







Induced Current, Weyl Anomaly & Holography for Boundary Conformal Field Theory (BCFT)

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Outline

- 1. Induced Current as Exact Universal Behaviour of BCFT
- 2. Induced Current from AdS/BCFT
- 3. Application to 6d: Weyl anomaly from Induced String Current.
- Summary and Discussions

Anomalies, Magnetic Casimir Effect in Boundary CFT

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Novel boundary effects

A motivation of our work is to study novel effect of boundary CFT. Casimir effect arises from energetic response of the vacuum to the presence of boundary.

In this talk, I want to talk about a new kind of response of the vacuum to the boundary:

$$\vec{J} = c \vec{h} \cdot \vec{B}$$

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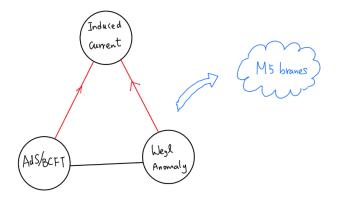
In this talk, I want to talk about a new kind of response of the vacuum to the boundary:

$$\vec{J}_{x} \qquad \vec{J} = c \quad \vec{h}_{x} \vec{B}$$

 This can be derived from exact analysis of BCFT (section 1) or AdS/BCFT (section 2).

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In section 3, we will apply it to boundary M5-branes system and learn something about the Weyl anomaly in 6d.



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1.1.1. Casmir effect in BCFT

In general, for a *d*-dimensional BQFT, vev of renormalized stress tensor has the asymptotic behaviour near boundary:

$$\langle T_{ij} \rangle = x^{-d} T_{ij}^{(d)} ... + x^{-1} T_{ij}^{(1)} + \cdots, \quad x \sim 0,$$

x is proper distance from boundary, and

$$T_{ij}^{(d)} = \alpha_0 h_{ij}, \qquad T_{ij}^{(d-1)} = 2\alpha_1 \bar{k}_{ij},$$

$$T_{ij}^{(d-2)} = \frac{-4\alpha_1}{d-1} n_{(i} h'_{j)} \nabla_l k - \frac{4\alpha_1}{d-2} n_{(i} h'_{j)} n^p R_{lp} + \dots + t_{ij}$$

$$t_{ij} := \lceil \beta_1 C_{ikjl} n^k n^l + \beta_2 \mathcal{R}_{ij} + \beta_3 k k_{ij} + \beta_4 k'_i k_{ij} \rceil,$$

where n_i , h_{ij} and \overline{k}_{ij} are respectively the normal vector, induced metric and the traceless part of extrinsic curvature of the boundary P.

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where n_i , h_{ij} and \overline{k}_{ij} are respectively the normal vector, induced metric and the traceless part of extrinsic curvature of the boundary P.

 The Casimir coefficient (α₀, α₁, β_i) fixes the shape dependence of the leading Casimir effects of BCFT.

1.1.2. Casimir effects from Weyl Anomaly

Boundary Weyl anomaly Weyl anomaly

$$\mathcal{A} := \partial_{\sigma} W[e^{2\sigma}g_{ij}]|_{\sigma=0} = \int_{M} \langle T_{i}^{i} \rangle,$$

where

$$\langle T_i^i \rangle = \langle T_i^i \rangle_M + \delta(\mathbf{x}_\perp) \langle T_a^a \rangle_P.$$

- Weyl anomaly are classified in terms of curvature invariants.
 3d: (Tⁱ_i) = δ(x)[b₁R + b₂Trk²]
 4d: ...
- Bulk central charges c do not depend on BC. Boundary central charges b_i depend on BC in general.

<ロト < 団ト < 団ト < ヨト < ヨト ミ のの Chong-Sun Chu National Tsing-Hua University and NCTS Theorem: Consider BQFT, the variation of the Weyl anomaly under an arbitrary variaion of the metric can be measured by the 1-point function of the renormalized stress tensor (Chu, Miao 17, 18) "Integrability condition":

$$(\delta \mathcal{A})_{\partial M} = \left(rac{1}{2}\int_{x\geq\epsilon}\sqrt{g}\,T^{ij}\delta g_{ij}
ight)_{\log(1/\epsilon)}$$

where $(\delta A)_{\partial M}$ is the boundary terms in the variations of Weyl anomaly and T^{ij} is the renormalized bulk stress tensor.

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where $(\delta A)_{\partial M}$ is the boundary terms in the variations of Weyl anomaly and T^{ij} is the renormalized bulk stress tensor.

Note that the right hand side must give an exact variation, this imposes strong constraints on the possible form of the stress tensor near the boundary.

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Corollary: The energy momentum tensor $T_{\mu\nu}$ of BCFT has universal behaviour near the boundary. (Chu, Miao 17, 18)

"universal" means the Casimir coefficients does not need to be computed case by case. But they have specific relations in terms of the boundary central charges of the theory.

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E.g. 3d BCFT, Weyl anomaly has only boundary contributions

$$\begin{split} \mathcal{A} &= \int_{\partial M} \sqrt{h} (b_1 \mathcal{R} + b_2 \mathrm{Tr} \bar{k}^2), \\ LHS &= (\delta \mathcal{A})_{\partial M} = b_2 \int_{\partial M} \sqrt{h} \Big[(\frac{\mathrm{Tr} \bar{k}^2}{2} h^{ab} - 2 \bar{k}_c^a k^{cb}) \delta h_{ab} + 2 \bar{k}^{ab} \delta k_{ab} \Big]. \end{split}$$

For RHS, sub. $T_{\mu\nu}$, int. over x and pick up the log divergent term

$$RHS = - \alpha_1 \int_P \sqrt{h} [(\frac{\mathrm{Tr}\bar{k}^2}{2}h^{ab} - 2\bar{k}_c^a k^{cb})\delta h_{ab} + 2\bar{k}^{ab}\delta k_{ab}] + \int_P \sqrt{h} [(\frac{\beta_3}{2} - \alpha_1)k\bar{k}^{ab}\delta h_{ab} + \frac{\beta_4}{2} [k_c^a k^{cb}]\delta h_{ab}].$$

We obtain
$$\alpha_1 = -b_2$$
, $\beta_3 = -2b_2$, $\beta_4 = 0$.

4d BCFT. Similar analysis and results for 4d.

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- It is remarkable that the Casimir coefficients are completely determined by the boundary central charges.
- The relations between them are universal and independent of BC and theory.

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1.2.1. Chiral Anomaly and Transport

Two famous Anomaly induced transport of charges:

CME: chiral magnetic effect

(Vilenkin 80; Giovannini Shaposhnikov 98; Froehlich etal 98)

$$\mathbf{J}_{V} = \sigma_{(\mathcal{B})V} \mathbf{B} \quad \mathbf{J}_{A} = \sigma_{(\mathcal{B})A} \mathbf{B},$$

where the chiral magnetic conductivities are

$$\sigma_{(\mathcal{B})V} = \frac{e\mu_A}{2\pi^2}, \quad \sigma_{(\mathcal{B})A} = \frac{e\mu_V}{2\pi^2}$$

 CVE: chiral vortical effect (Kharzeev, Zhitnitsky 07; Erfmemger etal 09; Son etal 09; Landsteiner etal 11)

$$\mathbf{J}_{V} = \sigma_{(\mathcal{V})V}\omega, \quad \mathbf{J}_{A} = \sigma_{(\mathcal{V})A}\omega,$$

where the chiral vortical conductivities are

$$\sigma_{(\mathcal{V})\mathcal{V}} = \frac{\mu_{\mathcal{V}}\mu_{\mathcal{A}}}{\pi^2}, \quad \sigma_{(\mathcal{V})\mathcal{A}} = \frac{\mu_{\mathcal{V}}^2 + \mu_{\mathcal{A}}^2}{2\pi^2} + \frac{T^2}{6}$$

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Note that these anomalous transport occurs only in a material system where the chemical potentials are non-vanishing.

Q. In the presence of boundary, can the phenomena of anomalous transport occur in vacuum like Casimir effect? if so, how is it possible?

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1.2.2. Weyl Anomaly and induced current

Just as energy momentum tensor, the renormalized current also admits an asymptotic expansion near the boundary:

$$\langle J_i
angle = x^{-3} J_i^{(3)} + x^{-2} J_i^{(2)} + x^{-1} J_i^{(1)}, \quad x \sim 0,$$

where x is the proper distance from the boundary and $J_i^{(n)}$ depend only on the background geometry and the background vector field strength.

Imposing current conservation

$$\nabla_i \langle J^i \rangle = 0,$$

we obtain the gauge invariant solutions

$$J_{\mu}^{(3)} = 0, \qquad J_{\mu}^{(2)} = 0,$$

$$J_{\mu}^{(1)} = \alpha_1 F_{\mu\nu} n^{\nu} + \alpha_2 \mathcal{D}_{\mu} k + \alpha_3 \mathcal{D}_{\nu} k_{\mu}^{\nu} + \alpha_4 \star F_{\mu\nu} n^{\nu}$$

Under an arbitrary of A_{μ} , one can similarly establish the integrability condition

$$(\delta \mathcal{A})_{\partial M} = \Big(\int_{\mathcal{M}} \sqrt{g} J^{\mu} \delta A_{\mu}\Big)_{\log rac{1}{\epsilon}}$$

Using it, the current coefficients are determined completely in terms of central charges.

• Consider background U(1) gauge field, e.g. QED

$${\cal A}=\int_{\cal M}\sqrt{g}[b_1F_{\mu
u}F^{\mu
u}+{
m metric} \; {
m part}], \quad b_1=-eta(e)/(2e^3), \; {
m centeral} \; {
m charge}$$

This implies that $(\delta A)_{\partial M} = -4b_1 \int_{\partial M} \sqrt{h} F^b{}_n \delta a_b$. Matching it with the RHS of the integrability condition, we obtain

$$\alpha_1 = 4b_1, \quad \alpha_2 = \alpha_3 = \alpha_4 = 0.$$

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Explicitly, we obtain the induced current near the boundary of a BQFT:

$$\mathbf{J} = \frac{e^2 c}{\hbar} \frac{4 b_1 \mathbf{n} \times \mathbf{B}}{x}, \quad x \sim 0$$

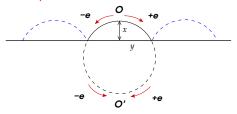
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Q. What is the physics of this current?

• The current is a result of charge separation due to vacuum fluctuation in the presence of external *B*-field.

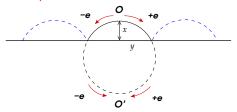


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- Q. What is the physics of this current?
 - The current is a result of charge separation due to vacuum fluctuation in the presence of external *B*-field.



 Equivalently, it can also be seen as arising from the magnetization of the vacuum due to presence of boundary:
 J = ∇ × M.





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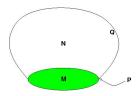
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2.1. Statement of AdS/BCFT

- Consider d dimensional CFT defined on R^{1,d-1}. There is a SO(2, d) conformal symmetry. This is realized in holography as isometries of the bulk of AdS_{d+1} space
- When a boundary is introduced, the full conformal symmetry is reduced at the boundary. Takayanagi proposed to extend that the gravity dual is given by gravity in a d + 1 dimensional manifold N whose boundary is given by M and Q. (Takayanagi 11)



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The bulk gravity action is given by

$$I = \int_{N} \sqrt{G}(R - 2\Lambda) + 2 \int_{M} \sqrt{g}K + 2 \int_{Q} \sqrt{h}(K - T) + 2 \int_{P} \sqrt{\sigma}\theta,$$

T measures the boundary degrees of freedom (g-function). differential equation for Q.

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The central issue is the determination of the location of Q in the bulk. Takayanagi proposed to impose Neumann boundary condition on Q to fix its position:

EOM of Q:
$$K_{\alpha\beta} - (K - T)h_{\alpha\beta} = 0,$$
 (*1)

This gives a second order DE.

However since Q is of co-dimension one, the location of Q is determined by a single embedding function:

$$z = z(x^i)$$
, here $x^i =$ coordinates of M

The embedding equation

$$K_{\alpha\beta} - (K - T)h_{\alpha\beta} = 0,$$
 (*1)

generally imposes too many constraints and (*1) does not has solution for general shape P of BCFT.

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Alternatively, we proposed to impose on Q a mixed BC and this leads to:

$$(1-d)K + dT = 0 \tag{*2}$$

(Chu, Guo, Miao 17; Chu, Miao 17)

- (*2) is natural as there is only one embedding function for Q and we expect one condition for it.
- This is a consistent proposal and describes the duals for a wide class of BCFTs, with the original proposal of Takayanagi as a special case.

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Non FG (Fefferman-Graham) expansion

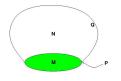
In the standard AdS/CFT, FG expansion of the bulk metric is assumed:

$$ds^2 = rac{dz^2 + g_{ij}dx^i dx^j}{z^2}, \quad g_{ij} = g_{ij}^{(0)} + z^2 g_{ij}^{(1)} + \cdots.$$

 $g_{ij}^{(0)}$ is the metric of BCFT on *M*. $g_{ij}^{(1)}$ is fixed by Einstein equation:

$$g_{ij}^{(1)} = -rac{1}{d-2}(R_{ij}^{(0)}-rac{R^{(0)}}{2(d-1)}g_{ij}^{(0)}).$$

However in the case of AdS/BCFT, the dual manifold N has discontinuity at the corner P where Q and M meet.



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- We have to give up the assumption that the dual space has a metric that can be FG expanded in small z near M. Solving Einstein equation is hard!
- Convenient to use the Gauss normal coordinates. The metric g⁽⁰⁾_{ij} of the BCFT takes the form

$$ds_0^2 = dx^2 + (\sigma_{ab} + 2xk_{ab} + x^2q_{ab} + \cdots)dy^a dy^b,$$

where *P* is located at x = 0.

▶ We found a new systematic construction of non-FG expanded metric by employing k_{ab}, q_{ab} etc as expansion parameter, but keeping both the z and x dependence as exact.

In this way, we are able to construct a perturbative solution to the bulk Einstein equation: (Chu, Miao 2017)

$$ds^{2} = \frac{dz^{2} + dx^{2} + \left(\delta_{ab} - 2x\bar{k}_{ab}f\left(\frac{z}{x}\right)\right)dy^{a}dy^{b}}{z^{2}} + \cdots$$

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2.2 Application: Induced current near boundary

 To investigate the renormalized current in holographic models of BCFT, we add a Maxwell action:

$$I = \int_{N} \sqrt{G} [R - 2\Lambda - \frac{1}{4} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}] + 2 \int_{Q} \sqrt{\gamma} [K - T]$$

 Consider 4d and planar boundary, one can solve for the bulk Maxwell equation and BC, and obtain

$$\mathcal{A}_{a} = F_{xa}\sqrt{x^{2} + z^{2}}, \qquad (2)$$

where F_{xa} is the field strength at the boundary.

The holographic current is

$$\langle J^{a} \rangle = \lim_{z \to 0} \frac{\delta I}{\delta A_{a}} = \lim_{z \to 0} \sqrt{G} \mathcal{F}^{za} = -\frac{F_{ax}}{x} + \cdots$$

Same as before!

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- 3. Application to 6d: Weyl anomaly from Induced String Current.

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3.1 Boundary string current from holography

Consider a charged particle moving on the worldline C: x^μ = x^μ(τ). The motion gives a current and a coupling to gauge field:

$$J^{\mu}(x) = \delta^{(d-1)}(x - x(\tau)) rac{dx^{\mu}(\tau)}{d au}$$

 $\int_{M} J_{\mu} A^{\mu} = \int_{C} A_{\mu} dx^{\mu}$

Similarly, movement of strings gives the higher 2-form current and a coupling to the 2-form potential $B_{\mu\nu}$:

$$egin{aligned} J_{\mu
u} &= \delta^{(d-2)}(x-x(\sigma, au))\epsilon^{lphaeta}rac{\partial x^{\mu}}{\partial\sigma^{lpha}}rac{\partial x^{
u}}{\partial\sigma^{eta}}.\ &\int_{M}J_{\mu
u}B^{\mu
u} &= \int_{\Sigma}B_{\mu
u}dx^{\mu}dx^{n}. \end{aligned}$$

Q. Any implication of knowing the existence of such a coupling?

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Consider a BCFT in 6d and denote the Weyl anomaly as A. The gravitational part is well understood. (Deser, Schwimmer)

$$\langle T^{\mu}_{\mu} \rangle = \frac{1}{(4\pi)^{d/2}} \left(\sum_{j} c_{dj} I^{(d)}_{j} - (-1)^{\frac{d}{2}} a_{d} E_{d} \right).$$

- Q. What about the contribution from background gauge field?
- Claim: One can similarly establish the relation

$$(\delta \mathcal{A})_{\partial M} = ig(\int_{M_\epsilon} J_{\mu
u} \delta B^{\mu
u} ig)_{\log 1/\epsilon}.$$

Thus, knowing the current, or vice versa, would allow us to learn something about the anomaly structure of the 6d CFT.

Consider a 6d BCFT dual to the the bulk action with an H-field

$$I = \int d^7 x \sqrt{G} (R - 2\Lambda - \frac{1}{12} H_{\mu\nu\lambda}^2)$$

Using the BCFT holography, one finds a string current parallel to the boundary when a H-field strength is turned on

$$J_{ab} = b_1 \frac{H_{abx}}{x}.$$

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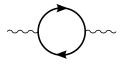
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3.2. Prediction for the Weyl anomaly in 6d

► The relation $(\delta A)_{\partial M} = (\int_{M_{\epsilon}} J_{\mu\nu} \delta B^{\mu\nu})_{\log 1/\epsilon}$ predicts the Weyl anomaly in the 6d CFT:

$$\mathcal{A} = \int_{M} \frac{b_1}{12} H^2$$

 It is interesting to understand how matter fields would couple to the B_{μν} field (covariant derivatives?) and give rises to the Weyl anomaly.



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String loop covariant derivatives

- As B_{µν} is coupled to a worldsheet, the natural way to construct a covariant derivative is by considering a string functional Ψ(C).
- Define loop derivative

$$\partial_{\mu\nu}\Psi := rac{\delta\Psi(C)}{\delta\sigma^{\mu
u}} := \lim_{\Delta\sigma^{\mu
u} o 0} rac{\Psi(C + \delta C) - \Psi(C)}{\Delta\sigma^{\mu
u}}$$



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 A general unitary transformation that depends on the loop takes the form

$$\Psi(C) \rightarrow \Psi(C) \exp(i \int_C \alpha),$$

where $\alpha = \alpha_{\mu} dx^{\mu}$ is a 1-form.

The derivative

$$\mathcal{D}_{\mu
u}\Psi:=(\partial_{\mu
u}-iB_{\mu
u})\Psi$$

is covariant: $\mathcal{D}_{\mu\nu}(e^{i\int \alpha}\Psi) = e^{i\int \alpha} \mathcal{D}_{\mu\nu}\Psi$ since $\mathcal{B}_{\mu\nu}$ transforms as

$$B_{\mu\nu} o B_{\mu\nu} + \partial_{\mu}\alpha_{\nu} - \partial_{\nu}\alpha_{\mu}$$

It is more natural to consider a theory of self-dual string and think of the Weyl anomaly as a property of the effective action of the string partition function.

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M5-branes system

- For a system of *N* M5-branes, the gravity dual is given by $AdS_5 \times S^5$.
- Restoring the units, b_1 is given by

$$b_1 = \frac{R^5}{16\pi G_7} = \frac{N^3}{3\pi^3},$$

where $G^{(7)} = G^{(11)}/R_S^4$, $R_S = I_P(\pi N)^{1/3}$ is the 4-sphere radius and $R = 2R_S$ is the AdS_7 radius.

Therefore for a system of N M5-branes with boundary, one finds for the singlet current

$$J_{ab} = \frac{N^3}{3\pi^3} \frac{H_{abx}}{x}.$$

This results suggest that there is N^3 degrees of freedom in the interacting (2,0) theory.

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Conclusions and Discussions

- 1. We found new universal relations for near boundary behaviour of stress tensor and electric current.
- In the presence of a magnetic field, we predict a magnetization current in the vicinity of the boundary of QED vacuum. This is a kind of magnetic Casimir effect.
- 3. Based on the original work of Takayanagai, we have constructed a complete proposal of holographic BCFT.
- 3. We predict a Weyl anomaly for the M5-branes system.

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Open questions:

- What is the origin of the Weyl anomaly of M5-brane?
- What is the implicition on the partition function?
- Quantum Hall effect can be understoood in terms of NCG:

$$[x^i, x^j] = i\theta^{ij}.$$

Can we understand the magnetization of the vacuum in terms of NCG?

What about the M5-brane worldvolume?

$$[x^i, x^j, x^k] = i\theta^{ijk}?$$

Thank you!

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