

Probing Early Universe with PBHs and SIGWs

Yungui Gong

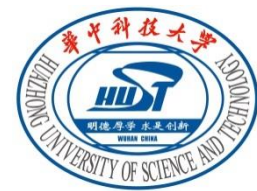
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2021.6.10



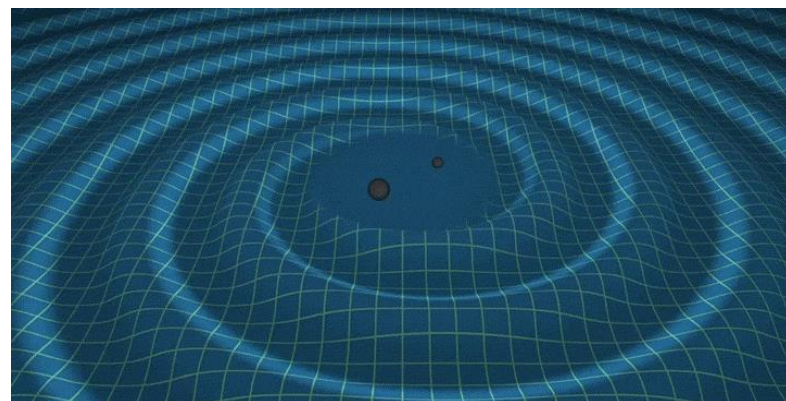
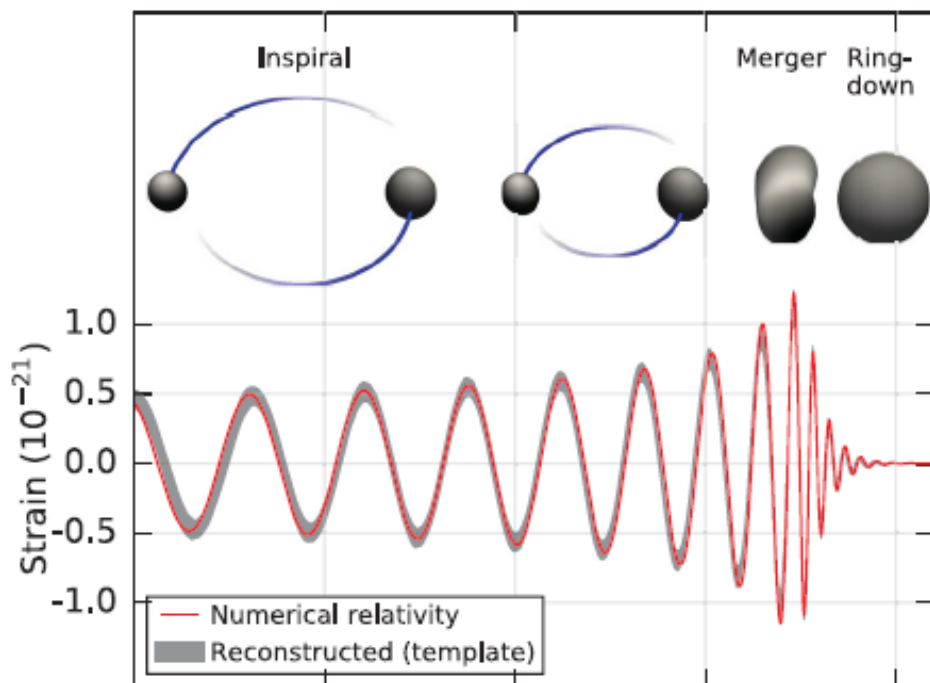
Outline

- Gravitational Waves (GWs) and Gravitational Universe
- Inflation and GWs in early Universe
- Higgs inflation
- The new enhancement mechanism
- Conclusions

Gao, Gong and Li, 1405.6451 (PRD); Di and Gong, 1707.09578 (JCAP); Yi and Gong, 1712.07478 (JCAP); Lu et al., 1907.11896 (JCAP); Lin et al, 2001.05909 (PRD); Lu et al., 2006.03450 (PRD); Yi et al., 2007.09957 (PRD); Arshad et al., 2009.11081 (PRD); Yi et al., 2011.10606 (PRD); Zhang et al., 2012.06960 (JCAP); Gao et al., 2012.03856

Motivation

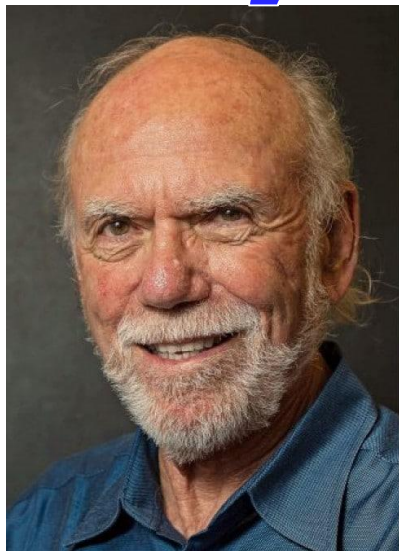
- The discovery of Gravitational Waves (GWs)



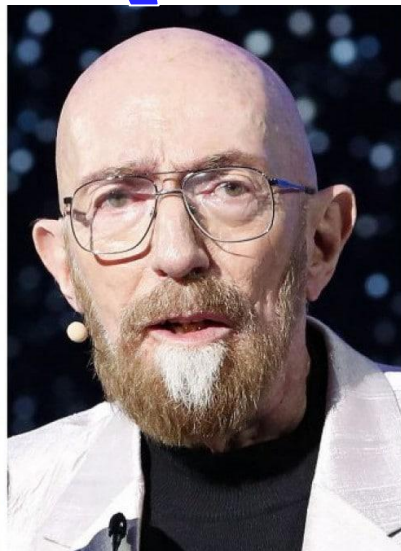
GW150914: PRL 116 (16) 061102

The discovery of GWs

2017 Nobel Prize



Barry C. Barish



Kip S. Thorne

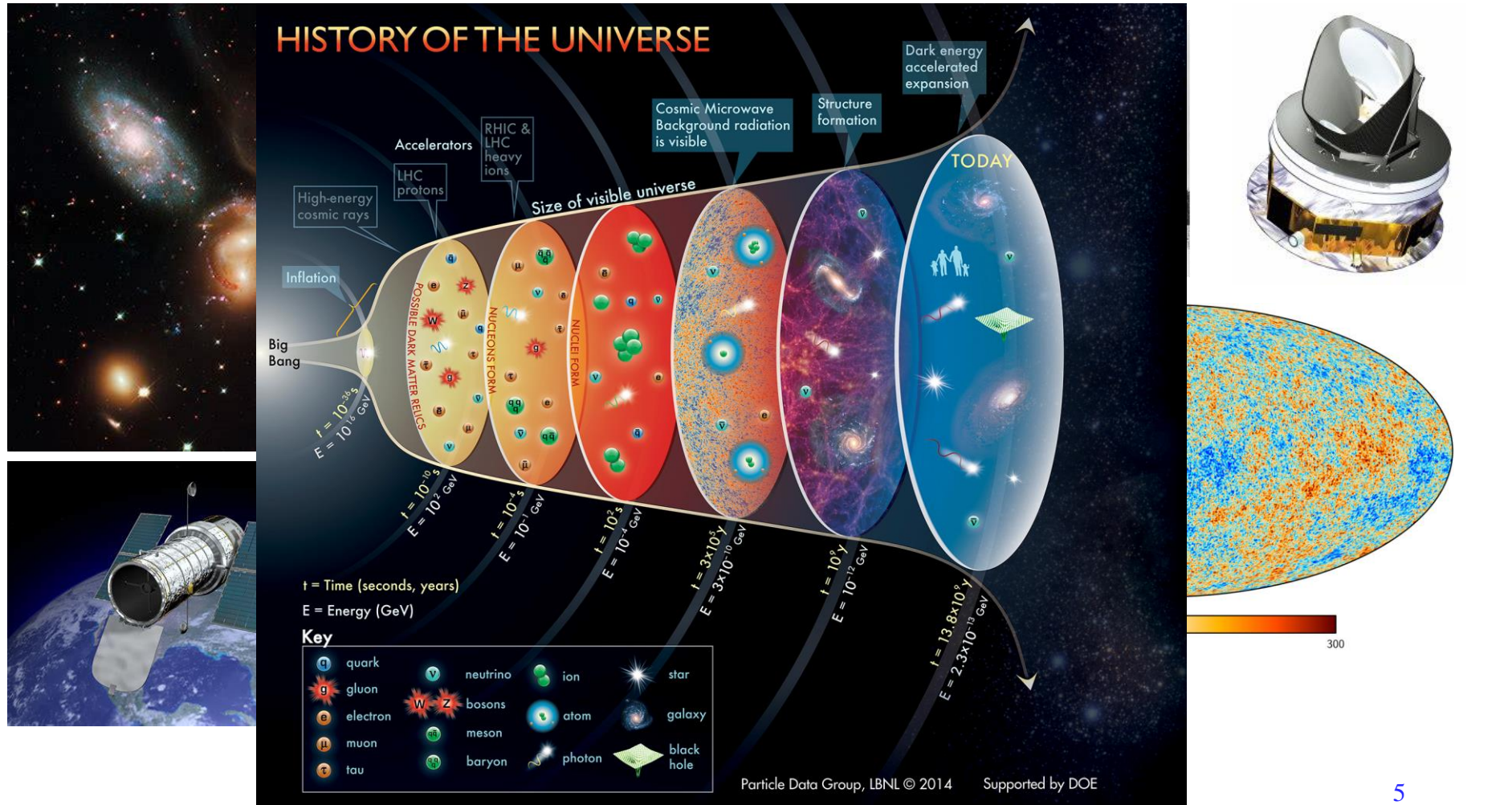


Rainer Weiss

For decisive contributions to the LIGO detector and the observation of gravitational waves

Seeing the Universe

Electromagnetic method



Gravitational Universe

- Opens a new window to uncover the Universe



- The dawn of multi-band/multi-messenger astronomy

eLISA, 1305.5720

GW tools

- Test of gravity in strong field and nonlinear regimes
- Provides model independent measurement of distance

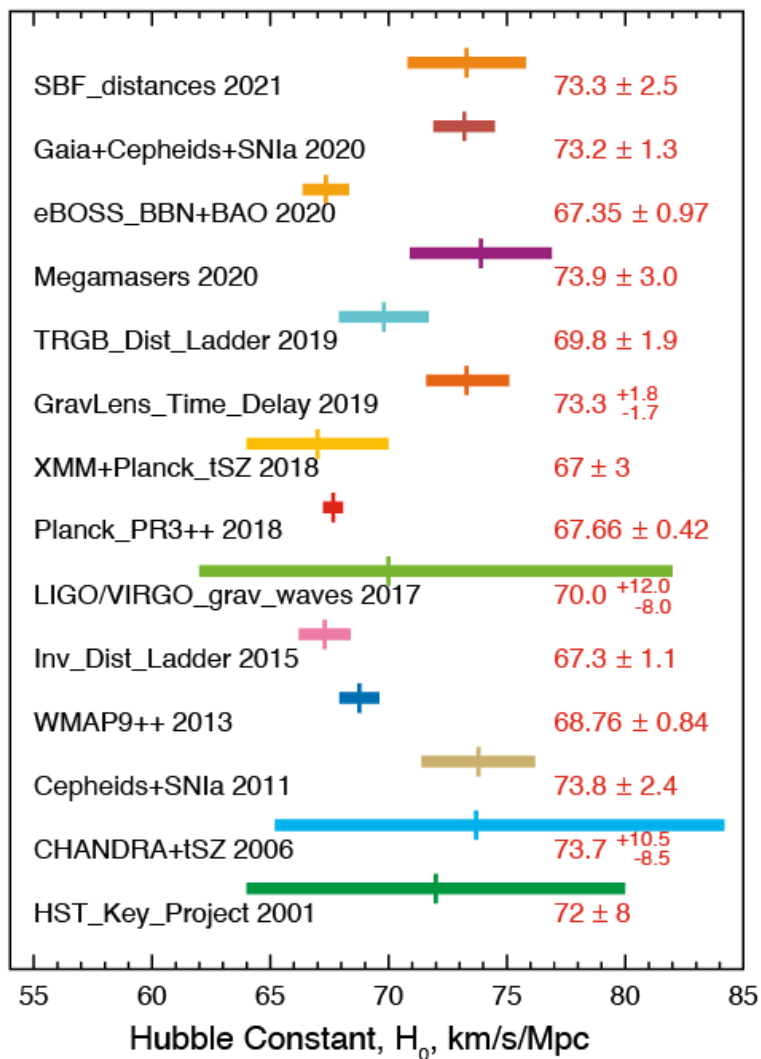
GW170817/GRB170817A



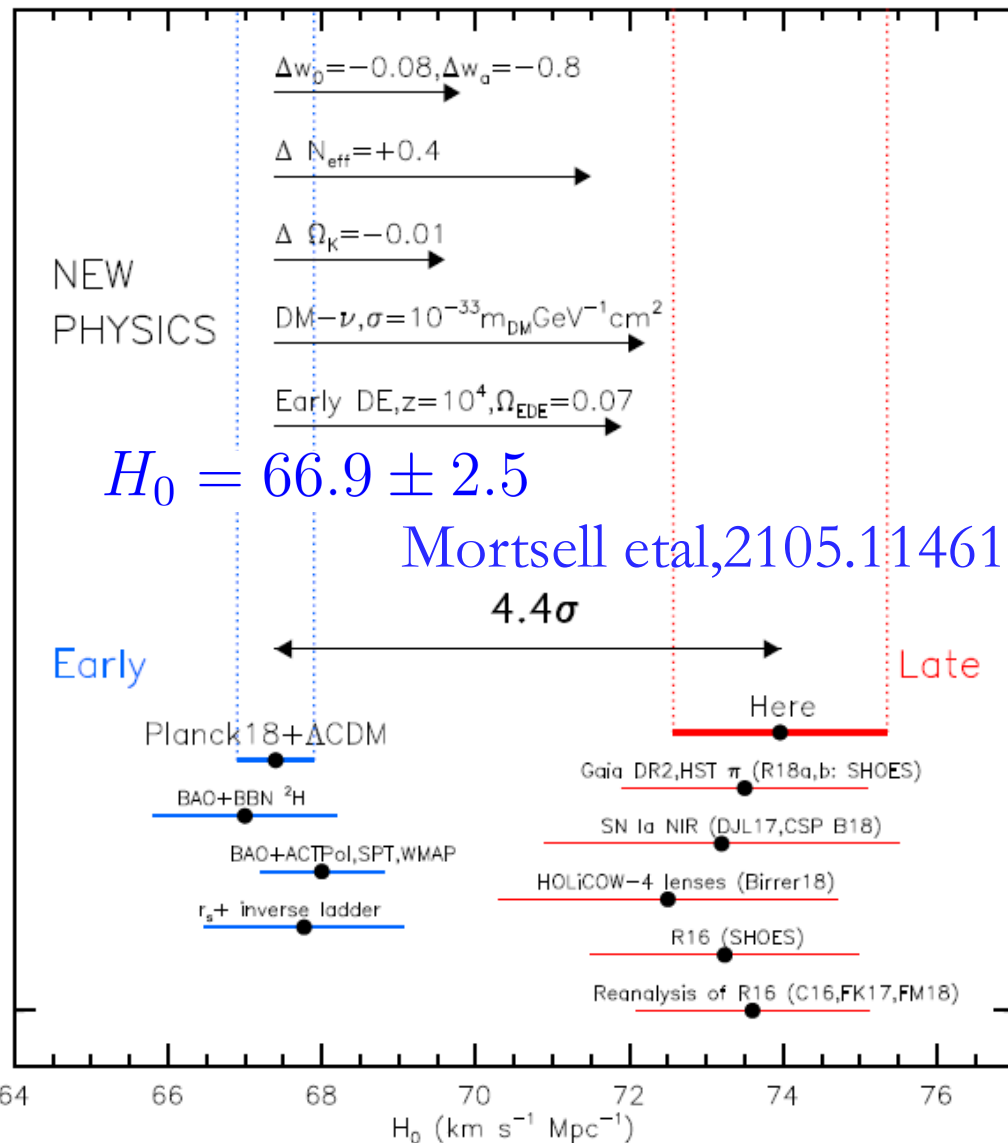
- Ground-based detectors: source localization
 - 10-1000Hz frequency band
 - A few seconds of signals
 - Stellar mass black holes and neutron stars
- Three or more detectors needed: Timing Triangulation



Hubble constant measurements



LAMBDA - February 2021

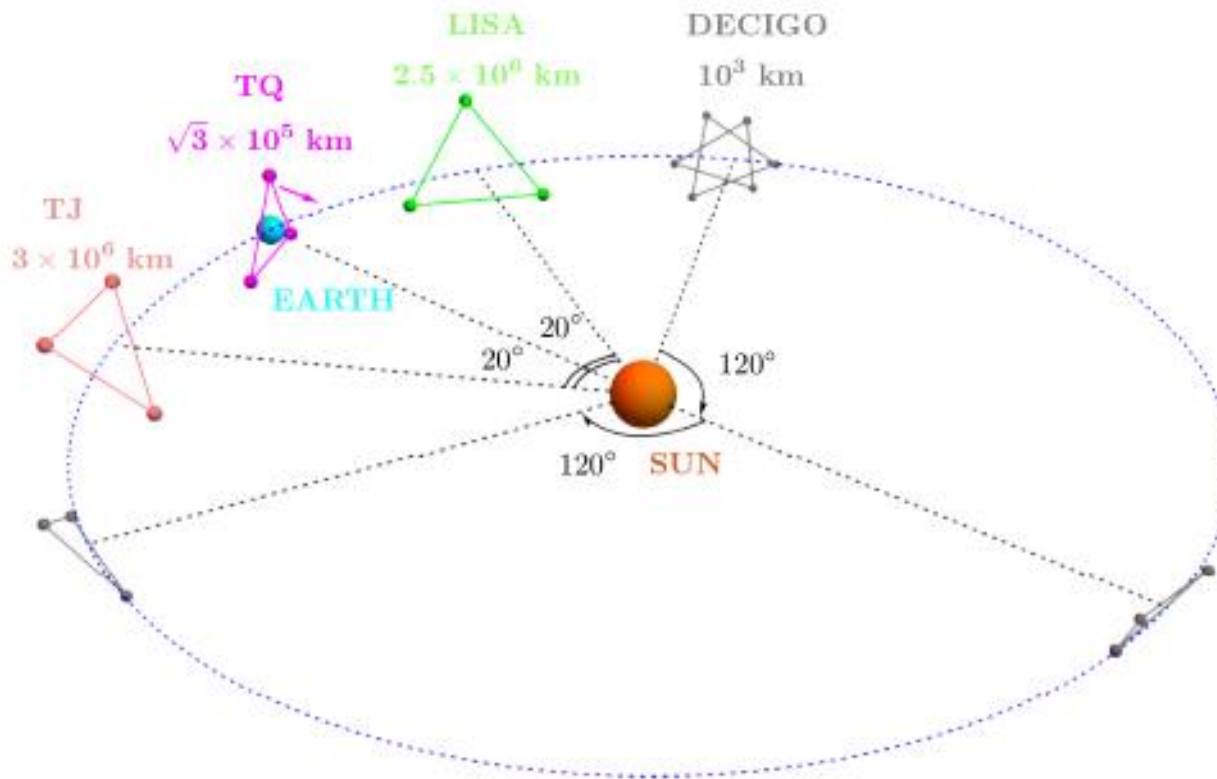


Spaceborne detectors

- Space-based detectors
 - mHz band
 - Last several years
 - Early inspiral signals (monochromatic): months to years before merger
 - Inspiral, merger and ringdown signals
 - Massive and Supermassive BHs
 - Extreme mass ratio inspiral (EMRI)
 - Sky localization and polarization measurement
 - The motion of detectors: Doppler modulation

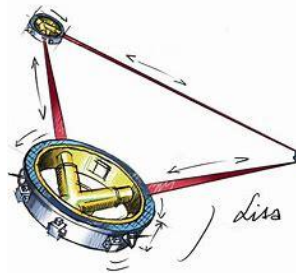
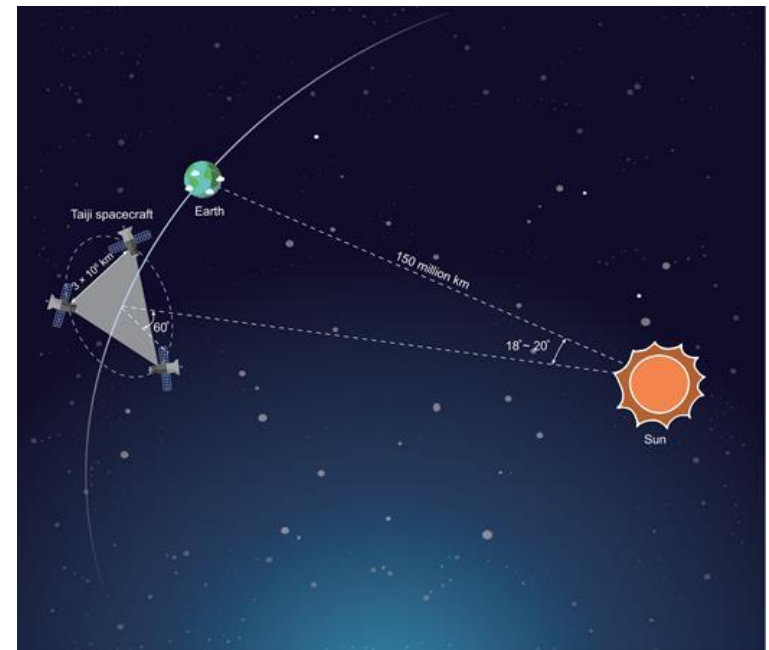
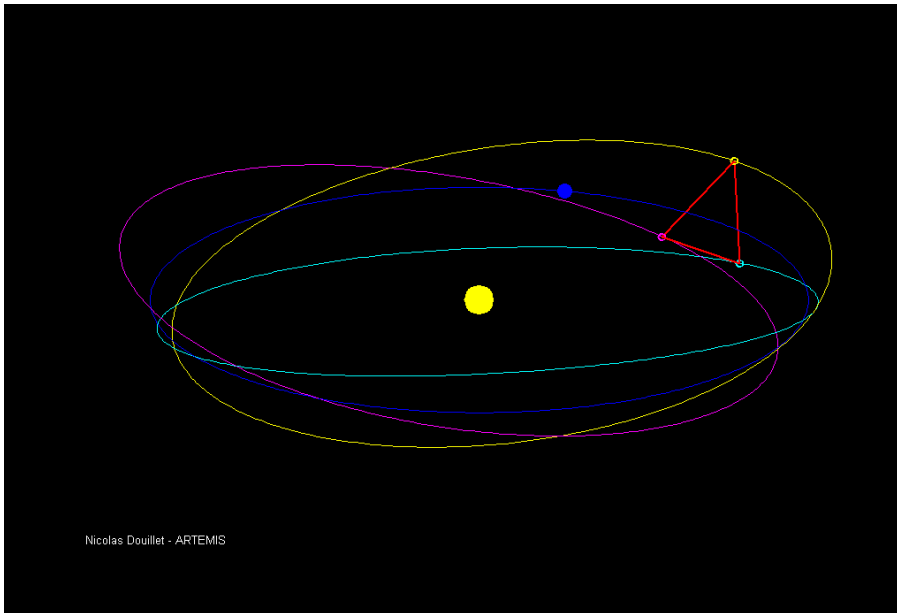
Space-based GW detectors

- LISA/Taiji/TianQin/DECIGO (OMEGA)



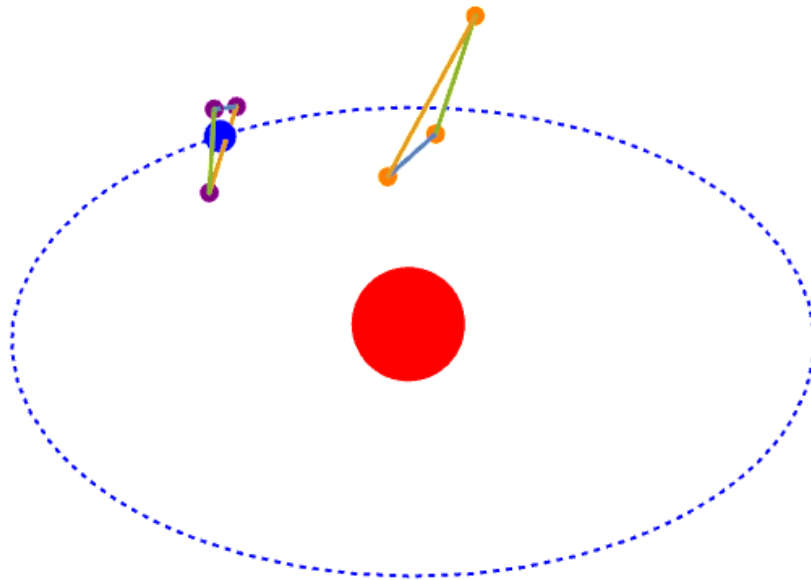
Space born GW detector

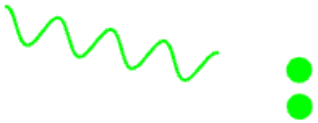
■ LISA/Taiji/TianQin: Polarization



LISA/Taiji/TianQin

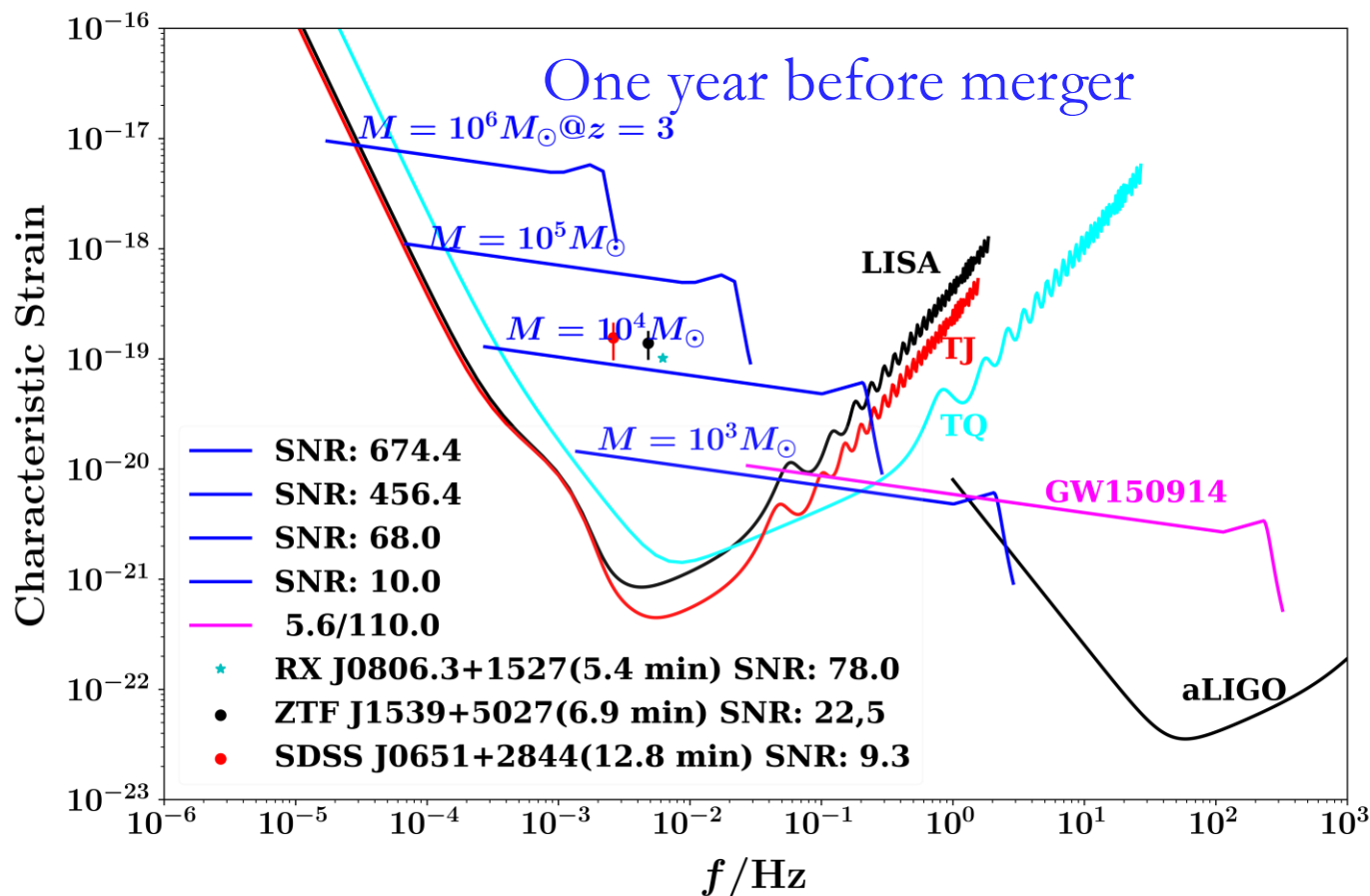
■ TianQin



A green wavy line representing a gravitational wave signal, followed by two green dots representing the source location.
RX J0806.3+1527

LISA/Taiji/TianQin

■ Noise Curve

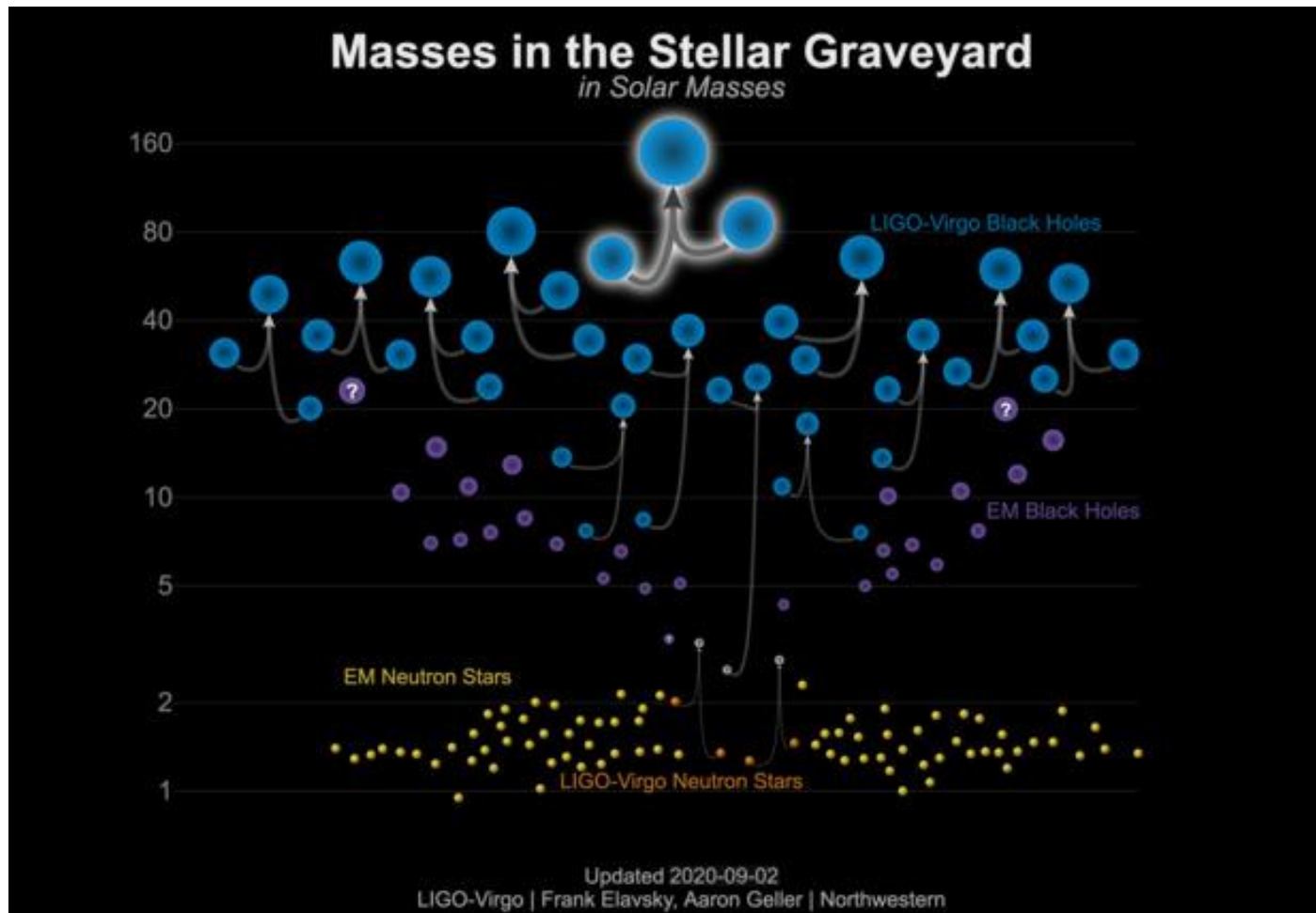


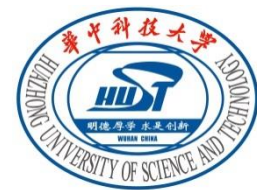
LIGO/Virgo Results

- Tens of GWs

GWTC-1: 1811.12907

GWTC-2: 2010.14527

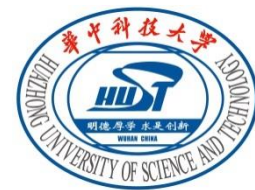




LIGO/Virgo Results

- GW170817: first BNS with EM counterparts, Standard Siren
- GW190425: BNS? 1.6/1.46 solar mass NS?
- GW190412: 30/8 BBH with asymmetric mass, higher multipoles
- GW190814: 23/2.6 solar mass, heaviest NS or lightest BH?
- GW190521: Intermediate mass BH, about 150 solar mass BH

GWTC2: 2010.14527



Primordial black holes (PBHs)

- PBHs: PBH forms in the radiation era as a result of gravitational collapse of density perturbations generated during inflation

Hawking, MNRAS 152 (1971) 75;

Carr & Hawking, MNRAS 168 (1974) 399

- PBHs: LIGO/Virgo BHs are PBHs?

PRL 116, 201301 (2016)

PHYSICAL REVIEW LETTERS

week ending
20 MAY 2016

Did LIGO Detect Dark Matter?

Simeon Bird,^{*} Ilias Cholis, Julian B. Muñoz, Yacine Ali-Haïmoud, Marc Kamionkowski,
Ely D. Kovetz, Alvise Raccanelli, and Adam G. Riess

PRL 117, 061101 (2016)

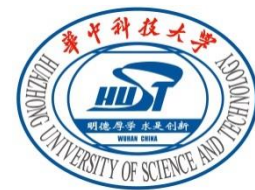
PHYSICAL REVIEW LETTERS

week ending
5 AUGUST 2016



Primordial Black Hole Scenario for the Gravitational-Wave Event GW150914

Misao Sasaki,¹ Teruaki Suyama,² Takahiro Tanaka,^{3,1} and Shuichiro Yokoyama⁴



PBHs from LIGO/Virgo

■ LIGO/Virgo

PHYSICAL REVIEW LETTERS **126**, 051101 (2021)

GW190521 Mass Gap Event and the Primordial Black Hole Scenario

V. De Luca¹, V. Desjacques², G. Franciolini¹, P. Pani^{3,4} and A. Riotto¹

PHYSICAL REVIEW LETTERS **126**, 071101 (2021)

GW190425; GW190814

Test for the Origin of Solar Mass Black Holes

Volodymyr Takhistov^{1,2,*}, George M. Fuller^{3,4,†} and Alexander Kusenko^{1,2}

Evidence from GWTC-2 data: 2102.03809;
2105.03349 → 30% PBHs

Evidence for PBH DM

■ Planet 9

PHYSICAL REVIEW LETTERS **125**, 051103 (2020)

Editors' Suggestion

Featured in Physics

What If Planet 9 Is a Primordial Black Hole?

Jakub Scholtz¹ and James Unwin²

■ NANOGrav

PHYSICAL REVIEW LETTERS **126**, 041303 (2021)

Editors' Suggestion

NANOGrav Data Hints at Primordial Black Holes as Dark Matter

V. De Luca^{1,*}, G. Franciolini^{1,†} and A. Riotto^{1,2,‡}

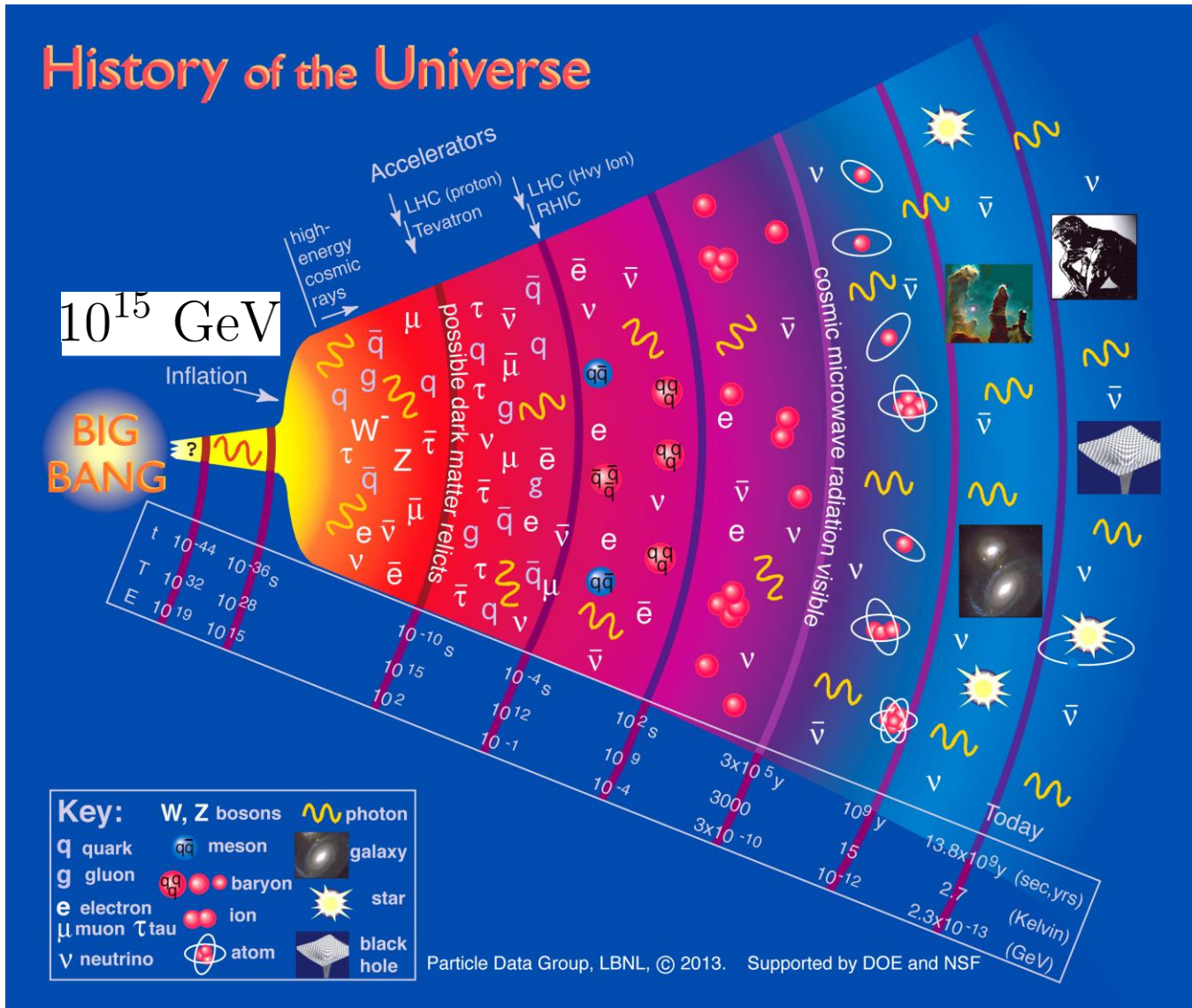
PHYSICAL REVIEW LETTERS **126**, 051303 (2021)

Editors' Suggestion

Did NANOGrav See a Signal from Primordial Black Hole Formation?

Ville Vaskonen^{1,*} and Hardi Veermäe^{2,†}

Early Universe



Inflationary models

- The power spectrum is parameterized

$$\mathcal{P}_{\mathcal{R}} = \frac{k^3}{2\pi^2} |\mathcal{R}_k|^2 = A_{\mathcal{R}}(k_*) \left(\frac{k}{k_*} \right)^{n_s - 1 + \frac{1}{2} n'_s \ln(k/k_*) + \dots}$$

order of 10^{-9}

$$\mathcal{P}_T = A_T(k_*) \left(\frac{k}{k_*} \right)^{n_t + \frac{1}{2} n'_t \ln(k/k_*) + \dots} \approx 64\pi G \left(\frac{H}{2\pi} \right)^2$$

$$n_s - 1 = \left. \frac{d \ln \mathcal{P}_{\mathcal{R}}}{d \ln k} \right|_{k=aH} = 3 - 2\nu = 2\eta_H - 4\epsilon_H \approx 2\eta - 6\epsilon$$

$$r = \frac{A_T}{A_{\mathcal{R}}} = 16\epsilon_H = 16\epsilon = -8n_T \quad A_T = r A_{\mathcal{R}} \sim H^2 \sim V(\phi)$$

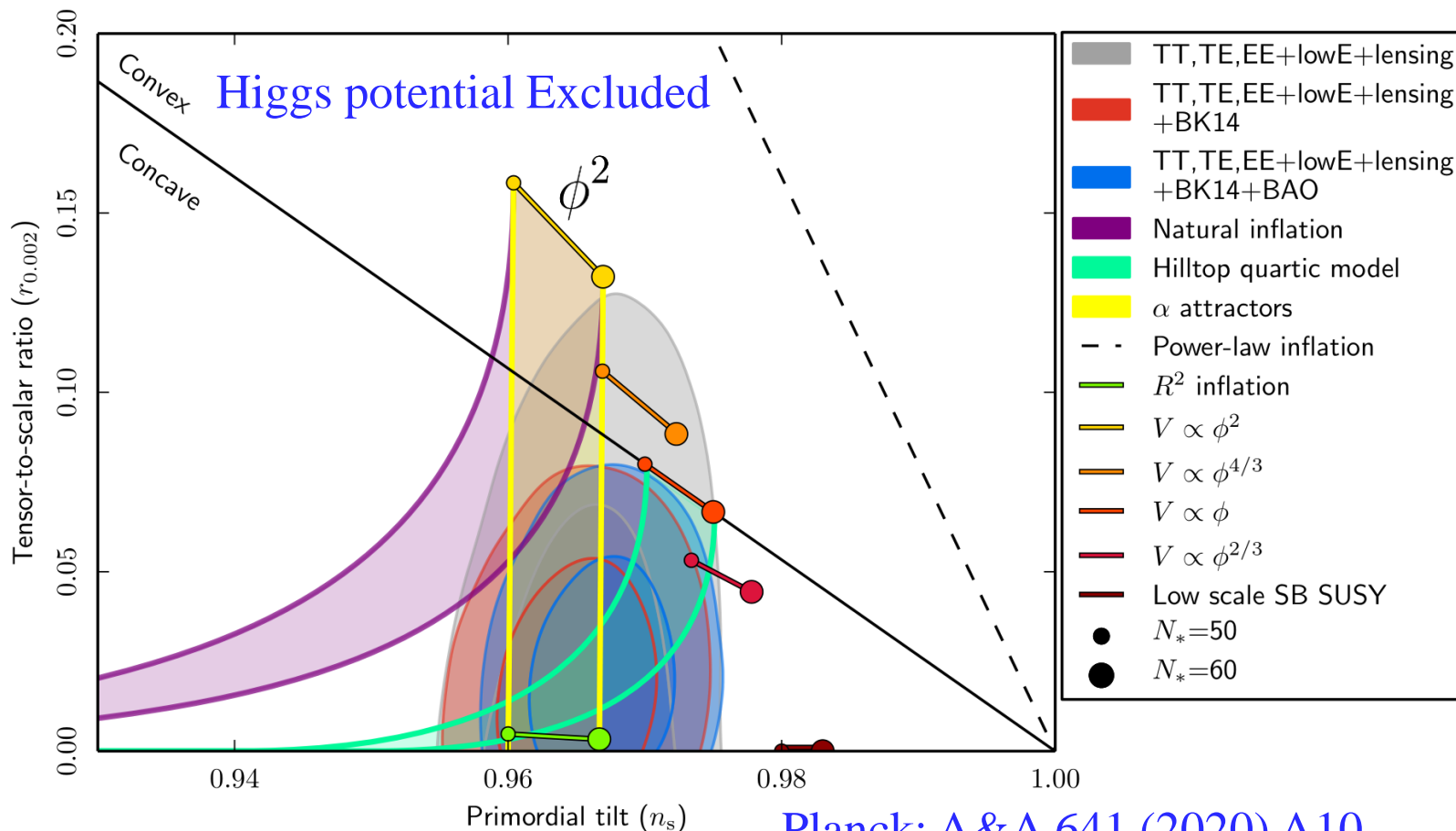
- Energy scale of inflation: measurement of r

CMB constraints

Planck 18

$$\ln(10^{10} A_s) = 3.044 \pm 0.014 \quad \text{order of } 10^{-9}$$

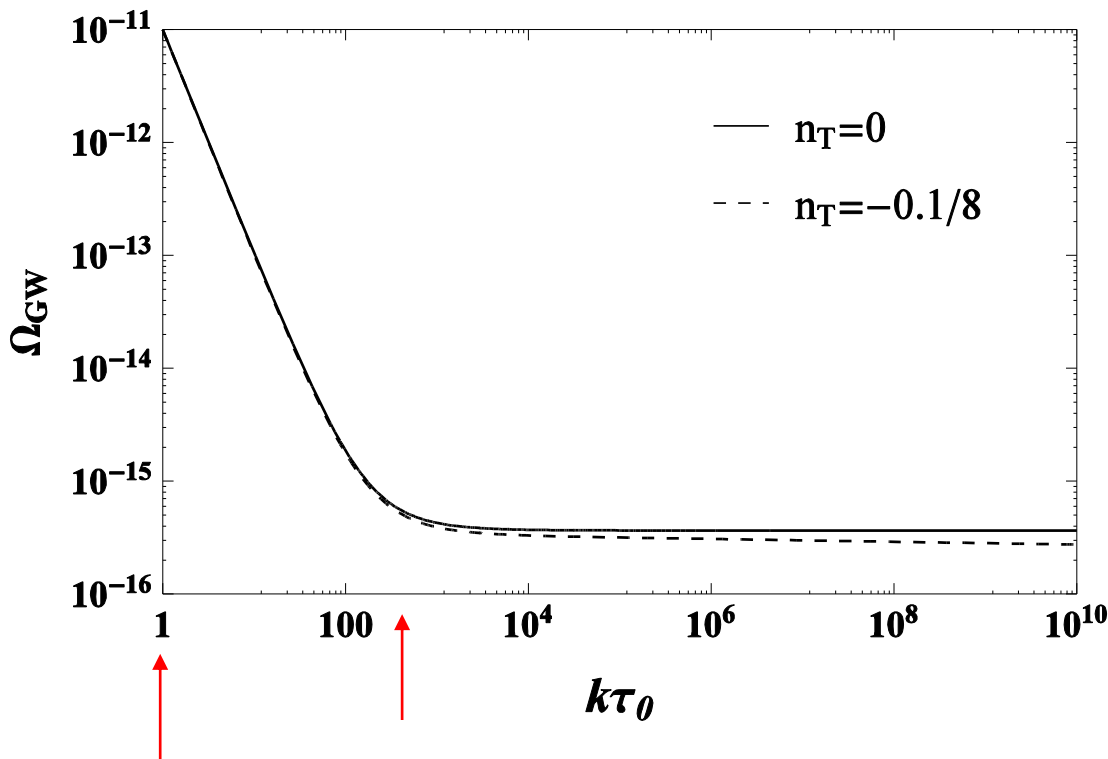
$$r_{0.05} < 0.06, \quad 95\%$$



Planck: A&A 641 (2020) A10

BICEP: PRL 121 (2018) 221301

Primordial GWs



arXiv: 1502.02114
1502.01589

$$\Omega_{m0} = 0.3156$$

$$H_0 = 67.27 \text{ km/s/Mpc}$$

$$T_{\gamma 0} = 2.725 \text{ K}$$

$$r = 0.1$$

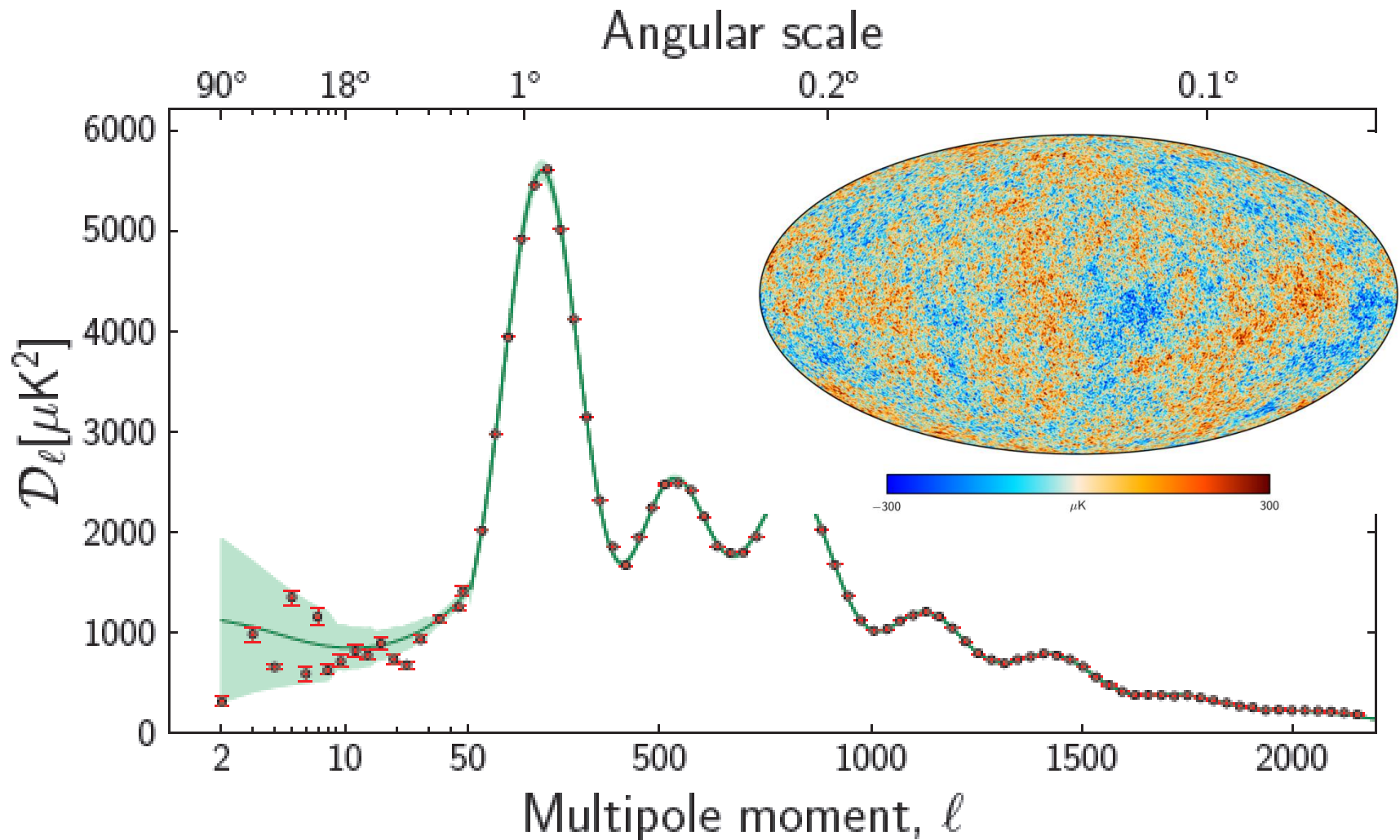
$$A_s = 2.2 \times 10^{-9}$$

Size of universe
14161.5 Mpc
 $2.2 \times 10^{-18} \text{ Hz}$

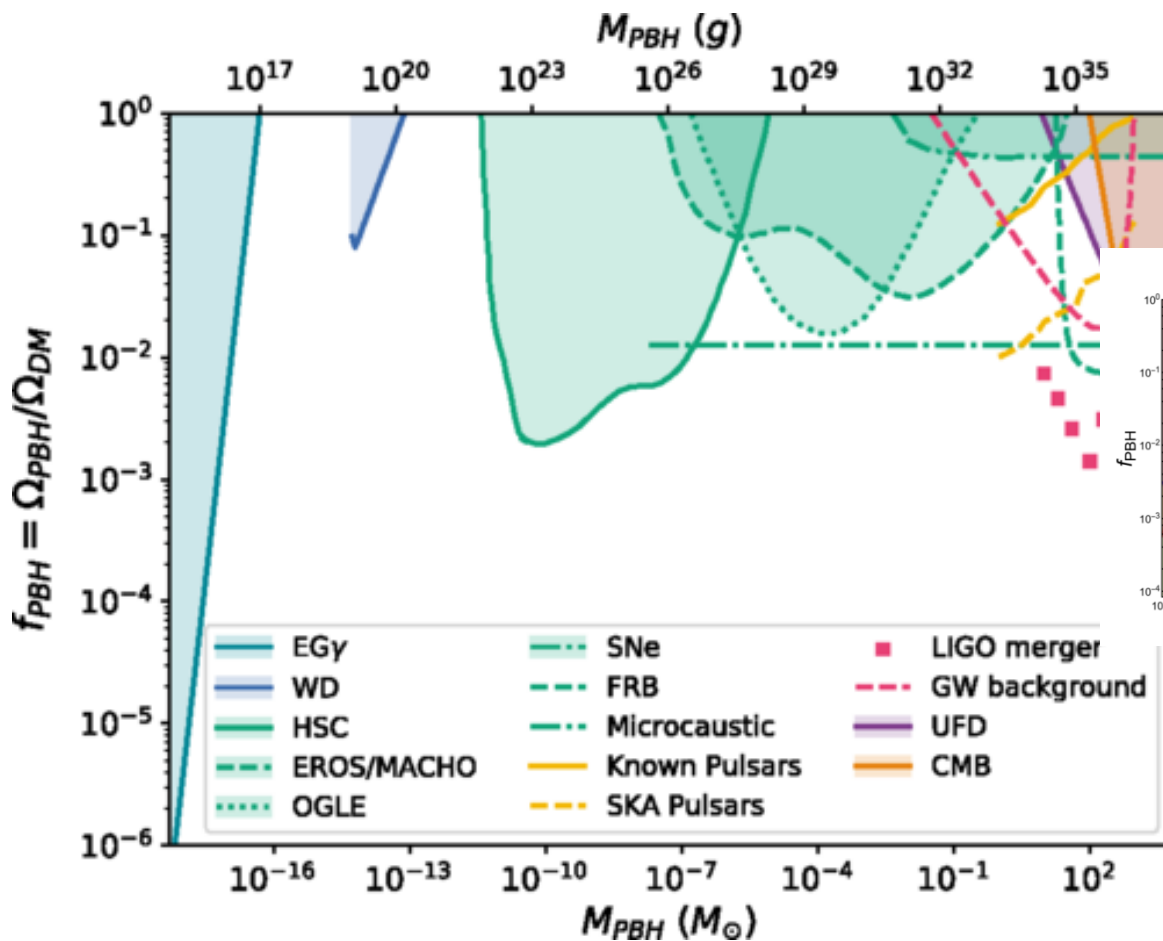
Equality
112.1 Mpc
 $1.0 \times 10^{-16} \text{ Hz}$

End of inflation $\sim 10^{15} \text{ GeV}$
 $8.9 \times 10^7 \text{ Hz}$

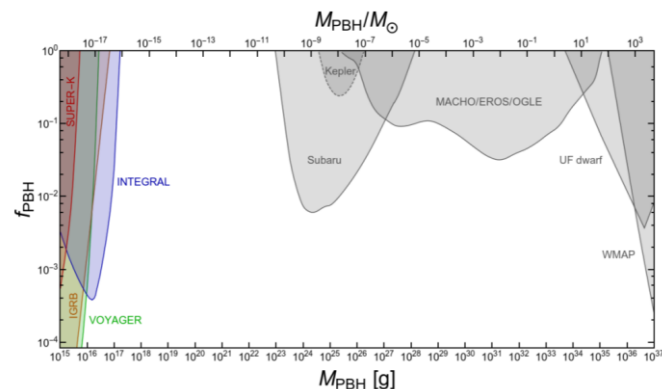
Primordial temperature spectrum



PBH constraints



Spinning PBHs

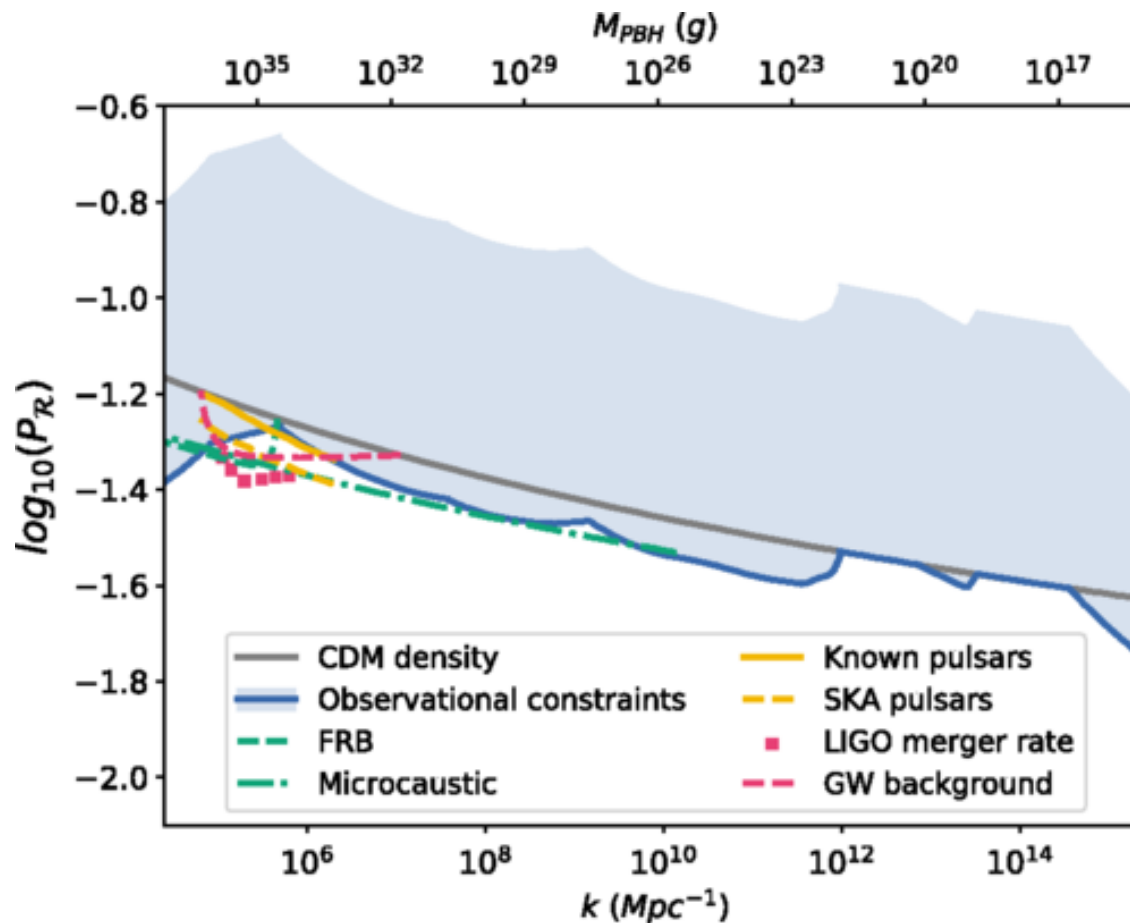


Dasgupta, Laha and Ray,
PRL 125 (2020) 101101

Sato-Polito, Kovetz, Kamionkowski, PRD 100 (19) 063521

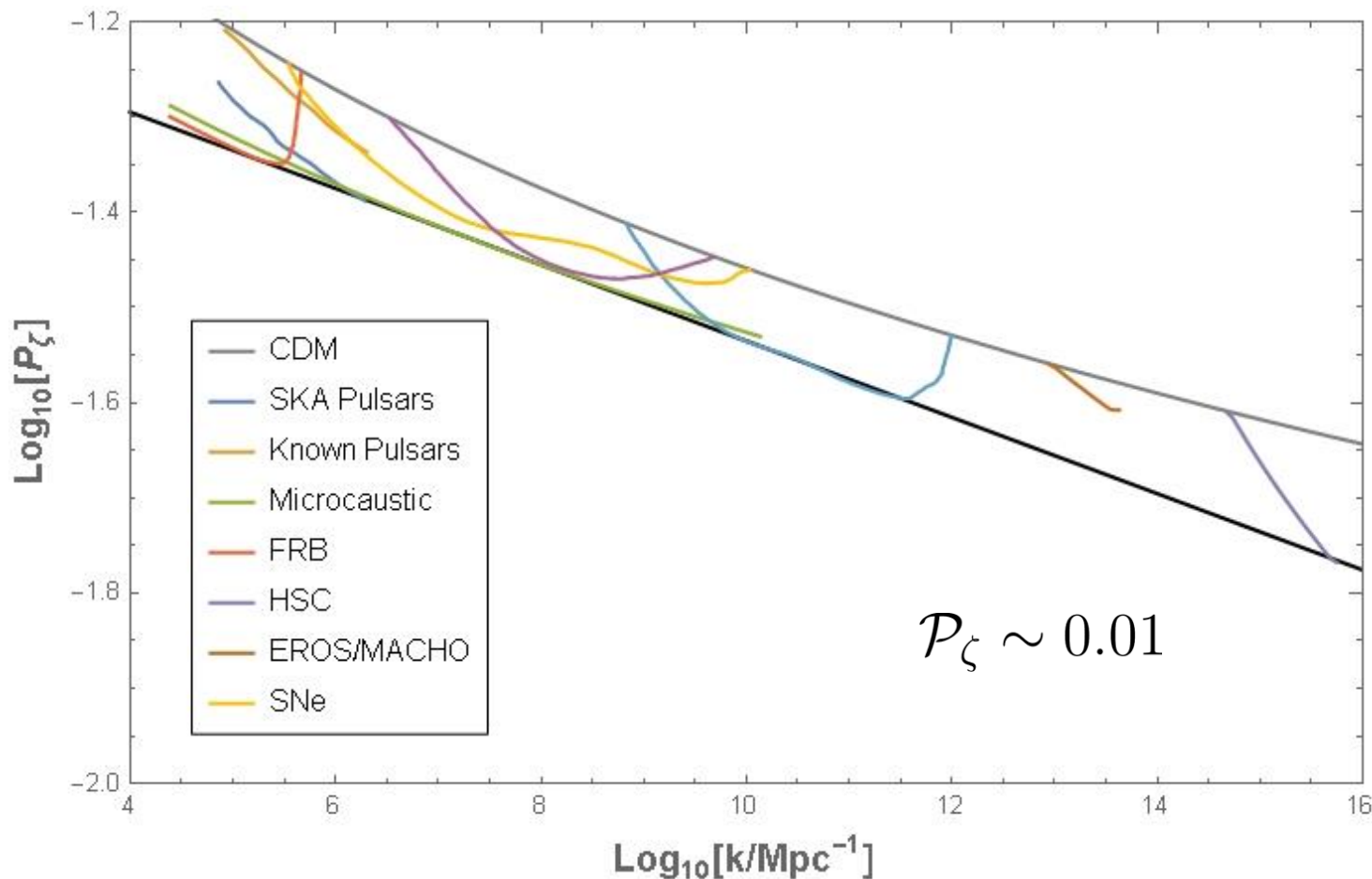
Observational constraints

- PBH fraction** $f_{\text{PBH}} \Rightarrow \mathcal{P}_\zeta$ $\beta = \frac{\rho_{\text{PBH}}}{\rho_{\text{tot}}} \approx \text{erfc} \left(\frac{\delta_c}{\sqrt{2\mathcal{P}_\delta}} \right) = \text{erfc} \left(\frac{9\delta_c}{4\sqrt{\mathcal{P}_\zeta}} \right)$



Constraints on power spectrum

■ Result



Scalar induced GWs (SIGWs)

■ Tensor-scalar mixing

First order scalar perturbations as the source of the second order tensor perturbation $\Phi, \Psi \sim 0.1$

$$h''_{ij} + 2\mathcal{H}h'_{ij} - \nabla^2 h_{ij} = -4S_{ij}$$

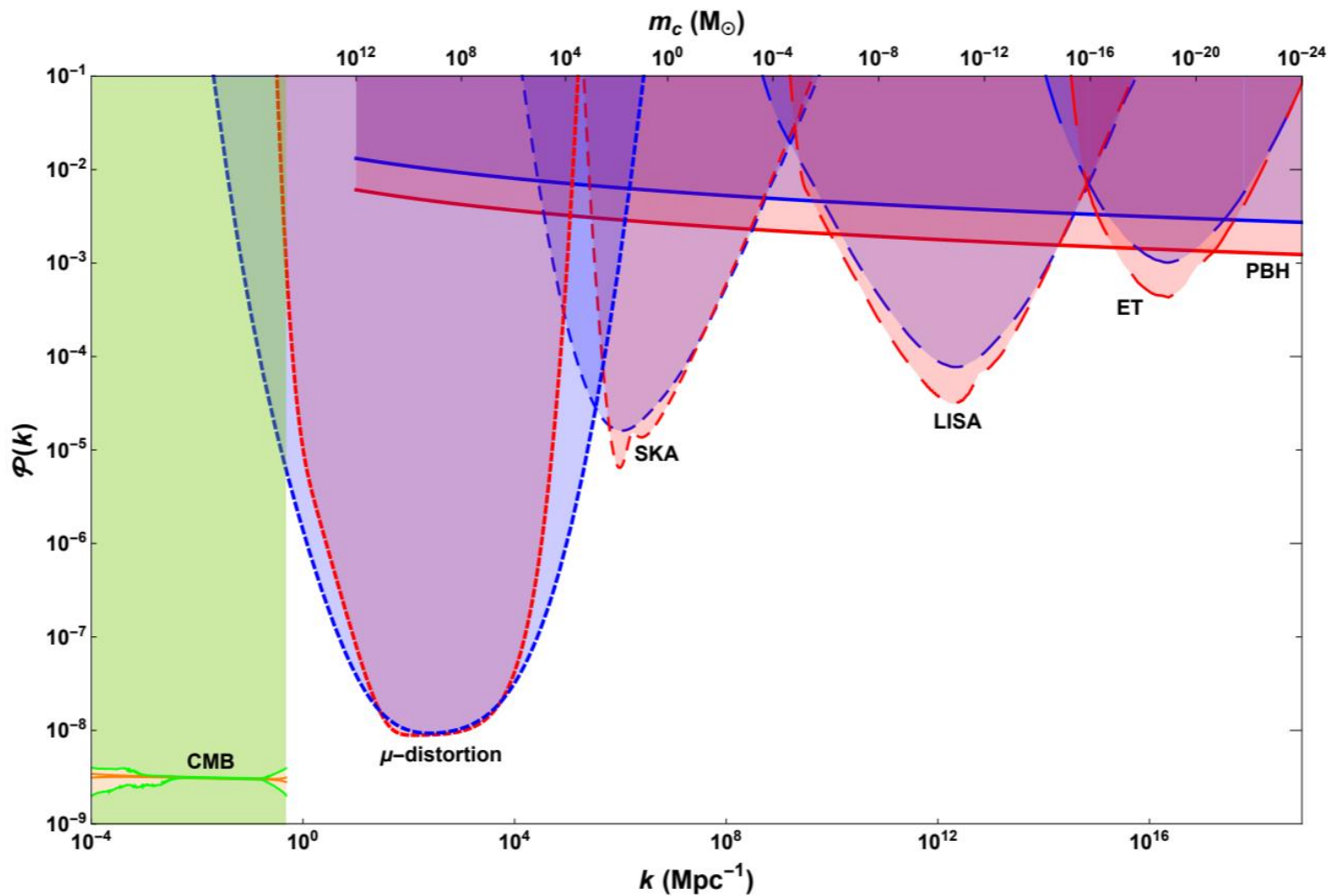
$$S_{ij} = 2\Phi\Phi_{,ij} + 2\Psi\Psi_{,ij} + \Phi_{,i}\Phi_{,j} + 3\Psi_{,i}\Psi_{,j} - \Psi_{,i}\Phi_{,j} - \Phi_{,i}\Psi_{,j} - \frac{4}{3(1+w)\mathcal{H}^2}(\Psi' + \mathcal{H}\Phi)_{,i}(\Psi' + \mathcal{H}\Phi)_{,j}$$

$$h_{ij}(\mathbf{x}, \eta) = \frac{1}{(2\pi)^{3/2}} \int d^3k e^{i\mathbf{k}\cdot\mathbf{x}} [h_{\mathbf{k}}(\eta)e_{ij}(\mathbf{k}) + \tilde{h}_{\mathbf{k}}(\eta)\tilde{e}_{ij}(\mathbf{k})]$$

$$\langle h_{\mathbf{k}}(\eta)h_{\tilde{\mathbf{k}}}(\eta) \rangle = \frac{2\pi^2}{k^3} \delta^{(3)}(\mathbf{k} + \tilde{\mathbf{k}}) \mathcal{P}_h(k, \eta)$$

$$\Omega_{\text{GW}}(k, \eta) = \frac{1}{24} \left(\frac{k}{aH} \right)^2 \overline{\mathcal{P}_h(k, \eta)}$$

GW Constraints



Gow, Byrnes, Cole, Young, JCAP 02 (2021) 002

Enhancement: generic feature

Very small ϵ at small scales

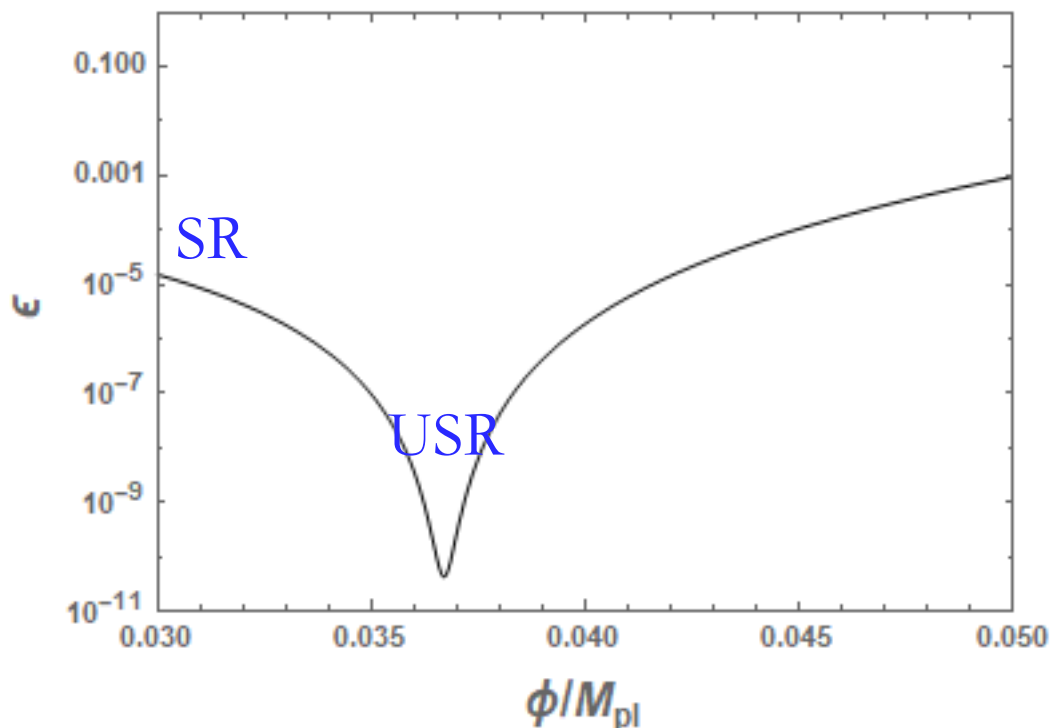
Slow-roll inflation H^2

$$\mathcal{P}_\zeta = \frac{H^2}{8\pi^2\epsilon}$$

$$\mathcal{P}_\zeta \sim 10^{-9} \text{ Large scales}$$



$$\mathcal{P}_\zeta \sim 0.01 \text{ Small scales}$$



$$\epsilon = \frac{1}{2} \left(\frac{V_\phi}{V} \right)^2 \sim 0$$

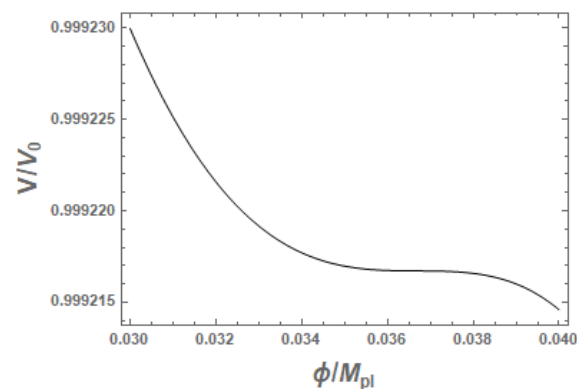
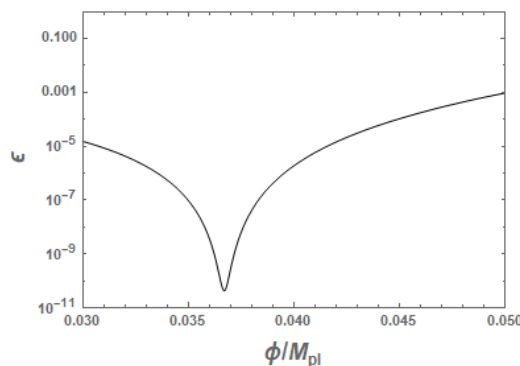
Motivation and
Goal: Decrease by 7
orders of magnitude

Slow-roll parameter ϵ cannot increase monotonically

Inflection point inflation

- Small ϵ requires very flat potential: inflection point

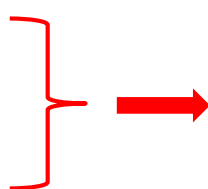
$$\mathcal{P}_\zeta = \frac{H^2}{8\pi^2\epsilon}$$



- Ultra-slow-roll inflation

$$\ddot{\phi} + 3H\dot{\phi} + V_\phi(\phi) = 0$$

$$V_\phi(\phi) = 0$$



$$\eta_H = -\frac{\ddot{\phi}}{H\dot{\phi}} = 3 \quad \text{constant-roll}$$

Slow-roll

$$3H\dot{\phi} \approx -V_\phi(\phi) = 0$$

Break-down of slow-roll

Tsamis, Woodard, PRD 69 (04) 084005;

Motohashi, Starobinsky, Yokoyama, JCAP 1509, 018

Ultra-slow-roll inflation

- The field rolls faster $\dot{\phi} \propto a^{-3}$ $\rho_{\phi}^{KE} \propto a^{-6}$

$$N = \int_{\phi}^{\phi_e} \frac{d\phi}{\sqrt{2\epsilon(\phi)}}$$

N can be much larger than 60

Breakdown of Lyth bound

USR helps to reduce N

The contribution to N during ultra-slow-roll inflation (inflection point) becomes smaller

$$\eta_H = -\frac{\ddot{\phi}}{H\dot{\phi}} = 3$$

- Constant roll η_H constant

$$n_s - 1 = 3 - 2\nu \quad \nu = \left| \frac{3}{2} - \eta_H \right| + \frac{(6 - 5\eta_H - 4\eta_H^2) \epsilon_H}{|3 - 2\eta_H| (1 + 2\eta_H)}$$

- How to enhance the power spectrum at the power spectrum while keeping the number of e-folds to be around 60

Modified model

Polynomial potential

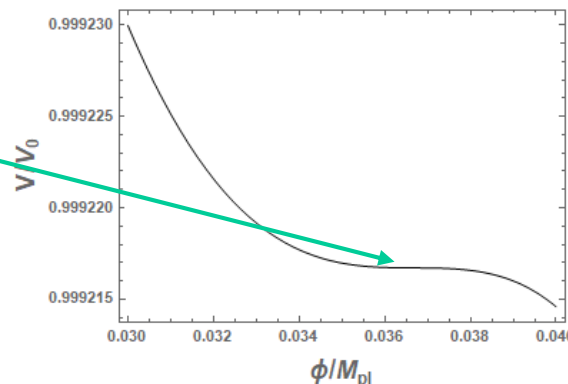
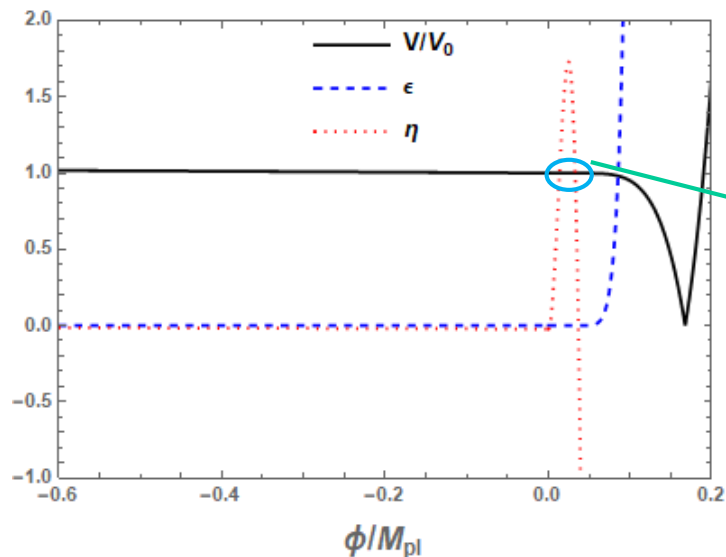
Di & Gong, JCAP 07 (18) 007

$$V(\phi) = \begin{cases} V_0 \left[1 + \sum_{m=1}^{m=5} \lambda_m \left(\frac{\phi}{M_{\text{Pl}}} \right)^m \right], & \phi \geq 0, \\ V_0 \left[1 + \sum_{m=3}^{m=5} \lambda_m \left(\frac{\phi}{M_{\text{Pl}}} \right)^m \right], & \phi < 0, \end{cases}$$

fine-tuning

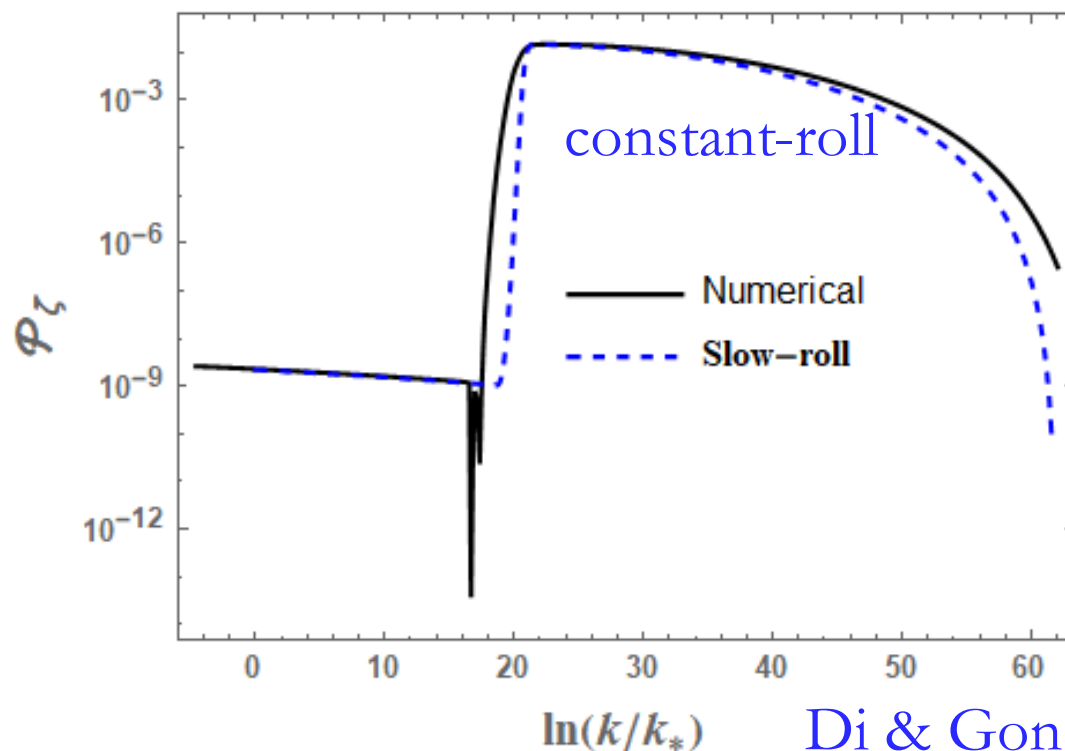
$$\lambda_1 = -0.0353553, \quad \lambda_2 = -0.0115783, \quad \lambda_3 = -0.00235702,$$

$$\lambda_4 = 728.239, \quad \lambda_5 = -11882.9$$



The power spectrum

■ Numerical solution



Di & Gong, JCAP 07 (18) 007

$$k_* = 0.05 \text{Mpc}^{-1}, n_s = 0.9674, r = 0.005, n'_s = -0.0008$$

Peak value $\mathcal{P}_\zeta = 0.0175$

Ultra-slow-roll to SR

■ USR to SR transition

$$V(\phi) = V_0 + \frac{\beta}{2} \left[\phi + \delta_1 \log \left\{ \cosh \left(\frac{\phi - \phi_1}{\delta_1} \right) \right\} \right] + \frac{\gamma}{2} \left[\phi - \delta_2 \log \left\{ \cosh \left(\frac{\phi_2 - \phi}{\delta_2} \right) \right\} \right]$$

$$\{\beta, \phi_1, \delta_1\} = \{10^{-14}, 0, 10^{-2}\} \quad \gamma = 6 \times 10^{-21}$$

fine-tuning

Fast transition $\phi_2 = -0.1580281699$ $\delta_2 = 2.12 \times 10^{-10}$

Slow transition $\phi_2 = -0.1580282187$, $\delta_2 = 3.6 \times 10^{-8}$

Ultra-slow-roll models

■ String inflation

$$V_{\text{inf}} = \frac{W_0^2}{\mathcal{V}^3} \left[\frac{C_{\text{up}}}{\mathcal{V}^{1/3}} - \frac{C_W}{\sqrt{\tau_{K3}}} + \frac{A_W}{\sqrt{\tau_{K3}} - B_W} + \frac{\tau_{K3}}{\mathcal{V}} \left(D_W - \frac{G_W}{1 + R_W \frac{\tau_{K3}^{3/2}}{\mathcal{V}}} \right) \right]$$

fine-tuning

	C_W	A_W	B_W	$G_W/\langle\mathcal{V}\rangle$	$R_W/\langle\mathcal{V}\rangle$	$\langle\tau_{K3}\rangle$	$\langle\mathcal{V}\rangle$
\mathcal{P}_1	1/10	2/100	1	1.303386×10^{-3}	6.58724×10^{-3}	3.89	107.3
\mathcal{P}_2	4/100	2/100	1	3.080548×10^{-5}	7.071067×10^{-4}	14.30	1000
\mathcal{P}_3	1.978/100	1.65/100	1.01	9.257715×10^{-8}	1.414×10^{-5}	168.03	5×10^4

M. Cicoli, V.A. Diaz, F.G. Pedro, JCAP 1806, 034

■ SUGRA $W = a_0(1 + a_1 e^{-b_1 \Phi} + a_2 e^{-b_2 \Phi} + a_3 e^{-b_3 \Phi})$.

	a_0	a_3	b_1	b_2	b_3	c
1	4.35×10^{-6}	7×10^{-8}	3.05	6.3868164	-4.4	2.8
2	4.06×10^{-6}	1×10^{-6}	2.89	7.251197	-3.2	2.85

T.J. Gao, Z.K. Guo, PRD
98, 063526

Higgs field

- Higgs particle

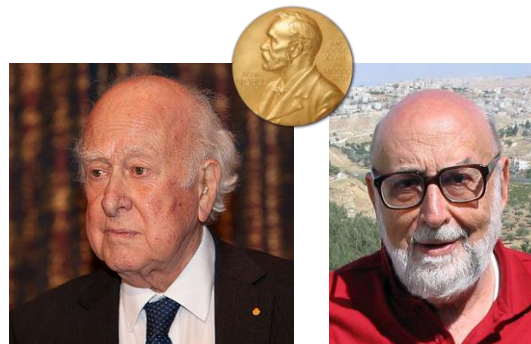
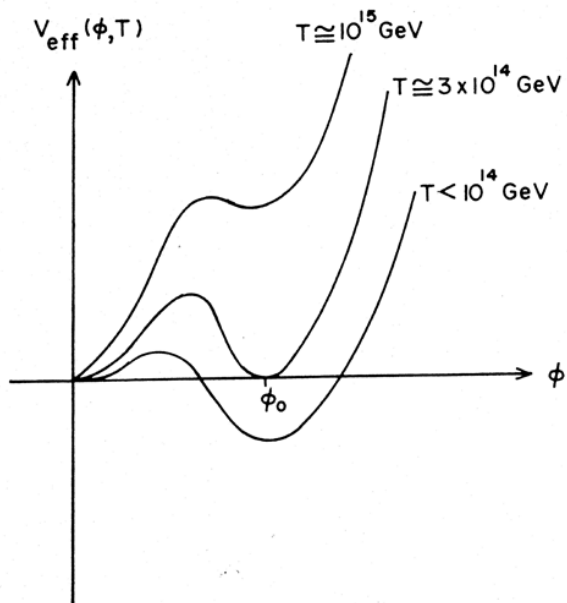
$m = 125 \text{ GeV}$ 2012

- 2013 Nobel prize

$$V(\phi) = \frac{\lambda}{4}(\phi^2 - v^2)^2 + bT^2\phi^2$$

$$V(\phi) = \frac{\lambda}{4}\phi^4, \quad T \gg T_{crt}$$

A. Linde, 80s



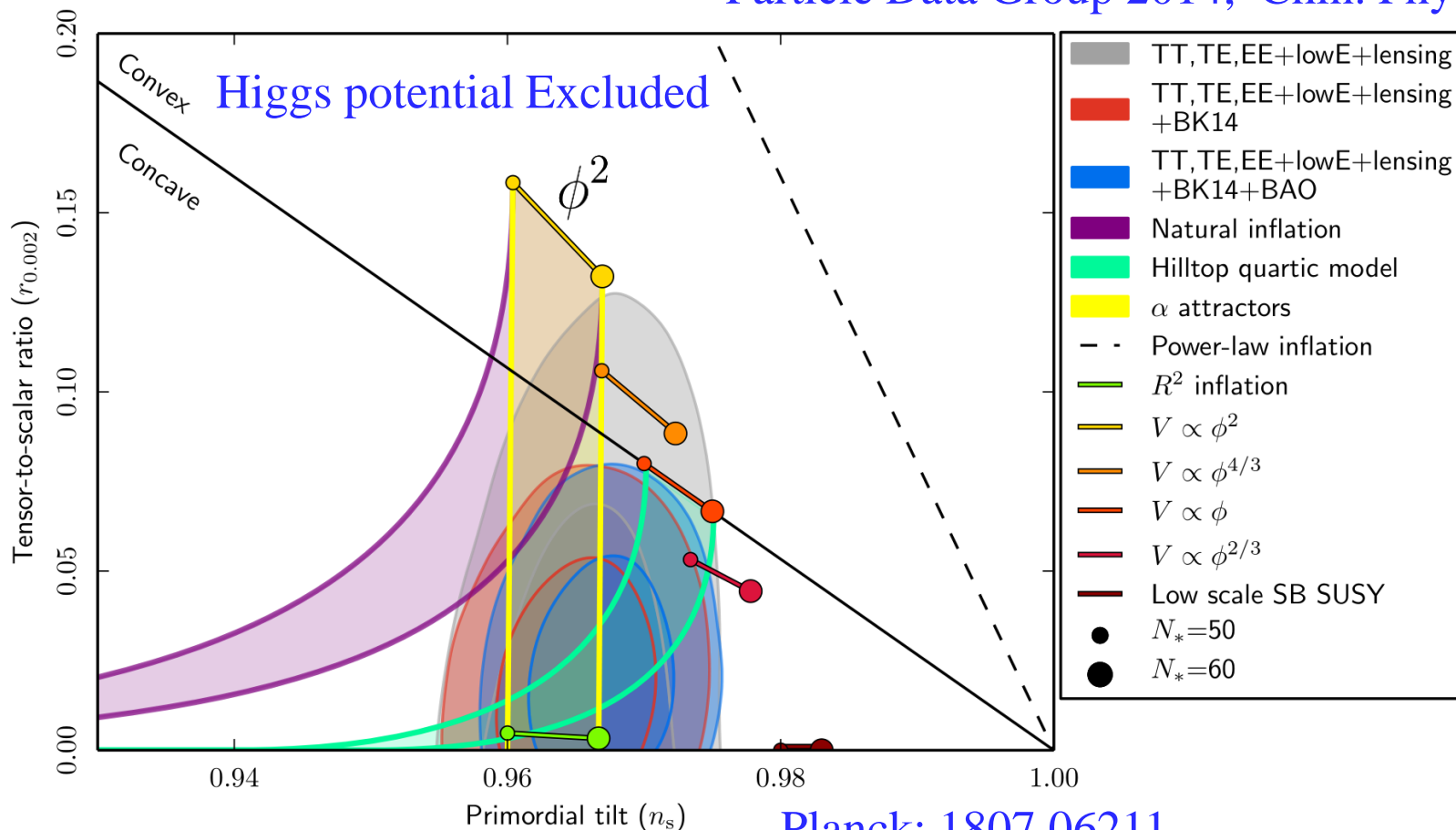
Higgs

Englert

CMB constraints

■ Planck 18 $V(h_c) = \frac{1}{4} \lambda h_c^4 \quad \lambda = 0.13$

Particle Data Group 2014, Chin. Phys. C



Planck: 1807.06211

BICEP: PRL 121 (2018) 221301

Higgs inflation

■ Nonminimal coupling

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2} (1 + \xi \phi^2) R - \frac{1}{2} g^{\mu\nu} \nabla_\mu \phi \nabla_\nu \phi - \frac{1}{4} \lambda \phi^4 \right]$$

Strong coupling attractors $n_s \approx 1 - \frac{2}{N}, \quad r \approx \frac{12}{N^2}$

Kaiser, PRD 52 (95) 4295

Bezrukov and Shaposhnikov, PLB 659 (08) 703

■ Critical inflation

RG running of coupling constant $\lambda = 0, \quad \beta_\lambda = 0$

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu) \quad \xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu)$$

Hamada, Kawai, Oda and Park, PRL 112, 241301

Bezrukov and Shaposhnikov, PLB 734 (14) 249

Critical Higgs Inflation

■ The Higgs inflation (nonminimal coupling)

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2} (1 + \xi \phi^2) R - \frac{1}{2} g^{\mu\nu} \nabla_\mu \phi \nabla_\nu \phi - \frac{1}{4} \lambda(\phi) \phi^4 \right]$$

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu) \quad \xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu)$$

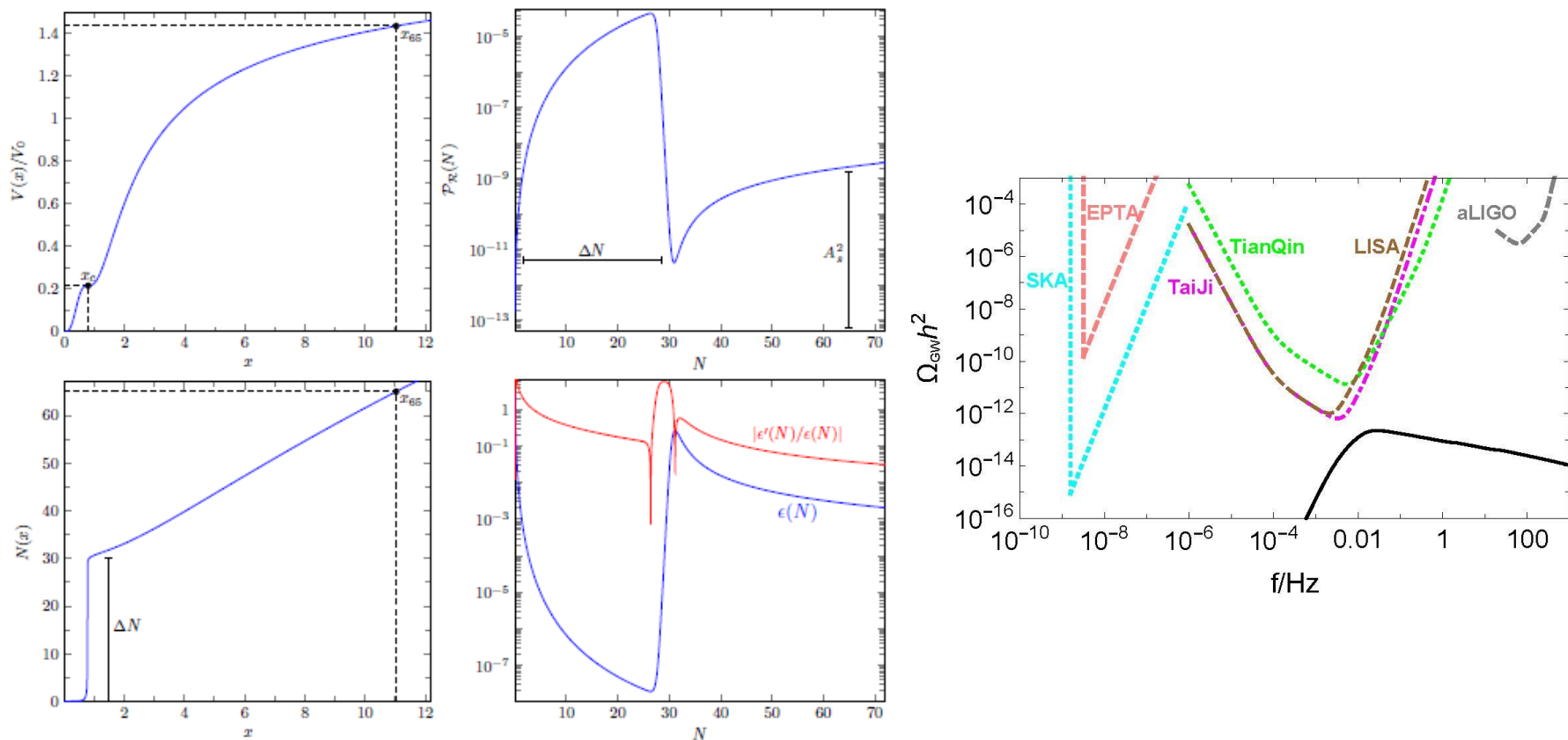
$$S = \int dx^4 \sqrt{-g} \left[\frac{1}{2} R - \frac{1 + \xi \phi^2 + 6(\xi \phi + \xi_\phi \phi^2/2)^2}{(1 + \xi \phi^2)^2} \frac{1}{2} g_{\mu\nu} \nabla^\mu \phi \nabla^\nu \phi - V(\phi) \right]$$

$$V(x) = \frac{V_0 (1 + a \ln^2 x) x^4}{[1 + c(1 + b \ln x) x^2]^2},$$

$$x = \phi/\mu, \quad V_0 = \lambda_0 \mu^4/4, \quad a = \lambda_1/\lambda_0, \quad b = \xi_1/\xi_0 \quad \text{and} \quad c = \xi_0 \mu^2.$$

Critical Higgs Inflation

■ The Higgs inflation (nonminimal coupling)



$$n_s = 0.952, \quad r = 0.043.$$

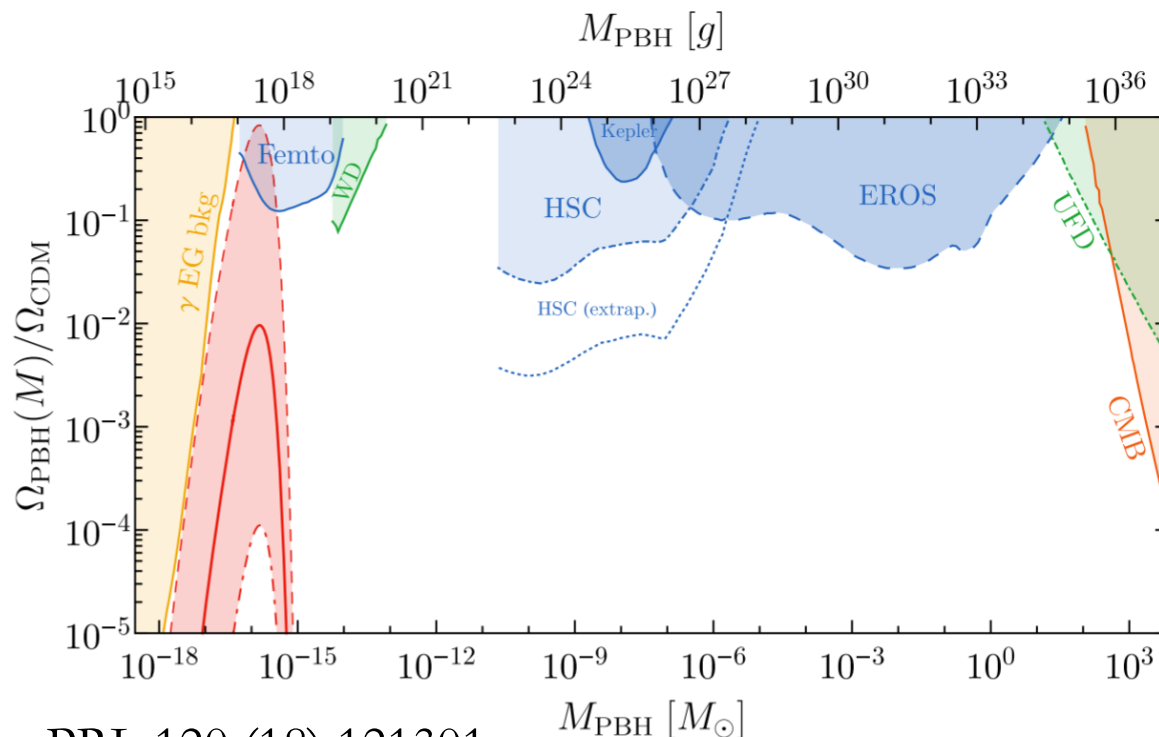
Ezquiaga, Garcia-Bellido, Morales, PLB 776 (18) 345

Spectator Higgs model

- Higgs field is not responsible for inflation, but its fluctuation generate large power

$$V(h_c) = -\frac{1}{4}\lambda h_c^4$$

RG running,
coupling
becomes negative
Higgs instability



Espinosa, Racco, Riotto, PRL 120 (18) 121301

Passaglia, Hu, Motohashi, PRD 101 (20) 123523

Nonminimal coupling and $R+R^2$ Gundhi & Steinwachs, 2011.09485

Horndeski Theory

- The most general scalar-tensor theory with 2nd order of EOMs

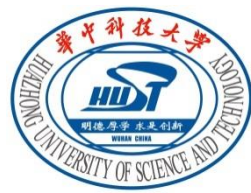
$$L_H = L_2 + L_3 + L_4 + L_5$$

$$L_2 = K(\phi, X), \quad X = -\frac{1}{2}\nabla_\mu\phi\nabla^\mu\phi$$

$$L_3 = -G_3(\phi, X)\square\phi$$

$$L_4 = G_4(\phi, X)R + G_{4,X} [(\square\phi)^2 - (\nabla_\mu\nabla_\nu\phi)(\nabla^\mu\nabla^\nu\phi)]$$

$$L_5 = G_5(\phi, X)G_{\mu\nu}\nabla^\mu\nabla^\nu\phi - \frac{1}{6}G_{5,X} [(\square\phi)^3 - 3(\square\phi)(\nabla_\mu\nabla_\nu\phi)(\nabla^\mu\nabla^\nu\phi) + 2(\nabla^\mu\nabla_\alpha\phi)(\nabla^\alpha\nabla_\beta\phi)(\nabla^\beta\nabla_\mu\phi)]$$



Horndeski Theory: Special cases

■ Non-minimally coupling

$$L_4 = G_4(\phi, X)R + G_{4,X} [(\square\phi)^2 - (\nabla_\mu\nabla_\nu\phi)(\nabla^\mu\nabla^\nu\phi)]$$

$$G_4(\phi, X) = f(\phi) \quad \text{Non-minimal coupling } f(\phi)R$$

■ Non-minimally derivative coupling

$$G_5(\phi, X)G_{\mu\nu}\nabla^\mu\nabla^\nu\phi \longrightarrow G^{\mu\nu}\partial_\mu\phi\partial_\nu\phi \quad \begin{array}{l} \text{Non-minimal coupling} \\ \text{Gauss-Bonnet coupling} \\ \text{Derivative coupling} \end{array}$$
$$G_5(\phi, X) = \phi$$

■ New Higgs inflation

$$S = \frac{1}{2} \int d^4x \sqrt{-g} \left[M_{pl}^2 R - g^{\mu\nu} \partial_\mu\phi\partial_\nu\phi + \frac{1}{M^2} G^{\mu\nu} \partial_\mu\phi\partial_\nu\phi - 2V(\phi) \right]$$

k/G inflation

■ Non-canonical field

$$S = \frac{1}{2} \int d^4x \sqrt{-g} \left[M_{pl}^2 R - g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi + \frac{f(\phi)}{M^2} G^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - 2V(\phi) \right]$$

$$f(\phi) = \frac{d}{\sqrt{(\frac{\phi - \phi_r}{c})^2 + 1}} \quad V(\phi) = \lambda \phi^{2/5}$$

Fu, Wu & Yu, PRD 100 (19) 063532; PRD 101 (20) 023529

Parameter needs
to be fine tuned
at least to six
decimal digits

■ G inflation

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2} R + K(\phi, X) - G_3(\phi, X) \square \phi \right]$$

$$X = -g_{\mu\nu} \nabla^\mu \phi \nabla^\nu \phi / 2$$

Lin, Gao & Gong et al., PRD 101 (20) 103515

k/G inflation

■ G inflation

Special case: $G_{3\phi} = dG_3(\phi)/d\phi$

$$K(\phi, X) = X - V(\phi)$$

■ k inflation

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2}R + X + G(\phi)X - V(\phi) \right]$$

$$\mathcal{P}_\zeta = \frac{H^2}{8\pi^2\epsilon} (1 + G) \quad G \text{ used to generate a peak}$$

At large scales, G is negligible, we recover standard SR result

At small scales, G is very big, the power spectrum is enhanced

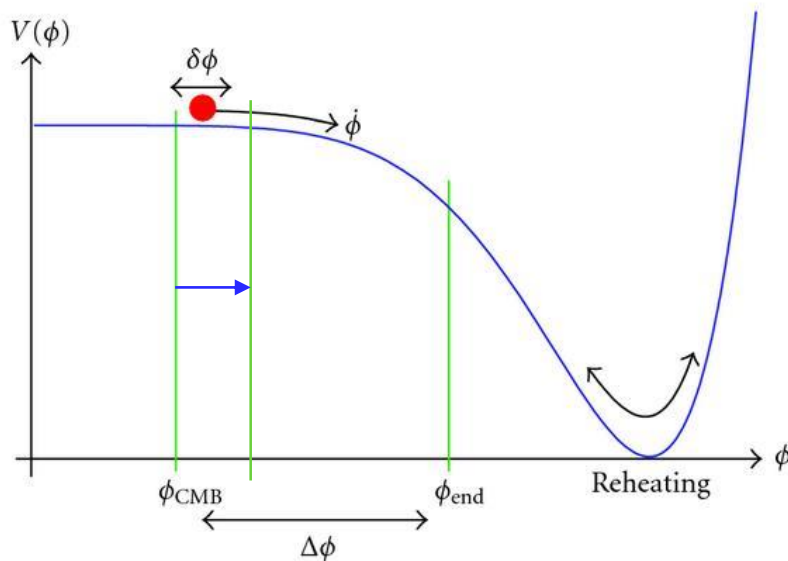
k/G inflation

- Number of e-folds around the peak

$$\Delta N = \int_{\phi_r - \Delta\phi}^{\phi_r + \Delta\phi} \frac{H}{\dot{\phi}} d\phi \simeq - \int_{\phi_r - \Delta\phi}^{\phi_r + \Delta\phi} \frac{V(1+G)}{V_\phi} d\phi$$

Peak width should be small

- The limit on the potential



$$\Delta N \sim 20$$

$$N_* \sim 60 \rightarrow N_* \sim 40$$

The possible potentials

- The power-law potential $V(\phi) = \lambda\phi^n$

$$n_s = 1 - \frac{n+2}{2N}$$

$$r = \frac{4n}{N}$$

Higgs potential $n = 4, N_* = 40$

$$n_s = 0.925$$

$$r = 0.4$$

$$n = 1/3, n_s = 0.971, r = 0.033$$

$$n = 2/3, n_s = 0.967, r = 0.067$$

k/G inflation

■ Examples for peak functions

Peak function $G_a(\phi) = \frac{d}{1 + \left| \frac{\phi - \phi_r}{c} \right|}$

Brans-Dicke theory: $\omega(\phi) = 1/\phi$

Around the peak $|\phi - \phi_r| \ll c, G_a(\phi) \sim d$

To get the enhancement, $d \sim 10^8$

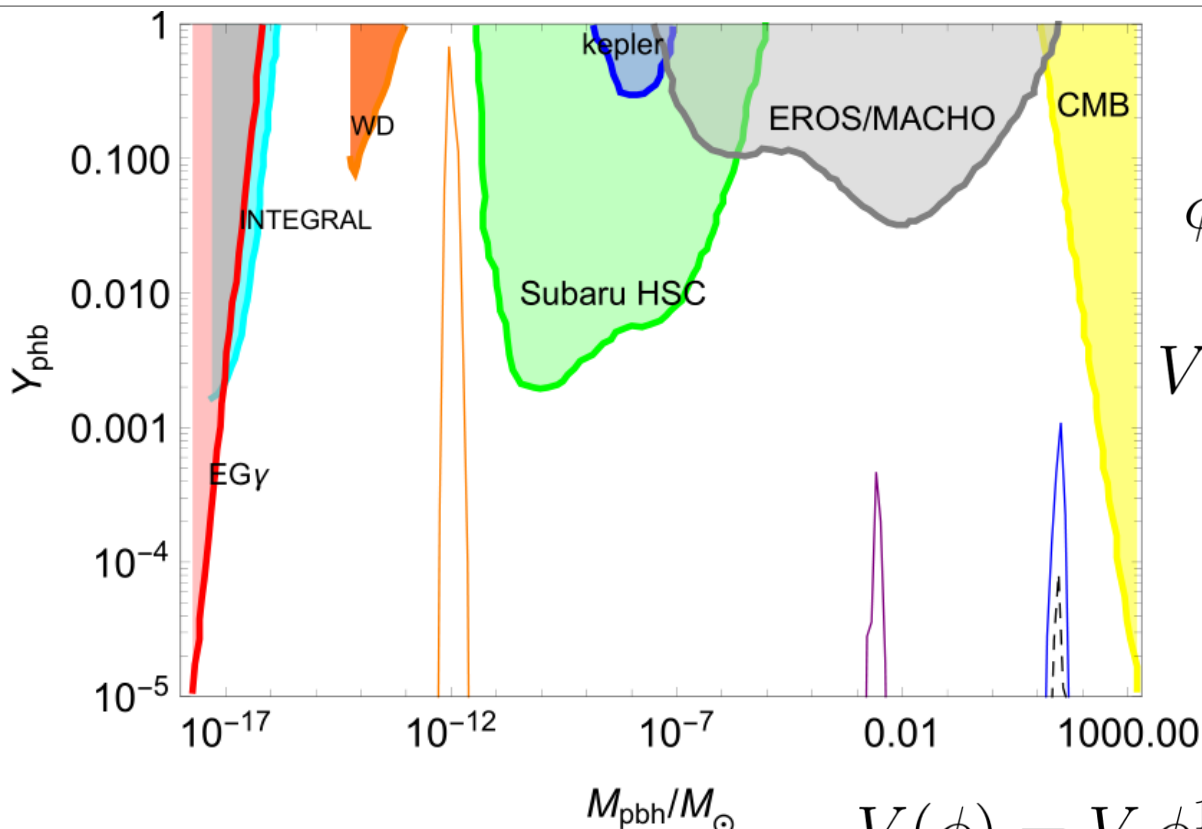
To ensure enhancement at small scales, ϕ_r should away from ϕ_*

Away from the peak $|\phi - \phi_r| \gg c, G_a(\phi) \sim dc/|\phi - \phi_r|$
 $\sim O(0.01) \quad \sim O(1)$

Small peak width $c \sim 10^{-10}$ at most

PBH from k/G inflation

Sets	ϕ_r	c	n_s	$k_{\text{peak}}/\text{Mpc}^{-1}$	$P_{\zeta(\text{peak})}$	$M_{\text{pbh}}^{\text{peak}}/M_{\odot}$	$Y_{\text{PBH}}^{\text{peak}}$	f_c/Hz
A	4.5	9.54×10^{-11}	0.9736	2.86×10^5	1.66×10^{-2}	28.9	7.7×10^{-5}	4.43×10^{-10}
B	4.5	9.568×10^{-11}	0.9737	2.7×10^5	1.86×10^{-2}	32.5	0.001	4.18×10^{-10}
C	4.1	1.05×10^{-10}	0.969	3×10^7	1.49×10^{-2}	0.0026	4.7×10^{-4}	4.6×10^{-8}
D	2.97	1.472×10^{-10}	0.967	1.63×10^{12}	1.32×10^{-2}	9×10^{-13}	0.73	2.5×10^{-3}



$$\phi_* = 5.21$$

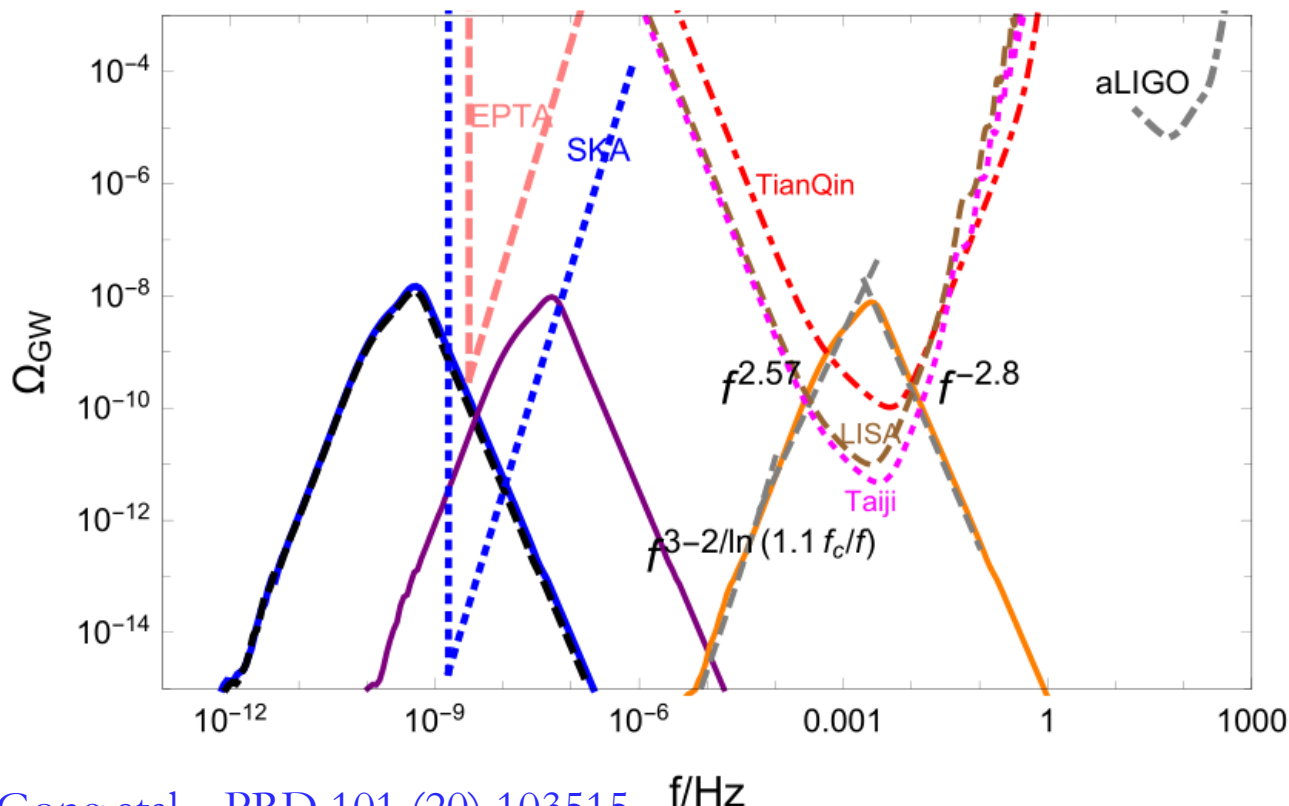
$$V(\phi) = V_0 \phi^{2/5}$$

Gao, 2102.07369

$$V(\phi) = V_0 \phi^{1/3}$$

SIGWs from k/G inflation

Sets	ϕ_r	c	n_s	$k_{\text{peak}}/\text{Mpc}^{-1}$	$P_{\zeta(\text{peak})}$	$M_{\text{pbh}}^{\text{peak}}/M_{\odot}$	$Y_{\text{PBH}}^{\text{peak}}$	f_c/Hz
A	4.5	9.54×10^{-11}	0.9736	2.86×10^5	1.66×10^{-2}	28.9	7.7×10^{-5}	4.43×10^{-10}
B	4.5	9.568×10^{-11}	0.9737	2.7×10^5	1.86×10^{-2}	32.5	0.001	4.18×10^{-10}
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D	2.97	1.472×10^{-10}	0.967	1.63×10^{12}	1.32×10^{-2}	9×10^{-13}	0.73	2.5×10^{-3}



The new mechanism

■ Combine slow roll with the peak

To generate peak

$$L = [1 + G_a(\phi)]X - U(\phi)$$

Transform non-canonical field to canonical field

$$L = [1 + G(\varphi)]X - V(\varphi)$$

$$G = G_a + f(\varphi)$$

Slow roll $L = f(\varphi)X - V(\varphi) \quad V(\varphi) = \lambda\varphi^4, \quad f(\varphi) = f_0\varphi^{22}$

$$d\phi = \sqrt{f(\varphi)}d\varphi, \quad U(\phi) = V[\varphi(\phi)]$$

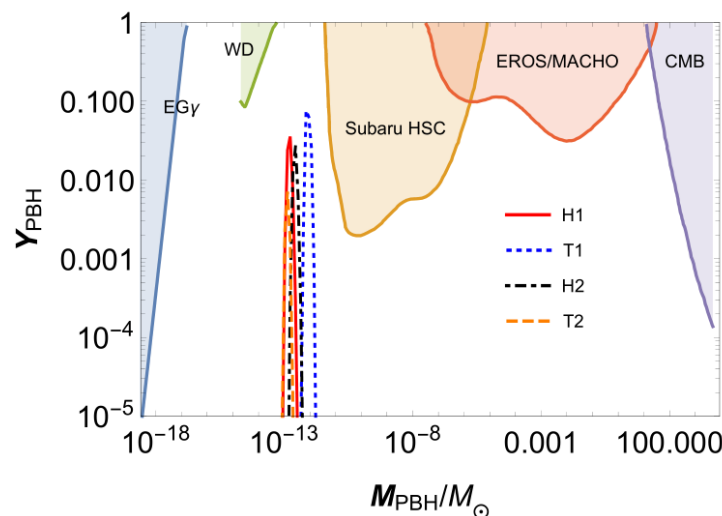
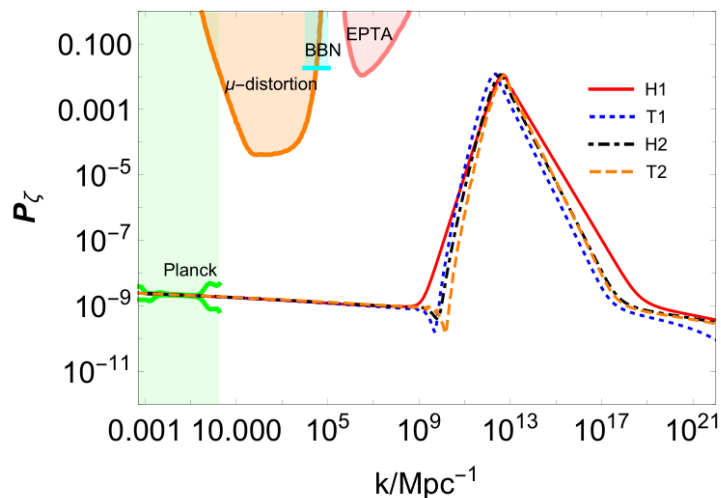
$$L = X - U(\phi) \quad U(\phi) = \lambda\phi^{1/3}$$

Higgs k/G inflation

Model	d	c	ϕ_p	ϕ_*	λ/V_0	f_0	N	n_s	r	$k_{\text{peak}}/\text{Mpc}^{-1}$
H1	1.05×10^{10}	2.04×10^{-10}	1.344	1.40	1.24×10^{-9}	1	62.3	0.9681	0.0383	4.66×10^{12}
T1	4.72×10^9	8.89×10^{-11}	0.451	0.81	1.68×10^{-9}	36	55.6	0.9686	0.0369	2.29×10^{12}
H2	7.13×10^9	1.94×10^{-10}	1.750	1.88	6.40×10^{-10}	1	64.2	0.9694	0.0641	3.67×10^{12}
T2	8.90×10^9	4.75×10^{-11}	0.835	1.35	2.95×10^{-9}	36	63.4	0.9704	0.0597	5.24×10^{12}

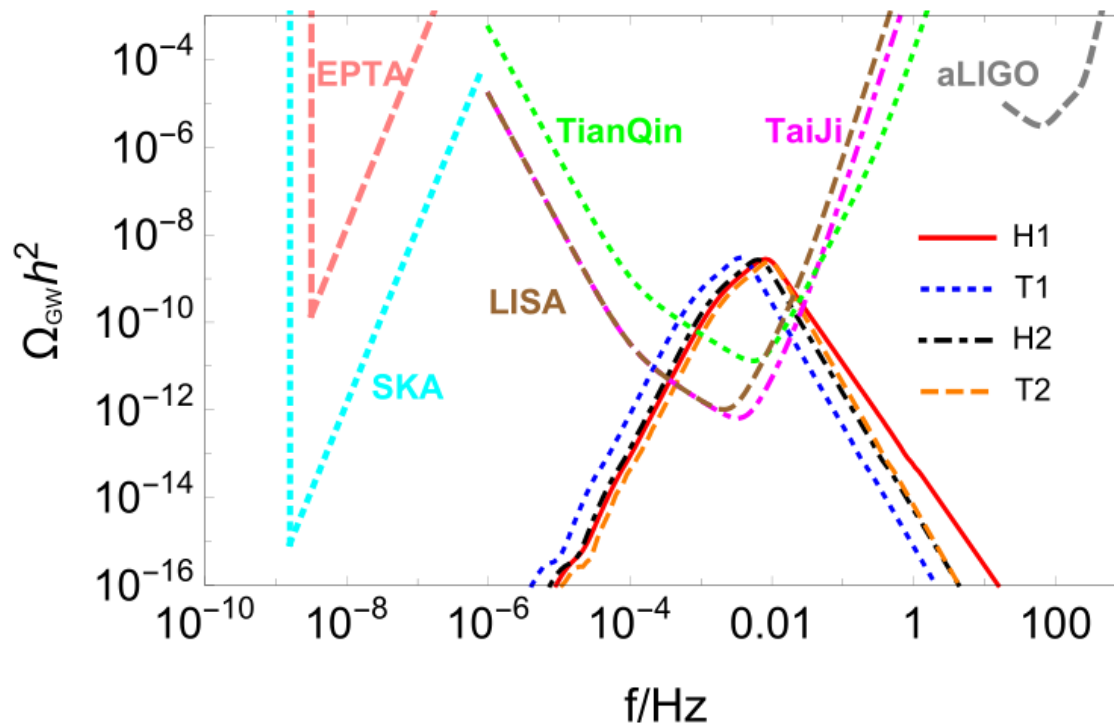
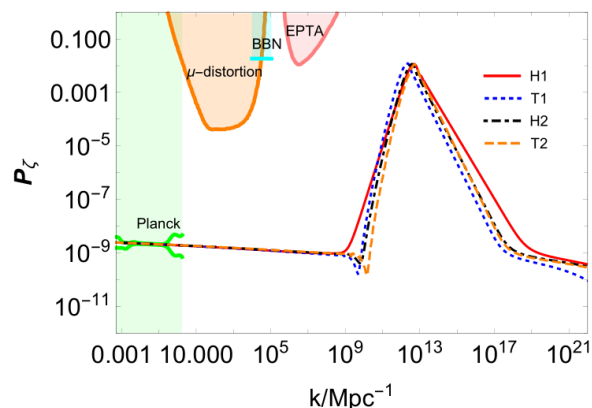
Model	$P_{\zeta(\text{peak})}$	$M_{\text{peak}}/M_{\odot}$	$Y_{\text{PBH}}^{\text{peak}}$	f_c/Hz
H1	1.16×10^{-2}	1.70×10^{-13}	3.57×10^{-2}	8.11×10^{-3}
T1	1.21×10^{-2}	7.05×10^{-13}	7.64×10^{-2}	3.54×10^{-3}
H2	1.15×10^{-2}	2.73×10^{-13}	2.64×10^{-2}	6.40×10^{-3}
T2	1.10×10^{-2}	1.34×10^{-13}	7.12×10^{-3}	9.13×10^{-3}

Yi, Gong, Wang,
Zhu,
2007.09957



SIGWs from Higgs field

■ Peak (broken power law form)



Yi, Gong, Wang, Zhu, 2007.09957

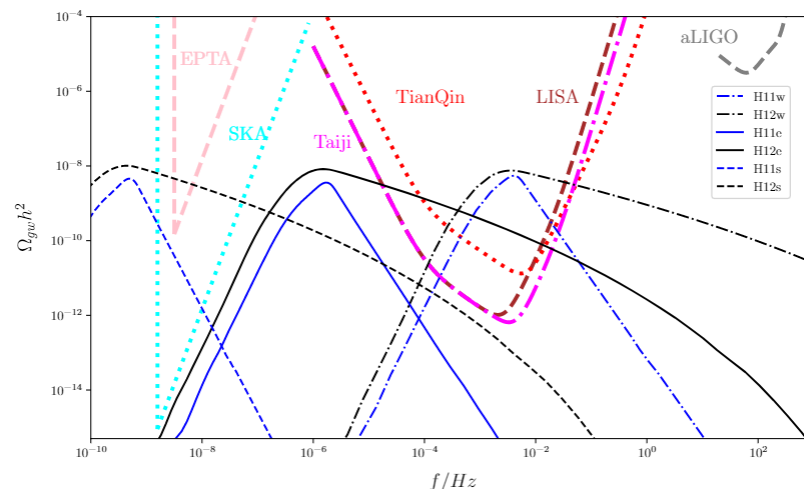
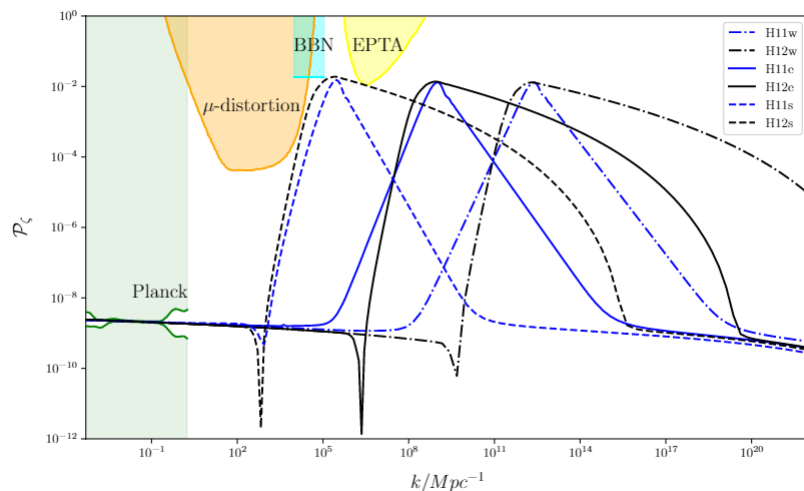
Broad Spectrum

■ Non-canonical kinetic

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2} R + X + G(\phi) X - V(\phi) \right]$$

$$G = G_a + f(\phi) \quad V(\phi) = \lambda \phi^4 / 4$$

$$G_a(\phi) = \frac{h}{1 + (|\phi - \phi_p|/w)^q} \quad q = 5/4 \quad f(\phi) = \phi^{22}$$



Non-Gaussianity

■ Bispectrum

$$\left\langle \hat{\zeta}_{\mathbf{k}_1} \hat{\zeta}_{\mathbf{k}_2} \hat{\zeta}_{\mathbf{k}_3} \right\rangle = (2\pi)^3 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B_\zeta(k_1, k_2, k_3)$$

$$f_{\text{NL}}(k_1, k_2, k_3) = \frac{5}{6} \frac{B_\zeta(k_1, k_2, k_3)}{P_\zeta(k_1)P_\zeta(k_2) + P_\zeta(k_2)P_\zeta(k_3) + P_\zeta(k_3)P_\zeta(k_1)}$$

■ PBH

$$\mathcal{J} = \frac{1}{6\sigma_R^3} \int \frac{d^3k_1}{(2\pi)^3} \int \frac{d^3k_2}{(2\pi)^3} \int \frac{d^3k_3}{(2\pi)^3} W(k_1 R) W(k_2 R) W(k_3 R) \left\langle \hat{\zeta}_{\mathbf{k}_1} \hat{\zeta}_{\mathbf{k}_2} \hat{\zeta}_{\mathbf{k}_3} \right\rangle$$

$$\mathcal{J}_{\text{peak}} = \frac{3}{20\pi} f_{\text{NL}}(k_{\text{peak}}, k_{\text{peak}}, k_{\text{peak}}) \sqrt{\Delta_\zeta^2(k_{\text{peak}})}$$

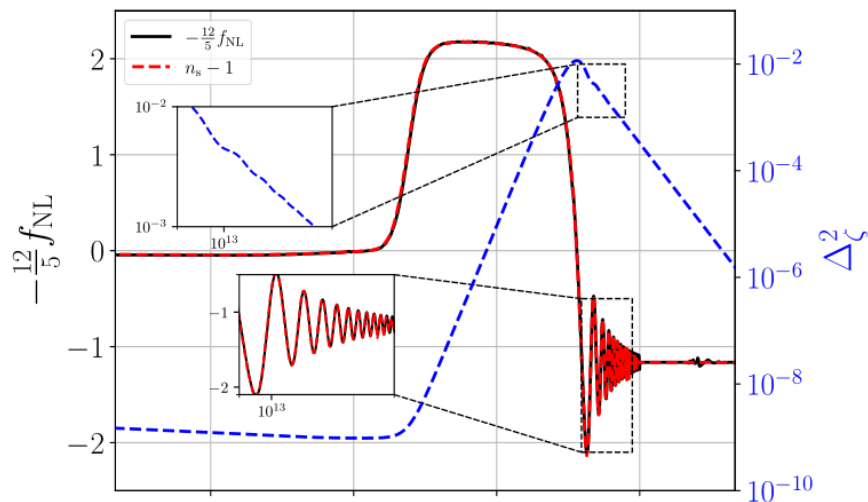
R. Saito, J. Yokoyama and R. Nagata, JCAP 06 (2008) 024

■ SIGWs $f_{\text{NL}}^2 \Delta_\zeta^2 \gtrsim 1$

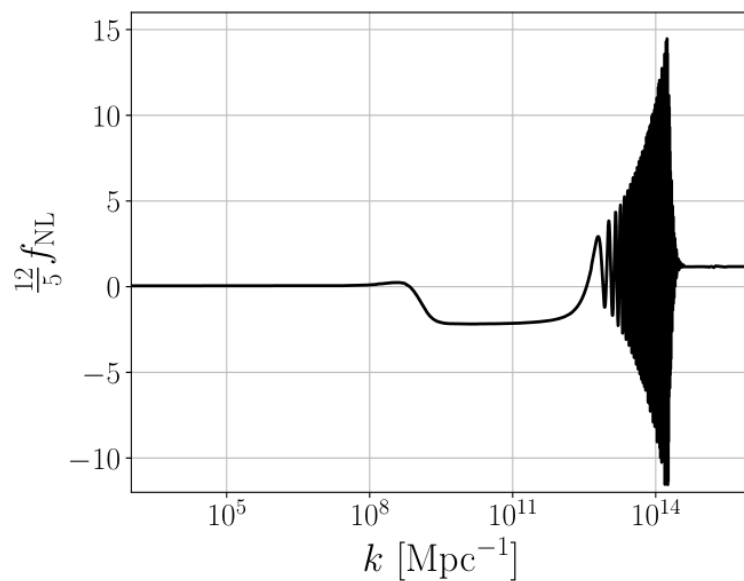
R.-G. Cai, S. Pi and M. Sasaki, PRL 122 (2019) 201101

Non-Gaussianity in k/G inflation

Squeezed limit

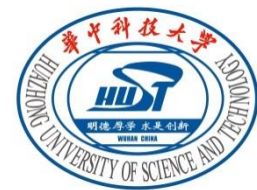


Equilateral



Conclusion

- Higgs field drives inflation, explains DM in the form of PBHs
- The mechanism works for more general scalar fields
- Different types of spectrum are also possible
- The observations of PBH and SIGWs can be used to probe early universe



Thank You