf{c}|\mathbf{x}_i)$  (or the log likelihood) gives the best estimator for  $\mathbf{c}$ . (matrix-element method)
- Suppose we have two equal-size samples  $\{\mathbf{x}_{i,\mathbf{c}_0}\} \sim p(\mathbf{x}|\mathbf{c}_0)$  and  $\{\mathbf{x}_{i,\mathbf{c}_1}\} \sim p(\mathbf{x}|\mathbf{c}_1)$ , one could define the cross-entropy loss function(al)

$$L(\hat{s}) = -\sum_{i=1}^{N} \log \hat{s}(\mathbf{x}_{i,e_1}) - \sum_{i=1}^{N} \log (1 - \hat{s}(\mathbf{x}_{i,e_0})),$$

which is minimized by the optimal decision function

$$s(\mathbf{x}|\mathbf{c}_0,\mathbf{c}_1) = \frac{p(\mathbf{x}|\mathbf{c}_1)}{p(\mathbf{x}|\mathbf{c}_0) + p(\mathbf{x}|\mathbf{c}_1)}$$
.

## A rough sketch



From neural network we can construct a function  $\hat{s}(\mathbf{x})$ . By minimizing  $L(\hat{s})$  with respect to  $\hat{s}(\mathbf{x})$  we can obtain an estimator for the likelihood ratio

$$\hat{\mathbf{r}}(\mathbf{x}|\mathbf{c}_0,\mathbf{c}_1) = \frac{1 - \hat{\mathbf{s}}(\mathbf{x}|\mathbf{c}_0,\mathbf{c}_1)}{\hat{\mathbf{s}}(\mathbf{x}|\mathbf{c}_0,\mathbf{c}_1)} = \frac{\hat{\boldsymbol{p}}(\mathbf{x}|\mathbf{c}_0)}{\hat{\boldsymbol{p}}(\mathbf{x}|\mathbf{c}_1)},$$

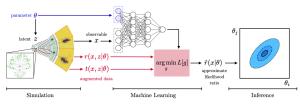
which is the same as the true likelihood ratio in the ideal limit (large sample, perfect training).

- ► There are many other ways to construct a loss function(al)....
- ▶ With additional assumptions on how  $\frac{d\sigma}{d\Omega}$  depends on  $\mathbf{c}$  (*i.e.*, a quadratic relation), we only need to train a finite number of times to know how the likelihood ratio depend on  $\mathbf{c}$ .

#### Particle physics structure

▶ One could make use of latent variable "z" (the parton level analytic result for  $\frac{d\sigma}{d\Omega}$ ) to increase the performance of ML.

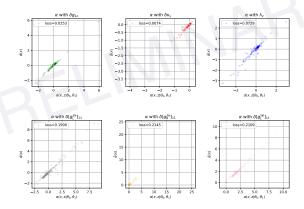
[1805.00013, 1805.00020] Brehmer, Cranmer, Louppe, Pavez



- Assuming linear dependences  $\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} c_i$ , there is a method called SALLY (Score approximates likelihood locally).
  - In this case, for each parameter we only need to train once to obtain  $\alpha_i \equiv \frac{S_{1,i}}{S_0}$ . (It is basically the ML version of Optimal Observables.)
  - We can calculate the "ideal"  $\alpha(z)$  which will help us train the actual  $\alpha(x)$ .

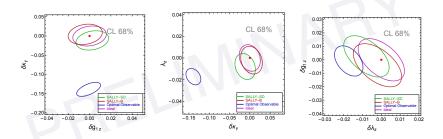
$$L[\hat{\alpha}(\mathbf{x})] = \sum_{\mathbf{x}_i, \mathbf{z}_i \sim \mathrm{SM}} |\alpha(\mathbf{z}_i) - \hat{\alpha}(\mathbf{x}_i)|^2.$$

## Machine Learning in $e^+e^- o WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)



 Semileptonic channel, MadGraph/Pythia/Delphes (CEPC detector card), with ZZ backgrounds.

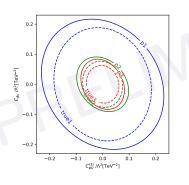
## Machine Learning in $e^+e^- o WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)

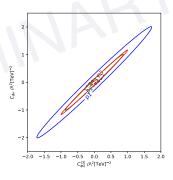


- ▶ 3-aTGC fit, scaled to 10<sup>4</sup> events.
  - OO+classifier: hybrid method that uses a classifier to discriminate background.
- Naively applying truth-level optimal observables could lead to a large bias!
- It's easier for machine learning to take care of systematics!

Jiayin Gu (顾嘉荫) Fudan University

## Machine Learning in $e^+e^- o t ar t$ (very preliminary results, Yifan Fei, JG, Tong Shen, Kerun Yu)





- $ightharpoonup e^+e^ightarrow tar{t}$ , 3 different channels (no background yet)
- ▶ **Left:**  $\sqrt{s} = 1$ TeV, **Right:**  $\sqrt{s} = 360$  GeV

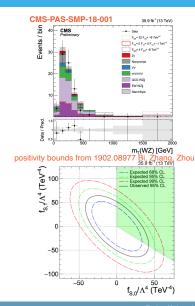
## Machine learning



- When will Machine take over?
  - ▶ Before or after a future lepton collider is built?

## Probing dimension-8 operators?

- ► The dimension-8 contribution has a large energy enhancement  $(\sim E^4/\Lambda^4)!$
- It is difficult for LHC to probe these bounds.
  - Low statistics in the high energy bins.
  - Example: Vector boson scattering.
  - $\Lambda \lesssim \sqrt{s}$ , the EFT expansion breaks down!
- Can we separate the dim-8 and dim-6 effects?
  - ▶ Precision measurements at several different √s?
    - (A very high energy lepton collider?)
  - Or find some special process where dim-8 gives the leading new physics contribution?

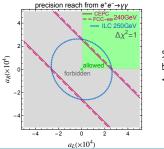


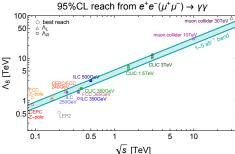
#### The diphoton channel [arXiv:2011.03055] Phys.Rev.Lett. 129, 011805, JG, Lian-Tao Wang, Cen Zhang

- $e^+e^- \rightarrow \gamma\gamma$  (or  $\mu^+\mu^- \rightarrow \gamma\gamma$ ), SM, non-resonant.
- ▶ Leading order contribution: dimension-8 contact interaction.  $(f^+f^- \rightarrow \bar{e}_L e_L \text{ or } e_R \bar{e}_R)$

$$\mathcal{A}(\mathbf{f}^{+}\mathbf{f}^{-}\gamma^{+}\gamma^{-})_{\mathrm{SM+d8}} = 2\mathbf{e}^{2} \frac{\langle 24 \rangle^{2}}{\langle 13 \rangle \langle 23 \rangle} + \frac{\mathbf{a}}{\mathbf{v}^{4}} [13][23] \langle 24 \rangle^{2}.$$

▶ Can probe dim-8 operators (and their positivity bounds) at a Higgs factory ( $\sim 240\,\mathrm{GeV}$ )!





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#### Conclusion

- We have no idea what is the new physics beyond the Standard Model.
- One important direction to move forward is to do precision measurements of the Standard Model processes.
  - A future lepton collider is an ideal machine for that.
  - SMEFT is a good theory framework (but is not everything).
  - Expanding the theory framework?
    - ► Loop contributions, dimension-8 operators, HEFT ...
- Machine learning is (likely to be) the future!

## A lesson from Christopher Columbus (哥伦布发现美洲大陆)

- You need to have a theory.
  - ► The earth is round, India is in the east...
- Your theory can be wrong!
  - Columbus did not find India, but found America instead...
- You need to ask money from the government!
  - Columbus convinced the monarchs of Spain to sponsor him.
- Will we discover the new world?





## backup slides

# $e^+e^- o WW$ with Optimal Observables

- TGCs (and additional EFT parameters) are sensitive to the differential distributions!
  - One could do a fit to the binned distributions of all angles.
  - Not the most efficient way of extracting information.
  - Correlations among angles are sometimes ignored.
  - What are optimal observables?

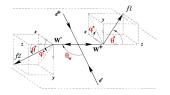
(See e.g. Z.Phys. C62 (1994) 397-412 Diehl & Nachtmann)

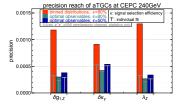
In the limit of large statistics (everything is Gaussian) and small parameters (linear contribution dominates), the best possible reaches can be derived analytically!

$$\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} g_i, \qquad c_{ij}^{-1} = \int d\Omega \frac{S_{1,i} S_{1,j}}{S_0} \cdot \mathcal{L},$$

The optimal observables are given by  $\mathcal{O}_i = \frac{S_{1,i}}{S_0}$ , and are functions of the 5 angles.

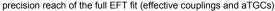


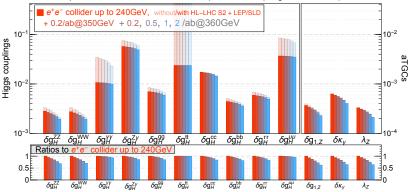




[arXiv:1907.04311] de Blas, Durieux, Grojean, JG, Paul

### Impact of a 350/360 GeV run

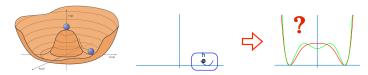




- ► 5.6 ab<sup>-1</sup> at 240 GeV assumed.
- Measurements at 350/360 GeV provides additional handles on the anomalous couplings (e.g.  $hZ^{\mu}Z_{\mu}$  vs.  $hZ^{\mu\nu}Z_{\mu\nu}$ ).
- Also improves the measurements of e<sup>+</sup>e<sup>−</sup> → WW (aTGCs).

# Higgs self-coupling

We know very little about the Higgs potential!

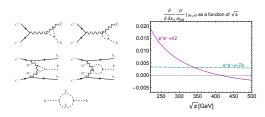


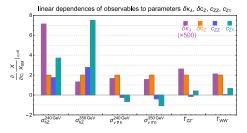
- To know more about the Higgs potential, we need to measure the Higgs self-couplings (hhh and hhhh couplings).
- ▶ The  $(H^{\dagger}H)^3$  operator can modify the Higgs self-couplings.
- Probing the <u>hhh</u> coupling at Hadron colliders.
  - ightharpoonup gg o hh
  - $ightharpoonup \lesssim 50\%$  at HL-LHC.
  - ► ≤ 5% at a 100 TeV collider.



# Triple Higgs coupling at one-loop order

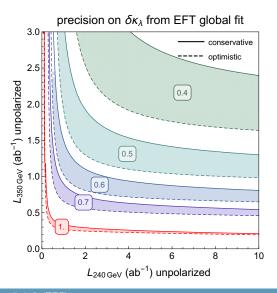
[arXiv:1711.03978] Di Vita, Durieux, Grojean, JG, Liu, Panico, Riembau, Vantalon





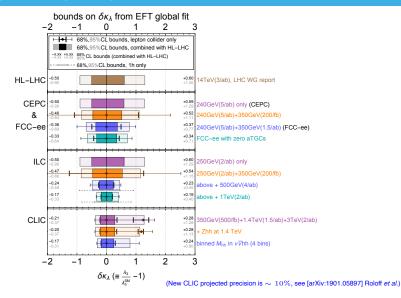
- $\begin{array}{l} \blacktriangleright \ \, \kappa_{\lambda} \equiv \frac{\lambda_{hhh}}{\lambda_{hhh}^{\rm SM}}, \\ \delta \kappa_{\lambda} \equiv \kappa_{\lambda} 1 = \textbf{\textit{C}}_{6} \frac{3}{2}\textbf{\textit{C}}_{\text{H}}, \\ \text{with } \mathcal{L} \supset -\frac{c_{6}\lambda}{2}(\textbf{\textit{H}}^{\dagger}\textbf{\textit{H}})^{3}. \end{array}$
- One loop corrections to all Higgs couplings (production and decay).
- 240 GeV: hZ near threshold (more sensitive to δκλ)
- at 350-365 GeV:
  - WW fusion
  - hZ at a different energy
- h → WW\*/ZZ\* also have some discriminating power (but turned out to be not enough).

# Triple Higgs coupling from EFT global fits



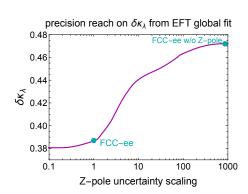
► Runs at two different energies (240 GeV and 350/365 GeV) are needed to obtain good constraints on the triple Higgs coupling in a global fit!

## Triple Higgs coupling from global fits [arXiv:1711.03978]



# Updates on the triple Higgs coupling determination from EFT global fits



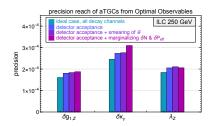


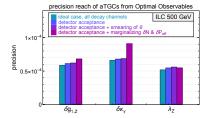
- ▶ 240, 365 GeV are better than 250, 350 GeV.
- Impacts of Z-pole measurements are not negligible. (eeZ(h) contact interaction enters e<sup>+</sup> e<sup>-</sup> → hZ.)



# Updates on the WW analysis with Optimal Observables

- How well can we do it in practice?
  - detector acceptance, measurement uncertainties, ...
- What we have done (current work for the snowmass study)
  - detector acceptance  $(|\cos \theta| < 0.9 \text{ for jets}, < 0.95 \text{ for leptons})$
  - some smearing (production polar angle only,  $\Delta=0.1$ )
  - ▶ ILC: marginalizing over total rate ( $\delta N$ ) and effective beam polarization ( $\delta P_{eff}$ )
- Constructing full EFT likelihood and feed it to the global fit. (For illustration, only showing the 3-aTGC fit results here.)
- Further verifications (by experimentalists) are needed.





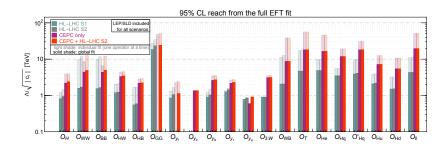
Jiayin Gu (顾嘉荫) Fudan University

# D6 operators

$\mathcal{O}_{H} = \frac{1}{2}(\partial_{\mu} \mathcal{H}^{2} )^{2}$	${\cal O}_{\sf GG}=g_{\sf s}^2 {\sf H} ^2G_{\mu u}^{\!A}G^{\!A,\mu u}$
$\mathcal{O}_{WW} = g^2  H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$\mathcal{O}_{y_u} = y_u  H ^2 \bar{q}_L \tilde{H} u_R + \text{h.c.}  (u \to t, c)$
$\mathcal{O}_{BB} = g'^2  H ^2 B_{\mu u}^{} B^{\mu u}$	$\mathcal{O}_{y_d} = y_d  H ^2 \bar{q}_L H d_R + \text{h.c.}  (d \to b)$
$\mathcal{O}_{HW} = ig(D^{\mu}H)^{\dagger}\sigma^{a}(D^{\nu}H)W^{a}_{\mu\nu}$	$\mathcal{O}_{y_e} = y_e  H ^2 \overline{I}_L He_R + \text{h.c.}  (e \to \tau, \mu)$
$\mathcal{O}_{HB}=\mathit{ig'}(\mathit{D}^{\mu}\mathit{H})^{\dagger}(\mathit{D}^{\nu}\mathit{H})\mathit{B}_{\mu u}$	$\mathcal{O}_{3W}=rac{1}{3!}g\epsilon_{abc}W_{\mu}^{a u}W_{ u ho}^{b}W^{c ho\mu}$
$\mathcal{O}_{W} = \frac{ig}{2} (H^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H) D^{\nu} W_{\mu\nu}^{a}$	$\mathcal{O}_{B} = \frac{i g'}{2} (H^{\dagger} \overleftrightarrow{D_{\mu}} H) \partial^{\nu} B_{\mu \nu}$
$\mathcal{O}_{WB} = gg'H^{\dagger}\sigma^{a}HW^{a}_{\mu u}B^{\mu u}$	$\mathcal{O}_{H\ell} = i H^\dagger \overrightarrow{D_\mu} H \overline{\ell}_L \gamma^\mu \ell_L$
$\mathcal{O}_{\mathcal{T}} = rac{1}{2} (\mathcal{H}^\dagger \overleftrightarrow{\mathcal{D}_\mu} \mathcal{H})^2$	$\mathcal{O}_{H\ell}' = i H^\dagger \sigma^a \overrightarrow{D_\mu} H ar{\ell}_L \sigma^a \gamma^\mu \ell_L$
$\mathcal{O}_{\ell\ell} = (\bar{\ell}_L \gamma^\mu_\mu \ell_L)(\bar{\ell}_L \gamma_\mu \ell_L)$	$\mathcal{O}_{He} = iH^\dagger \overrightarrow{D_\mu} H \overline{e}_R \gamma^\mu e_R$
$\mathcal{O}_{Hq} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overrightarrow{q}_{L} \gamma^{\mu} q_{L}$	$\mathcal{O}_{Hu} = iH^\dagger \overleftrightarrow{D}_{\mu} H \bar{u}_{R} \gamma^\mu u_{R}$
$\mathcal{O}_{Hq}^{\prime} = iH^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H \overline{q}_{L} \sigma^{a} \gamma^{\mu} q_{L}$	$\mathcal{O}_{Hd} = iH^\dagger \overrightarrow{D_\mu} H \overrightarrow{d}_R \gamma^\mu d_R$

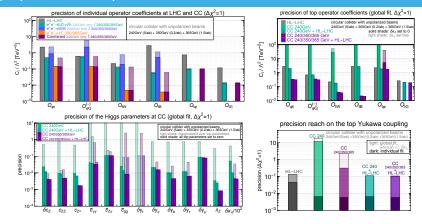
- ▶ SILH' basis (eliminate  $\mathcal{O}_{WW}$ ,  $\mathcal{O}_{WB}$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ )
- ▶ Modified-SILH' basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ )
- ▶ Warsaw basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{HW}$  and  $\mathcal{O}_{HB}$ )

### Reach on the scale of new physics



- Reach on the scale of new physics Λ.
- Note: reach depends on the couplings c<sub>i</sub>!

### Top operators in loops [arXiv:1809.03520] G. Durieux, JG, E. Vryonidou, C. Zhai



- Higgs precision measurements have sensitivity to the top operators in the loops.
  - But it is challenging to discriminate many parameters in a global fit!
- HL-LHC helps, but a 360 or 365 GeV run is better.
- ▶ Indirect bounds on the top Yukawa coupling.

# You can't really separate Higgs from the EW gauge bosons!

$$\begin{array}{l} \blacktriangleright \ \, \mathcal{O}_{H\ell} = i H^\dagger \overleftarrow{D_\mu} H \bar{\ell}_L \gamma^\mu \ell_L, \\ \mathcal{O}_{H\ell}' = i H^\dagger \sigma^a \overleftarrow{D_\mu} H \bar{\ell}_L \sigma^a \gamma^\mu \ell_L, \\ \mathcal{O}_{He} = i H^\dagger \overleftarrow{D_\mu} H \bar{e}_R \gamma^\mu e_R \end{array}$$

(or the ones with quarks)

- modifies gauge couplings of fermions,
- also generates hVff type contact interaction.

$$\mathcal{O}_{HW} = ig(D^{\mu}H)^{\dagger}\sigma^{a}(D^{\nu}H)W_{\mu\nu}^{a},$$

$$\mathcal{O}_{HB} = ig'(D^{\mu}H)^{\dagger}(D^{\nu}H)B_{\mu\nu}$$

- generate aTGCs  $\delta g_{1,Z}$  and  $\delta \kappa_{\gamma}$ ,
- ▶ also generates HVV anomalous couplings such as  $hZ_{\mu}\partial_{\nu}Z^{\mu\nu}$ .



# You also have to measure the Higgs!

- Some operators can only be probed with the Higgs particle.
- ►  $|H|^2 W_{\mu\nu} W^{\mu\nu}$  and  $|H|^2 B_{\mu\nu} B^{\mu\nu}$ 
  - ►  $H \rightarrow v/\sqrt{2}$ , corrections to gauge couplings?
  - Can be absorbed by field redefinition! This applies to any operators in the form |H|<sup>2</sup>O<sub>SM</sub>.

$$egin{aligned} c_{\mathrm{SM}}\mathcal{O}_{\mathrm{SM}} & ext{ vs. } & c_{\mathrm{SM}}\mathcal{O}_{\mathrm{SM}} + rac{c}{\Lambda^2}|\mathcal{H}|^2\mathcal{O}_{\mathrm{SM}} \ & = (c_{\mathrm{SM}} + rac{c\,v^2}{2\,\Lambda^2})\mathcal{O}_{\mathrm{SM}} + ext{terms with } h \ & = c_{\mathrm{SM}}'\mathcal{O}_{\mathrm{SM}} + ext{terms with } h \end{aligned}$$

- probed by measurements of the hγγ and hZγ couplings, or the hWW and hZZ anomalous couplings.
- or Higgs in the loop (different story...)
- ► Yukawa couplings, Higgs self couplings, ...

# Why lepton colliders?

- EFT is good for lepton colliders.
  - A systematic parameterization of Higgs (and other) couplings.
- Lepton colliders are also good for EFT!
  - ► High precision  $\Rightarrow E \ll \Lambda$  Ideal for EFT studies!
  - LHC is built for discovery, but ....

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Standard Model Effective Field Theory at Future Lepton Colliders (with Machine Learning)

- Energy vs. Precision
  - Poor measurements at the high energy tails lead to problems in the interpretation of EFT...



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## A lesson from history

- In 1875, a young Max Planck was told by his advisor Philipp von Jolly not to study physics, since there was nothing left to be discovered.
  - Planck did not listen.

- In 1887, Michelson and Morley tried to find ether, the postulated medium for the propagation of light that was widely believed to exist.
  - They didn't find it.

#### Max Planck:

Before quantum physics:









 "Our future discoveries must be looked for in the sixth place of decimals." — Albert A. Michelson

# Conclusion



Waiting for a future lepton collider to be built...