

# Renormalizable Wess-Zumino Model on Bosonic-Fermionic Noncommutative Superspace

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# Bosonic Noncommutative Superspace

- Obtain bosonic noncommutative superspace from string theory, [N. Seiberg et al, [hep-th/9908142](#)].
- Construct Wess-Zumino and super Yang-Mills model on bosonic noncommutative superspace. [S. Ferrara et al, [hep-th/0002084](#), [hep-th/0307039](#)].
- Bosonic noncommutative Wess-Zumino model is renormalizable to all orders, [ H. O. Girotti et al, [hep-th/0005272](#), A. A. Bichl et al, [hep-th/0007050](#), I. L. Buchbinder et al, [hep-th/0107022](#)].

# NAC Superspace

- Obtain NAC superspace from string theory, [H. Ooguri et al, hep-th/0303063, N. Berkovits et al, hep-th/0306226].
- Construct Wess-Zumino and super Yang-Mills model on NAC superspace, [N. Seiberg, hep-th/0305248].
- New renormalization theorem for NAC Wess-Zumino model, [R. Britto et al, hep-th/0306215].
- Calculate the 1PI effective action for NAC Wess-Zumino model, [M. T. Grisaru et al, hep-th/0307099].
- Analyze renormalization of NAC Wess-Zumino model by using two global  $U(1)$  symmetry, [R. Britto et al, hep-th/0307165, A. Romagnoni, hep-th/0307209].

# BFNC Superspace

- Obtain BFNC superspace from string theory, [[J. de Boer et al, hep-th/0302078](#)].
- Investigate BFNC Wess-Zumino model, [[Y. Kobayashi et al, hep-th/0505011](#)].
- One-loop renormalizable BFNC Wess-Zumino model, [[Y. G. Miao et al, arXiv: 1403.4705](#)]
- BFNC Wess-Zumino model renormalizable to all orders, [[Y. G. Miao et al, arXiv: 1403.5046](#)]

- One-Loop Renormalizable BFNC Wess-Zumino Model

# Chiral Superfield

- $Q$  and  $D$  are defined by,

$$\begin{aligned} Q_\alpha &\equiv \frac{\partial}{\partial\theta^\alpha}, \quad \bar{Q}_{\dot{\alpha}} \equiv -\frac{\partial}{\partial\bar{\theta}^{\dot{\alpha}}} + 2i\theta^\beta\sigma^k{}_{\beta\dot{\alpha}}\frac{\partial}{\partial y^k}, \\ D_\alpha &\equiv \frac{\partial}{\partial\theta^\alpha} + 2i\sigma^k{}_{\alpha\dot{\beta}}\bar{\theta}^{\dot{\beta}}\frac{\partial}{\partial y^k}, \quad \bar{D}_{\dot{\alpha}} \equiv -\frac{\partial}{\partial\bar{\theta}^{\dot{\alpha}}}. \end{aligned}$$

- The chiral superfield  $\Phi$  and the antichiral superfields  $\Phi^+$  satisfy the following conditions, respectively,

$$\bar{D}_{\dot{\alpha}}\Phi = 0, \quad D_\alpha\Phi^+ = 0.$$

- They can be expressed by component fields as follows,

$$\begin{aligned} \Phi(y, \theta) &= A(y) + \sqrt{2}\theta^\alpha\psi_\alpha(y) + \theta^\alpha\theta_\alpha F(y), \\ \Phi^+(y, \theta, \bar{\theta}) &= A^*(y) + \sqrt{2}\bar{\theta}_{\dot{\alpha}}\bar{\psi}^{\dot{\alpha}}(y) + \bar{\theta}_{\dot{\alpha}}\bar{\theta}^{\dot{\alpha}}F^*(y) - 2i\sigma^k{}_{\alpha\dot{\beta}}\theta^\alpha\bar{\theta}^{\dot{\beta}}\partial_k A^*(y) \\ &\quad + i\sqrt{2}\sigma^k{}_{\alpha\dot{\beta}}\theta^\alpha\bar{\theta}_{\dot{\zeta}}\bar{\theta}^{\dot{\zeta}}\partial_k\bar{\psi}^{\dot{\beta}}(y) + \eta^{kl}\theta^\alpha\theta_\alpha\bar{\theta}_{\dot{\beta}}\bar{\theta}^{\dot{\beta}}\partial_k\partial_l A^*(y), \end{aligned}$$

# Wess-Zumino Model

- The action of the Wess-Zumino model is

$$\begin{aligned} S_{WZ} = & \int d^4x \left\{ \Phi^+ \Phi|_{\theta^2 \bar{\theta}^2} + \frac{m}{2} \Phi \Phi|_{\theta^2} + \frac{m}{2} \Phi^+ \Phi^+|_{\bar{\theta}^2} \right. \\ & \left. + \frac{g}{3} \Phi \Phi \Phi|_{\theta^2} + \frac{g}{3} \Phi^+ \Phi^+ \Phi^+|_{\bar{\theta}^2} \right\}, \end{aligned}$$

where  $\Phi^+ \Phi|_{\theta^2 \bar{\theta}^2}$  denotes the  $\theta^2 \bar{\theta}^2$  component of  $\Phi^+ \Phi$ , and the other terms have the similar meaning.

- The Wess-Zumino action can be transformed to a total superspace integral,

$$\begin{aligned} S_{WZ} = & \int d^8z \left\{ \Phi^+ \Phi - \frac{m}{8} \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{m}{8} \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) \right. \\ & \left. - \frac{g}{12} \Phi \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{g}{12} \Phi^+ \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) \right\}. \end{aligned}$$

# BFNC Star Product

- The BFNC  $\star$ -product can be expressed in terms of the tensor algebraic notation which is frequently used in quantum group theory,

$$\mathbf{F} \star \mathbf{G} \equiv \mu \left\{ \exp \left[ \frac{i}{2} \Lambda^{k\alpha} \left( \frac{\partial}{\partial y^k} \otimes \frac{\partial}{\partial \theta^\alpha} - \frac{\partial}{\partial \theta^\alpha} \otimes \frac{\partial}{\partial y^k} \right) \right] \triangleright (\mathbf{F} \otimes \mathbf{G}) \right\},$$

- The Taylor expansion takes the form,

$$\begin{aligned} \mathbf{F} \star \mathbf{G} = & \quad \mathbf{F}\mathbf{G} - \frac{i}{2} \Lambda^{k\alpha} (\partial_\alpha \mathbf{F}) (\partial_k \mathbf{G}) + (-1)^{|\mathbf{F}|} \frac{i}{2} \Lambda^{k\alpha} (\partial_k \mathbf{F}) (\partial_\alpha \mathbf{G}) \\ & + \frac{1}{8} \Lambda^{k\alpha} \Lambda^{l\beta} (\partial_k \partial_l \mathbf{F}) (\partial_\alpha \partial_\beta \mathbf{G}) + \frac{1}{8} \Lambda^{k\alpha} \Lambda^{l\beta} (\partial_\alpha \partial_\beta \mathbf{F}) (\partial_k \partial_l \mathbf{G}) \\ & + (-1)^{|\mathbf{F}|} \frac{1}{4} \Lambda^{k\alpha} \Lambda^{l\beta} (\partial_\beta \partial_k \mathbf{F}) (\partial_\alpha \partial_l \mathbf{G}) \\ & - \frac{i}{16} \Lambda^{k\alpha} \Lambda^{l\beta} \Lambda^{m\zeta} (\partial_\alpha \partial_l \partial_m \mathbf{F}) (\partial_\beta \partial_\zeta \partial_k \mathbf{G}) \\ & + (-1)^{|\mathbf{F}|} \frac{i}{16} \Lambda^{k\alpha} \Lambda^{l\beta} \Lambda^{m\zeta} (\partial_\alpha \partial_\beta \partial_m \mathbf{F}) (\partial_\zeta \partial_k \partial_l \mathbf{G}) \\ & - \frac{1}{64} \Lambda^{k\alpha} \Lambda^{l\beta} \Lambda^{m\zeta} \Lambda^{n\iota} (\partial_\alpha \partial_\zeta \partial_l \partial_n \mathbf{F}) (\partial_\beta \partial_\iota \partial_k \partial_m \mathbf{G}), \end{aligned}$$

where  $\partial_k \equiv \frac{\partial}{\partial y^k}$ , and  $\partial_\alpha \equiv \frac{\partial}{\partial \theta^\alpha}$ .

# BFNC $\star$ -Algebraic Relations of Coordinates

- As a simple application of the  $\star$ -product, we calculate some  $\star$ -algebraic relations of coordinates,

$$\begin{aligned}\left\{y^k, \theta^\alpha\right\}_\star &= i\Lambda^{k\alpha}, & \left[x^k, y^l\right]_\star &= -\sigma^k{}_{\alpha\dot{\beta}}\Lambda^{l\alpha}\bar{\theta}^{\dot{\beta}}, & \left[x^k, \theta^\alpha\right]_\star &= i\Lambda^{k\alpha}, \\ \left[x^k, x^l\right]_\star &= \sigma^l{}_{\alpha\dot{\beta}}\Lambda^{k\alpha}\bar{\theta}^{\dot{\beta}} - \sigma^k{}_{\alpha\dot{\beta}}\Lambda^{l\alpha}\bar{\theta}^{\dot{\beta}},\end{aligned}$$

# BFNC Wess-Zumino Model

- To analyze the effect of the BFNC superspace on the Wess-Zumino model, we replace the ordinary product by the  $\star$ -product and give the deformed action,

$$\begin{aligned} S_{\text{NC}} \equiv & \int d^4x \left\{ \Phi^+ \star \Phi|_{\theta^2 \bar{\theta}^2} + \frac{m}{2} \Phi \star \Phi|_{\theta^2} + \frac{m}{2} \Phi^+ \star \Phi^+|_{\bar{\theta}^2} \right. \\ & \left. + \frac{g}{3} \Phi \star \Phi \star \Phi|_{\theta^2} + \frac{g}{3} \Phi^+ \star \Phi^+ \star \Phi^+|_{\bar{\theta}^2} \right\}, \end{aligned}$$

- We make the transformation for the deformed action from its component form to the desired superfield form. This performance is necessary for us to compute effective actions.

$$\begin{aligned} S_{\text{NC}} = & \int d^8z \left\{ \Phi^+ \Phi - \frac{m}{8} \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{m}{8} \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) - \frac{g}{12} \Phi \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{g}{12} \Phi^+ \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) \right. \\ & + \frac{1}{32} (-g) \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) + \frac{1}{32} (-g) \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\ & + \frac{1}{6} (-g) \Lambda^{kl} \theta^4 \Phi^+ \square \Phi^+ \partial_k \partial_l \Phi^+ + \frac{1}{3} (-g) (\sigma \Lambda^{kl})^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+ \\ & + \frac{1}{6} g \eta^{kl} \Lambda^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+ + \frac{1}{16} (-g) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi) \\ & + \frac{1}{16} (-g) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k_\beta \Lambda^l_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\ & \left. + \frac{1}{3072} (-g) \Lambda^{kl} \Lambda^{no} \theta^4 (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \partial_o \partial_n (D^2 \Phi) \right\}, \end{aligned}$$

# Background Field Method

- ① Split superfields,

$$\Phi \rightarrow \Phi + \Phi_q, \quad \Phi^+ \rightarrow \Phi^+ + \Phi_q^+,$$

- ② Represent them by the general superfields,

$$\Phi_q = -\frac{1}{4}\bar{D}^2\Sigma, \quad \Phi_q^+ = -\frac{1}{4}D^2\Sigma^+,$$

- ③ New gauge symmetry,

$$\Sigma \rightarrow \Sigma + \bar{D}_{\dot{\alpha}}\bar{\Lambda}^{\dot{\alpha}}, \quad \Sigma^+ \rightarrow \Sigma^+ + D^\alpha\Lambda_\alpha,$$

- ④ Gauge fixing action  $\mathcal{S}_{\text{GF}}$ ,

$$\mathcal{S}_{\text{GF}} = \int d^8z \left\{ -\frac{3}{16}\xi\epsilon^{\dot{\alpha}\dot{\beta}}(\bar{D}_{\dot{\alpha}}\Sigma^+) (\bar{D}_{\dot{\beta}}D^2\Sigma) - \frac{1}{4}\xi\epsilon^{\alpha\beta}\epsilon^{\dot{\gamma}\dot{\delta}}(\bar{D}_{\dot{\gamma}}\Sigma^+) (D_\beta\bar{D}_i D_\alpha\Sigma) \right\},$$

- ⑤ Quadratic part,

$$\mathcal{S}^{(2)} = \frac{1}{2} \int d^8z \begin{pmatrix} \Sigma & \Sigma^+ \end{pmatrix} (M + V) \begin{pmatrix} \Sigma \\ \Sigma^+ \end{pmatrix},$$

- ⑥ One-loop  $n$ -point,

$$\Gamma = \frac{i}{2}\text{STr} \ln(1 + M^{-1}V) = \frac{i}{2} \sum_{n=1}^{\infty} \text{STr} \left[ \frac{(-1)^{n+1}}{n} (M^{-1}V)^n \right] \equiv \sum_{n=1}^{\infty} \Gamma^{(n)},$$

# Calculate Supertrace

① N points,

$$\text{STr} \left\{ \underbrace{\left( \mathcal{D}_{A_1} \partial_{C_1} \frac{1}{\square - m^2} (\square^{-1})^{s_1} \theta^4 \mathcal{F}_{B_1} \partial_{C'_1} \mathcal{D}_{A'_1} \right) \cdots \left( \mathcal{D}_{A_n} \partial_{C_n} \frac{1}{\square - m^2} (\square^{-1})^{s_n} \theta^4 \mathcal{F}_{B_n} \partial_{C'_n} \mathcal{D}_{A'_n} \right)}_{n \text{ terms}} \right\},$$

② Take  $n = 2$  as a sample,

$$(-1)^{|\mathcal{X}|+|\mathcal{Y}|} \text{STr} \left\{ \partial_{C'_2} \mathcal{D}_{A'_2} \left( \mathcal{D}_{A_1} \partial_{C_1} \frac{1}{\square - m^2} (\square^{-1})^{s_1} \theta^4 \mathcal{F}_{B_1} \partial_{C'_1} \mathcal{D}_{A'_1} \right) \mathcal{D}_{A_2} \partial_{C_2} \frac{1}{\square - m^2} (\square^{-1})^{s_2} \theta^4 \mathcal{F}_{B_2} \right\},$$

③ Move  $D$  operators,

$$\text{STr} \left\{ \partial_{C'_2} \partial_{C_1} \frac{1}{\square - m^2} (\square^{-1})^{s_1} \left( \mathcal{D}_{A''_1} \theta^4 \right) \mathcal{F}_{B'_1} \partial_{C'_1} \partial_{C_2} \frac{1}{\square - m^2} (\square^{-1})^{s_2} \mathcal{D}_{A''_2} \theta^4 \mathcal{F}_{B_2} \right\},$$

④ Only when  $\mathcal{D}_{A''_1} = D^2 \bar{D}^2$ ,

$$\text{STr} \left\{ \partial_{C'_2} \partial_{C_1} \frac{1}{\square - m^2} (\square^{-1})^{s_1} \mathcal{F}_{B'_1} \partial_{C'_1} \partial_{C_2} \frac{1}{\square - m^2} (\square^{-1})^{s_2} \mathcal{D}_{A''_2} \theta^4 \mathcal{F}_{B_2} \right\},$$

⑤ Only when  $\mathcal{D}_{A''_2} = D^2 \bar{D}^2$ ,

$$\text{Tr} \left\{ \partial_{C'_2} \partial_{C_1} \frac{1}{\square - m^2} (\square^{-1})^{s_1} \mathcal{F}_{B'_1} \partial_{C'_1} \partial_{C_2} \frac{1}{\square - m^2} (\square^{-1})^{s_2} \theta^4 \mathcal{F}_{B_2} \right\},$$

# The Actual Calculation

- Design Mathematica program to manage the algebra.
- Simplify the result as much as possible.
- Verify the result by using 1/2 supersymmetry invariance.
- Find new algebra relations.
- Optimize program.
- Represent the result.

simplification       $\Leftrightarrow$       verification

# New Notations for Presenting Effective Actions

- We define the new symbols for presenting actions in a concise form,

$$\Lambda^{kl} \equiv \epsilon^{\alpha\beta} \Lambda_{\beta}^k \Lambda_{\alpha}^l, \quad \Lambda^2 \equiv \eta_{kl} \Lambda^{kl},$$

$$\sigma \Lambda \Lambda \equiv \eta_{kn} \eta_{lo} (\sigma^{kl})^{\alpha\beta} \Lambda^n_{\alpha} \Lambda^o_{\beta}, \quad (\sigma \Lambda^{kl})^{n\alpha} \equiv (\sigma^{kl})^{\beta\alpha} \Lambda^n_{\beta},$$

$$(\eta \sigma \Lambda^k)^{\alpha} \equiv \eta_{ln} (\sigma^{nk})^{\beta\alpha} \Lambda'_{\beta}, \quad (\eta \sigma \Lambda \Lambda^k)' \equiv \eta_{no} (\sigma^{ok})^{\alpha\beta} \Lambda^n_{\alpha} \Lambda'_{\beta},$$

$$(\sigma \Lambda \Lambda^{kl})^{no} \equiv (\sigma^{kl})^{\alpha\beta} \Lambda^n_{\alpha} \Lambda^o_{\beta}.$$

- In addition, we hide the superscripts and/or subscripts of Bosonic derivatives, but only show the number of their product, for example,  $\partial_k \partial_l$  is written as  $\partial \partial$ , and also hide the subscripts of Fermionic derivatives, such as  $D$  and  $\bar{D}$  denoting  $D_{\alpha}$  and  $\bar{D}_{\dot{\beta}}$ , respectively.
- In particular, for all terms in effective actions we pick out different BFNC parameter factors as one class and different operator factors as the other class, which gives an explicit outline of effective actions.

# Structure of $\mathcal{S}_{\text{NC}}$

$$\begin{aligned}
 \mathcal{S}_{\text{NC}} = & \int d^8 z \left\{ \phi^+ \phi - \frac{m}{8} \phi \left( \frac{D^2}{\square} \phi \right) - \frac{m}{8} \phi^+ \left( \frac{\bar{D}^2}{\square} \phi^+ \right) - \frac{g}{12} \phi \phi \left( \frac{D^2}{\square} \phi \right) - \frac{g}{12} \phi^+ \phi^+ \left( \frac{\bar{D}^2}{\square} \phi^+ \right) \right. \\
 & + \frac{1}{32} (-g) \Lambda^{kl} \theta^4 \phi \left( D^2 \phi \right) \partial_l \partial_k \left( D^2 \phi \right) + \frac{1}{32} (-g) \Lambda^{kl} \theta^4 \phi \partial_k \left( D^2 \phi \right) \partial_l \left( D^2 \phi \right) \\
 & + \frac{1}{6} (-g) \Lambda^{kl} \theta^4 \phi^+ \square \phi^+ \partial_k \partial_l \phi^+ + \frac{1}{3} (-g) (\sigma \Lambda^{kl})^{no} \theta^4 \phi^+ \partial_k \partial_n \phi^+ \partial_l \partial_o \phi^+ \\
 & + \frac{1}{6} g \eta^{kl} \Lambda^{no} \theta^4 \phi^+ \partial_k \partial_n \phi^+ \partial_l \partial_o \phi^+ + \frac{1}{16} (-g) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \phi) \partial_l (D_\beta \phi) \left( D^2 \phi \right) \\
 & + \frac{1}{16} (-g) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\zeta \theta^4 \partial_k (D_\alpha \phi) \partial_l (D_\beta \phi) \left( D^2 \phi \right) \\
 & \left. + \frac{1}{3072} (-g) \Lambda^{kl} \Lambda^{no} \theta^4 \left( D^2 \phi \right) \partial_l \partial_k \left( D^2 \phi \right) \partial_o \partial_n \left( D^2 \phi \right) \right\},
 \end{aligned}$$

- Structure of  $\mathcal{S}_{\text{NC}}$ , BFNC parameter factors and operators,

$$\begin{aligned}
 & \Lambda^{kl}, \quad (\sigma \Lambda \Lambda^{kl})^{no}, \quad \eta^{kl} \Lambda^{no}, \quad \epsilon^{\alpha\beta} \Lambda^{kl}, \quad \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\zeta, \quad \Lambda^{kl} \Lambda^{no}, \\
 & \partial \partial \phi \left( D^2 \phi \right) \left( D^2 \phi \right), \quad \partial \partial (D \phi) (D \phi) \left( D^2 \phi \right), \quad \partial \partial \partial \phi^+ \phi^+ \phi^+, \\
 & \partial \partial \partial (D^2 \phi) \left( D^2 \phi \right) \left( D^2 \phi \right).
 \end{aligned}$$

# Structure of $\Gamma_{1st}$ in order $\Lambda^2$

As the first step of searching the renormalizable Wess-Zumino model on the BFNC superspace, we calculate the effective action of  $S_{NC}$  by using the background field method and denote it as  $\Gamma_{1st}$ . The structure of  $\Gamma_{1st}$  in order  $\Lambda^2$  is as follows,

- 14 BFNC parameter factors,

$$\begin{aligned} & \left( \eta \sigma \Lambda \Lambda^k \right)^l, \quad \Lambda^2, \quad \Lambda^{kl}, \quad \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^l, \quad \epsilon^{\alpha\beta} \Lambda^{kl}, \quad \Lambda^2 \eta^{kl}, \quad \Lambda^2 \epsilon^{\alpha\beta}, \quad \Lambda^2 \epsilon^{\dot{\alpha}\dot{\beta}}, \\ & \Lambda^2 \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta}, \quad \Lambda^2 \eta^{kl} \epsilon^{\alpha\beta}, \quad \Lambda^{kl} \eta_{ln} \left( \bar{\sigma}^n \right)^{\dot{\alpha}\beta}, \quad \eta_{kl} \left( \bar{\sigma}^l \right)^{\dot{\alpha}\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^n, \quad \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\zeta, \\ & \epsilon^{\alpha\beta} \eta_{kl} \left( \sigma \Lambda^{ln} \right)^{\circ\zeta} \Lambda^k{}_\beta. \end{aligned}$$

- 4 operators for 2 points,

$$\partial\partial\Phi (D^2\Phi), \quad \partial\partial(D\Phi)(D\Phi), \quad \partial\partial(D^2\Phi) \Phi^+, \quad \partial\partial\partial\partial(D^2\Phi) \Phi^+;$$

- 5 operators for 3 points,

$$\begin{aligned} & (D^2\Phi) (D^2\Phi) (\bar{D}^2\Phi^+), \quad \partial(D\Phi) (D^2\Phi) (\bar{D}\Phi^+), \quad \partial\partial\Phi (D^2\Phi) \Phi^+, \\ & \partial\partial(D\Phi)(D\Phi)\Phi^+, \quad \partial\partial(D^2\Phi) \Phi^+ \Phi^+; \end{aligned}$$

- 5 operators for 4 points,

$$\begin{aligned} & (D^2\Phi) (D^2\Phi) (\bar{D}\Phi^+) (\bar{D}\Phi^+), \quad (D^2\Phi) (D^2\Phi) \Phi^+ (\bar{D}^2\Phi^+), \\ & \partial(D\Phi) (D^2\Phi) \Phi^+ (\bar{D}\Phi^+), \quad \partial\partial\Phi (D^2\Phi) \Phi^+ \Phi^+, \quad \partial\partial(D\Phi)(D\Phi)\Phi^+ \Phi^+. \end{aligned}$$

# Comments

- We verify that  $\Gamma_{1st}$  is invariant under the 1/2 supersymmetry transformation.
- We see explicitly that  $\Gamma_{1st}$  cannot be absorbed by  $\mathcal{S}_{NC}$  because  $\Gamma_{1st}$  contains many extra terms that do not exist in  $\mathcal{S}_{NC}$ .

# Compare With NAC

- NAC, [M. T. Grisaru et al, hep-th/0307099].

$$\frac{-1}{\epsilon} g^2 \int d^8 z \ (m^*)^2 U (D^2 \Phi)^2, \quad U = \theta^2 \bar{\theta}^2 C^2,$$

The renormalizable action can be obtained by adding the effective action to the deformed Wess-Zumino model on the NAC superspace.

- BFNC: In our case the number of correction terms that should be added to  $S_{\text{NC}}$  is very large, for instance,  $\Gamma_{1\text{st}}$  contains 68 terms only at the order of  $\Lambda^2$ . So, it is a tremendously exciting challenge to find out the successive effective actions needed.

# Define $\mathcal{S}_{(1)}$ , Calculate Its Effective Action $\Gamma_{\text{2nd}}$

- $\Gamma_{\text{2nd}}$ : effective action of  $\mathcal{S}_{\text{NC}} + \Gamma_{\text{1st}}$ .

$$\begin{aligned}\mathcal{S}_{(1)} &\equiv \mathcal{S}_{\text{WZ}} + \mathcal{S}_\Lambda(\Lambda^2) + \Gamma_{\text{1st}}(\Lambda^2), \\ \mathcal{S}_{\text{WZ}} &= \mathcal{S}_0 + \mathcal{S}_{\text{int}}.\end{aligned}$$

- Gauge fixing term:  $\mathcal{S}_{\text{GF}}$ .  $\mathcal{S}_0 + \mathcal{S}_{\text{GF}} \rightarrow M$ .  $\mathcal{S}_{\text{int}} + \Gamma_{\text{1st}}(\Lambda^2) \rightarrow V_{(1)}$ .
- Result: 13 BFNC parameter factors, 6 groups of different operator factors.
- $\Gamma_{\text{2nd}}(\Lambda^2)$  cannot be absorbed by  $\mathcal{S}_{(1)}$ .

# Structure of $\Gamma_{2\text{nd}}$ in order $\Lambda^2$

13 BFNC parameter factors, 6 groups of different operator factors.

$$\begin{aligned} \sigma \Lambda \Lambda, \quad \Lambda^2 (\sigma^{kl})^{\alpha\beta}, \quad \sigma \Lambda \Lambda \eta^{kl}, \quad \sigma \Lambda \Lambda \epsilon^{\alpha\beta}, \quad \sigma \Lambda \Lambda \epsilon^{\dot{\alpha}\dot{\beta}}, \quad \sigma \Lambda \Lambda (\bar{\sigma}^k)^{\dot{\alpha}\beta}, \quad \epsilon^{\alpha\beta} (\eta \sigma \Lambda^k)^\zeta \Lambda_\beta^l, \quad \Lambda^2 \eta^{kl} \eta^{no}, \\ \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta}, \quad \sigma \Lambda \Lambda \eta^{kl} \epsilon^{\alpha\beta}, \quad \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda^n)^k, \quad \epsilon^{\alpha\beta} \eta_{kl} (\eta \sigma \Lambda^l)^\zeta \Lambda_\beta^k, \quad \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{np} \eta_{oq} \Lambda_\beta^p \Lambda_\iota^q. \end{aligned}$$

$D^2\Phi$ ; (1)

$$\Phi(D^2\Phi), \quad (D\Phi)(D\Phi), \quad (D^2\Phi)(D^2\Phi), \quad (D^2\Phi)(\bar{D}^2\Phi^+), \quad (D^2\Phi)\Phi^+, \quad \partial(D\Phi)(\bar{D}\Phi^+), \quad \partial\partial\Phi\Phi^+,$$

$\partial\partial(D^2\Phi)(D^2\Phi), \quad \partial\partial\Phi^+\Phi^+, \quad \partial\partial\partial\Phi^+\Phi^+$ ; (10)

$$\Phi\Phi(D^2\Phi), \quad \Phi(D\Phi)(D\Phi), \quad \Phi(D^2\Phi)(D^2\Phi), \quad \Phi(D^2\Phi)\Phi^+, \quad (D\Phi)(D\Phi)(D^2\Phi), \quad (D\Phi)(D\Phi)\Phi^+, \quad (D^2\Phi)(D^2\Phi)\Phi^+,$$

$$(D^2\Phi)(\bar{D}\Phi^+)(\bar{D}\Phi^+), \quad (D^2\Phi)\Phi^+(\bar{D}^2\Phi^+), \quad (D^2\Phi)\Phi^+\Phi^+, \quad \partial(D\Phi)\Phi^+(\bar{D}\Phi^+), \quad \partial\partial\Phi\Phi^+\Phi^+, \quad \partial\partial\Phi^+\Phi^+\Phi^+;$$

$$\Phi\Phi(D^2\Phi)(D^2\Phi), \quad \Phi\Phi(D^2\Phi)\Phi^+, \quad \Phi(D\Phi)(D\Phi)(D^2\Phi), \quad \Phi(D\Phi)(D\Phi)\Phi^+, \quad \Phi(D^2\Phi)(D^2\Phi)\Phi^+, \quad \Phi(D^2\Phi)\Phi^+\Phi^+,$$

$$(D\Phi)(D\Phi)(D^2\Phi)\Phi^+, \quad (D\Phi)(D\Phi)\Phi^+\Phi^+, \quad (D^2\Phi)\Phi^+(\bar{D}\Phi^+)(\bar{D}\Phi^+), \quad (D^2\Phi)\Phi^+\Phi^+(\bar{D}^2\Phi^+), \quad (D^2\Phi)\Phi^+\Phi^+\Phi^+,$$

$\partial(D\Phi)\Phi^+\Phi^+(\bar{D}\Phi^+), \quad \partial\partial\Phi\Phi^+\Phi^+\Phi^+, \quad \partial\partial\Phi^+\Phi^+\Phi^+\Phi^+$ ; (14)

$$\Phi\Phi(D^2\Phi)(D^2\Phi)\Phi^+, \quad \Phi\Phi(D^2\Phi)\Phi^+\Phi^+, \quad \Phi(D\Phi)(D\Phi)(D^2\Phi)\Phi^+, \quad \Phi(D\Phi)(D\Phi)\Phi^+\Phi^+, \quad \Phi(D^2\Phi)\Phi^+\Phi^+\Phi^+,$$

$$(D\Phi)(D\Phi)\Phi^+\Phi^+\Phi^+, \quad (D^2\Phi)\Phi^+\Phi^+(\bar{D}\Phi^+)(\bar{D}\Phi^+), \quad (D^2\Phi)\Phi^+\Phi^+\Phi^+(\bar{D}^2\Phi^+), \quad \partial(D\Phi)\Phi^+\Phi^+\Phi^+(\bar{D}\Phi^+),$$

$\partial\partial\Phi\Phi^+\Phi^+\Phi^+$ ; (10)

$$\Phi\Phi(D^2\Phi)\Phi^+\Phi^+\Phi^+, \quad \Phi(D\Phi)(D\Phi)\Phi^+\Phi^+\Phi^+. \quad (2)$$

# Comments

- Because of the existence of the above new forms,  $\Gamma_{2\text{nd}}(\Lambda^2)$  cannot be absorbed by  $S_{(1)}$ , which means  $S_{(1)}$  is still not renormalizable.
- Different from NAC case, we have to compute the third successive effective action  $\Gamma_{3\text{rd}}$ .

# Define $\mathcal{S}_{(2)}$ , Calculate Its Effective Action $\Gamma_{\text{3rd}}$

- Define

$$\mathcal{S}_{(2)} \equiv \mathcal{S}_{(1)} + \Gamma_{\text{2nd}} (\Lambda^2),$$

- New BFNC parameter factors that do not appear in  $\mathcal{S}_{(2)}$ ,

$$\eta^{kl} (\eta \sigma \Lambda \Lambda^n)^o, \quad \sigma \Lambda \Lambda (\sigma^{kl})^{\alpha\beta}.$$

- The operator factors in  $\Gamma_{\text{3rd}} (\Lambda^2)$  are exactly same as that in  $\mathcal{S}_{(2)}$ .

# Comments

- Therefore, there are still some terms in  $\Gamma_{3\text{rd}}(\Lambda^2)$  that cannot be absorbed by  $S_{(2)}$ . The reason is obvious because these terms are the products of the new BFNC parameter factors and the operator factors.
- This implies that we have to continue the iterative procedure in order to find the renormalizable Wess-Zumino model that possesses the  $1/2$  supersymmetry invariance on the BFNC superspace.
- At this stage, we notice that many terms in  $\Gamma_{1\text{st}}(\Lambda^2)$ ,  $\Gamma_{2\text{nd}}(\Lambda^2)$ , and  $\Gamma_{3\text{rd}}(\Lambda^2)$  are same, which brings us to compare the three effective actions and to analyze their structures.

# 1/2 Supersymmetry Invariant Subset

We explain our proposal as follows by using  $\Gamma_{1\text{st}}(\Lambda^2)$  as an example.

$$\Gamma_{1\text{st}}(\Lambda^2) = \sum_{i=1}^n L_i \quad \xrightarrow{\hspace{1cm}} \quad A = \sum_{i=1}^n X_i L_i \quad \xrightarrow{\hspace{1cm}} \quad \delta_\xi A = \sum_{j=1}^{n'} Y_j L'_j$$

$$Y_j = \sum_{i=1}^n c_{ji} X_i \quad \xrightarrow{\hspace{1cm}} \quad U_j = \{X_{i_1}, X_{i_2}, \dots\} \quad \xrightarrow{\hspace{1cm}} \quad W = \{U_1, U_2, \dots, U_{n'}\}$$

$$U_j \cap U_{j'} \neq \emptyset \quad \xrightarrow{\hspace{1cm}} \quad U_{jj'} \equiv U_j \cup U_{j'}, \quad (j \neq j')$$

$$W \quad \xrightarrow{\hspace{1cm}} \quad W' = \{I_1, I_2, \dots, I_m, \dots\}, \quad (I_m \cap I_{m'} = \emptyset \text{ when } m \neq m')$$

$$I_m = \{X_{m_1}, X_{m_2}, \dots\} \quad \xrightarrow{\hspace{1cm}} \quad f_m = \sum_{i=\{m_1, m_2, \dots\}} L_i$$

- The numbers of 1/2 supersymmetry invariant subsets of  $S_\Lambda(\Lambda^2)$ ,  $\Gamma_{1\text{st}}(\Lambda^2)$ ,  $\Gamma_{2\text{nd}}(\Lambda^2)$  and  $\Gamma_{3\text{rd}}(\Lambda^2)$  are 4, 17, 64 and 73.

# Analysis of Effective Actions by Invariant Subsets

- Construct a new action,

$$\Gamma(\Lambda^2) = \textcolor{red}{a_0} S_\Lambda(\Lambda^2) + \textcolor{red}{a_1} \Gamma_{1\text{st}}(\Lambda^2) + \textcolor{red}{a_2} \Gamma_{2\text{nd}}(\Lambda^2) + \textcolor{red}{a_3} \Gamma_{3\text{rd}}(\Lambda^2),$$

- $f_i$  represent all 74 invariant subsets of  $\Gamma(\Lambda^2)$ ,

$$\Gamma(\Lambda^2) = \sum_{i=1}^{74} f_i,$$

We list the 74 subsets  $f_i$ 's below, each of them is invariant under the 1/2 supersymmetry transformation.

$$f_1 = \frac{1}{512} g^4 m^4 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10a_2 - 71g^2 a_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi)$$

$$+ \frac{1}{512} g^4 m^4 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10a_2 + 71g^2 a_3) \theta^4 \Phi (D^2 \Phi),$$

$$f_2 = \frac{1}{256} g^5 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10a_2 - 71g^2 a_3) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi)$$

$$+ \frac{1}{512} g^5 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10a_2 + 71g^2 a_3) \theta^4 \Phi \Phi (D^2 \Phi),$$

$$f_3 = \frac{3}{256} g^5 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10a_2 - 71g^2 a_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+$$

$$+ \frac{3}{256} g^5 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10a_2 + 71g^2 a_3) \theta^4 \Phi (D^2 \Phi) \Phi^+,$$

$$f_4 = \frac{3}{128} g^6 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10a_2 - 71g^2 a_3) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+$$

$$+ \frac{3}{256} g^6 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10a_2 + 71g^2 a_3) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+,$$

$$f_5 = \frac{3}{128} g^6 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10a_2 - 71g^2 a_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+$$

$$+ \frac{3}{128} g^6 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10a_2 + 71g^2 a_3) \theta^4 \Phi (D^2 \Phi) \Phi^+ \Phi^+,$$

$$\begin{aligned} f_6 &= \frac{3}{64} g^7 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10\textcolor{red}{a}_2 - 71g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \\ &\quad + \frac{3}{128} g^7 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10\textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+ \Phi^+, \end{aligned}$$

$$\begin{aligned} f_7 &= \frac{1}{64} g^7 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10\textcolor{red}{a}_2 - 71g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+ \\ &\quad + \frac{1}{64} g^7 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10\textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 \Phi (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+, \end{aligned}$$

$$\begin{aligned} f_8 &= \frac{1}{32} g^8 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (10\textcolor{red}{a}_2 - 71g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+ \\ &\quad + \frac{1}{64} g^8 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-10\textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+, \end{aligned}$$

$$\begin{aligned} f_9 &= \frac{1}{512} g^5 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (2\textcolor{red}{a}_2 - 15g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \\ &\quad + \frac{1}{512} g^5 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2\textcolor{red}{a}_2 + 15g^2 \textcolor{red}{a}_3) \theta^4 \Phi (D^2 \Phi) (D^2 \Phi), \end{aligned}$$

$$\begin{aligned} f_{10} &= \frac{1}{256} g^6 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (2\textcolor{red}{a}_2 - 15g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \\ &\quad + \frac{1}{512} g^6 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2\textcolor{red}{a}_2 + 15g^2 \textcolor{red}{a}_3) \theta^4 \Phi \Phi (D^2 \Phi) (D^2 \Phi), \end{aligned}$$

$$\begin{aligned} f_{11} &= \frac{1}{256} g^6 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (2\textcolor{red}{a}_2 - 15g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \Phi^+ \\ &\quad + \frac{1}{256} g^6 m (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2\textcolor{red}{a}_2 + 15g^2 \textcolor{red}{a}_3) \theta^4 \Phi (D^2 \Phi) (D^2 \Phi) \Phi^+, \end{aligned}$$

$$\begin{aligned} f_{12} = & \frac{1}{128} g^7 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (2a_2 - 15g^2 a_3) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \Phi^+ \\ & + \frac{1}{256} g^7 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2a_2 + 15g^2 a_3) \theta^4 \Phi \Phi (D^2 \Phi) (D^2 \Phi) \Phi^+, \end{aligned}$$

$$\begin{aligned} f_{13} = & \frac{1}{64} ig^5 m^2 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (a_2 - 4g^2 a_3) (\bar{\sigma}^k)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\ & + \frac{1}{32} g^5 m^2 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \eta^{kl} \theta^4 \Phi \partial_k \Phi^+ \partial_l \Phi^+ \\ & + \frac{1}{512} g^5 m^2 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+), \end{aligned}$$

$$\begin{aligned} f_{14} = & \frac{1}{16} ig^6 m (3\Lambda^2 - 2\sigma\Lambda\Lambda) (a_2 - 4g^2 a_3) (\bar{\sigma}^k)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\ & + \frac{1}{8} g^6 m (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \eta^{kl} \theta^4 \Phi \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+ \\ & + \frac{1}{128} g^6 m (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+), \end{aligned}$$

$$\begin{aligned} f_{15} = & \frac{1}{16} ig^7 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (a_2 - 4g^2 a_3) (\bar{\sigma}^k)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \Phi^+ \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\ & + \frac{1}{8} g^7 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \eta^{kl} \theta^4 \Phi \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+ \\ & + \frac{1}{128} g^7 (3\Lambda^2 - 2\sigma\Lambda\Lambda) (-a_2 + 4g^2 a_3) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+), \end{aligned}$$

$$f_{16} = \frac{1}{2304} g^4 m^2 (-4a_2 + 23g^2 a_3) (\eta \sigma \Lambda \Lambda^k)' \theta^4 \Phi \partial_k \partial_l (D^2 \Phi)$$

$$\begin{aligned}
& + \frac{1}{2304} g^4 m^2 (-4 \textcolor{red}{a}_2 + 23g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi), \\
f_{17} &= \frac{1}{288} g^5 m \textcolor{red}{a}_2 \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda^k \right)^\zeta \Lambda'{}_\beta \theta^4 (D_\alpha \Phi) \partial_k \partial_l (D_\zeta \Phi) \Phi^+ \\
& - \frac{1}{36} g^5 m \textcolor{red}{a}_2 \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda^k \right)^\zeta \Lambda'{}_\beta \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \\
& + \frac{1}{9216} i g^5 m (-4 \textcolor{red}{a}_2 + 23g^2 \textcolor{red}{a}_3) \eta_{kl} \left( \bar{\sigma}' \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^n)^k \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{9216} i g^5 m (-4 \textcolor{red}{a}_2 + 23g^2 \textcolor{red}{a}_3) \eta_{kl} \left( \bar{\sigma}' \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^n)^k \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{4608} i g^5 m (-4 \textcolor{red}{a}_2 + 23g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{n\rho} \eta_{oq} \Lambda^p{}_\beta \Lambda^q{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \\
& + \frac{1}{1152} g^5 m (28 \textcolor{red}{a}_2 + 23g^2 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_o (D_\beta \Phi) \Phi^+ \\
& + \frac{1}{4608} g^5 m (-124 \textcolor{red}{a}_2 + 129g^2 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \\
& + \frac{1}{288} g^3 m (9 \textcolor{red}{a}_1 - 6g^2 \textcolor{red}{a}_2 + 17g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \\
& + \frac{1}{288} g^3 m (27 \textcolor{red}{a}_1 - 37g^2 \textcolor{red}{a}_2 + 69g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \\
& - \frac{1}{4608} i g^3 m (36 \textcolor{red}{a}_1 - 52g^2 \textcolor{red}{a}_2 + 83g^4 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{4608} i g^3 m (36 \textcolor{red}{a}_1 - 52g^2 \textcolor{red}{a}_2 + 83g^4 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+)
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{576} g^3 m (36 \textcolor{red}{a}_1 - 40g^2 \textcolor{red}{a}_2 + 87g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \\
& - \frac{1}{288} g^3 m (36 \textcolor{red}{a}_1 - 57g^2 \textcolor{red}{a}_2 + 106g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \eta_{kl} (\sigma \Lambda^{ln})^{o\zeta} \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \partial_n \partial_o (D_\zeta \Phi) \Phi^+ \\
& - \frac{1}{576} g^3 m (72 \textcolor{red}{a}_1 - 92g^2 \textcolor{red}{a}_2 + 189g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \eta_{kl} (\sigma \Lambda^{ln})^{o\zeta} \Lambda^k{}_\beta \theta^4 \partial_n (D_\alpha \Phi) \partial_o (D_\zeta \Phi) \Phi^+ \\
& + \frac{1}{576} g^3 m (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi \partial_k \partial_l (D^2 \Phi) \Phi^+ \\
& + \frac{1}{1152} g^3 m (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \Phi^+ \\
& + \frac{1}{288} g^3 m (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi) \Phi^+ \\
& + \frac{1}{2304} g^3 m (144 \textcolor{red}{a}_1 - 156g^2 \textcolor{red}{a}_2 + 325g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \\
& + \frac{1}{9216} ig^3 m (144 \textcolor{red}{a}_1 - 220g^2 \textcolor{red}{a}_2 + 401g^4 \textcolor{red}{a}_3) \\
& \quad \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{9216} ig^3 m (144 \textcolor{red}{a}_1 - 220g^2 \textcolor{red}{a}_2 + 401g^4 \textcolor{red}{a}_3) \\
& \quad \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{2304} g^3 m (144 \textcolor{red}{a}_1 - 220g^2 \textcolor{red}{a}_2 + 401g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{1152} g^3 m (180 \textcolor{red}{a}_1 - 244 g^2 \textcolor{red}{a}_2 + 469 g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) \Phi^+ \\
& + \frac{1}{2304} g^3 m (288 \textcolor{red}{a}_1 - 372 g^2 \textcolor{red}{a}_2 + 703 g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda^\kappa)^l \theta^4 \partial_k \Phi \partial_l (D^2 \Phi) \Phi^+ \\
& + \frac{1}{1152} g^3 m (288 \textcolor{red}{a}_1 - 372 g^2 \textcolor{red}{a}_2 + 703 g^4 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} (\eta \sigma \Lambda^\kappa)^l \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) \Phi^+ \\
& + \frac{1}{2304} (4g^5 m \textcolor{red}{a}_2 - 23g^7 m \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \eta_{kl} (\eta \sigma \Lambda')^\zeta \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \square (D_\zeta \Phi) \Phi^+ \\
& + \frac{1}{576} (6g^5 m \textcolor{red}{a}_2 - 23g^7 m \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 (D_\alpha \Phi) \partial_k \partial_o (D_\beta \Phi) \Phi^+ \\
& + \frac{1}{9216} g^3 m (288 \Lambda^2 \textcolor{red}{a}_1 - 16g^2 (22 \Lambda^2 - 7 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + 3g^4 (407 \Lambda^2 - 122 \sigma \Lambda \Lambda) \textcolor{red}{a}_3) \\
& \quad \theta^4 \square \Phi (D^2 \Phi) \Phi^+ \\
& + \frac{1}{49152} g^3 m (48 \Lambda^2 \textcolor{red}{a}_1 - 8g^2 (15 \Lambda^2 + 2 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + 3g^4 (127 \Lambda^2 + 18 \sigma \Lambda \Lambda) \textcolor{red}{a}_3) \\
& \quad \theta^4 (D^2 \Phi) (D^2 \Phi) (\bar{D}^2 \Phi^+) \\
& + \frac{1}{4608} g^5 m (148 \Lambda^2 \textcolor{red}{a}_2 + g^2 (-689 \Lambda^2 + 252 \sigma \Lambda \Lambda) \textcolor{red}{a}_3) \\
& \quad (\sigma^{kl})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \\
& + \frac{1}{2304} g^3 m (72 \Lambda^2 \textcolor{red}{a}_1 + g^2 ((-51 \Lambda^2 + 30 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (133 \Lambda^2 - 40 \sigma \Lambda \Lambda) \textcolor{red}{a}_3))
\end{aligned}$$

$$\theta^4 \Phi \square (D^2 \Phi) \Phi^+$$

$$\begin{aligned}
& + \frac{1}{9216} g^3 m (576 \Lambda^2 \textcolor{red}{a}_1 + g^2 ((-636 \Lambda^2 + 72 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (1565 \Lambda^2 + 106 \sigma \Lambda \Lambda) \textcolor{red}{a}_3)) \\
& \quad \eta^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \\
& + \frac{1}{36864} i g^3 m (288 \Lambda^2 \textcolor{red}{a}_1 + g^2 (-4 (217 \Lambda^2 + 26 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (2975 \Lambda^2 + 118 \sigma \Lambda \Lambda) \textcolor{red}{a}_3)) \\
& \quad \left( \bar{\sigma}^k \right)^{\dot{\alpha} \beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{9216} g^3 m (-288 \Lambda^2 \textcolor{red}{a}_1 + g^2 (-84 (\Lambda^2 + 2 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (721 \Lambda^2 + 218 \sigma \Lambda \Lambda) \textcolor{red}{a}_3)) \\
& \quad \eta^{kl} \epsilon^{\alpha \beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \\
& + \frac{1}{36864} i g^3 m (288 \Lambda^2 \textcolor{red}{a}_1 + g^2 (-44 (13 \Lambda^2 + 2 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (1597 \Lambda^2 + 530 \sigma \Lambda \Lambda) \textcolor{red}{a}_3)) \\
& \quad \left( \bar{\sigma}^k \right)^{\dot{\alpha} \beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{9216} g^3 m (288 \Lambda^2 \textcolor{red}{a}_1 + g^2 (4 (41 \Lambda^2 + 84 \sigma \Lambda \Lambda) \textcolor{red}{a}_2 - g^2 (533 \Lambda^2 + 896 \sigma \Lambda \Lambda) \textcolor{red}{a}_3)) \\
& \quad \epsilon^{\alpha \beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi) \Phi^+,
\end{aligned}$$

$$\begin{aligned}
f_{18} &= \frac{1}{4608} g^2 m^2 (144 \textcolor{red}{a}_1 - 220 g^2 \textcolor{red}{a}_2 + 401 g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \\
& + \frac{1}{4608} g^2 m^2 (144 \textcolor{red}{a}_1 - 220 g^2 \textcolor{red}{a}_2 + 401 g^4 \textcolor{red}{a}_3) \epsilon^{\alpha \beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi),
\end{aligned}$$

$$\begin{aligned}
f_{19} &= \frac{1}{576} (-72g^4 \textcolor{red}{a}_1 + 116g^6 \textcolor{red}{a}_2 - 235g^8 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \partial_k \partial_l \Phi^+ \\
&\quad + \frac{1}{576} (72g^4 \textcolor{red}{a}_1 - 116g^6 \textcolor{red}{a}_2 + 235g^8 \textcolor{red}{a}_3) \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \Phi (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+, \\
f_{20} &= \frac{1}{1152} (-72g^4 \textcolor{red}{a}_1 + 116g^6 \textcolor{red}{a}_2 - 235g^8 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \partial_k \partial_l \Phi^+ \\
&\quad + \frac{1}{1152} (72g^4 \textcolor{red}{a}_1 - 116g^6 \textcolor{red}{a}_2 + 235g^8 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+, \\
f_{21} &= \frac{g^6 \textcolor{red}{a}_2}{288} \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda^k \right)^\zeta \Lambda^l \beta \theta^4 (D_\alpha \Phi) \partial_k \partial_l (D_\zeta \Phi) \Phi^+ \Phi^+ \\
&\quad - \frac{1}{36} g^6 \textcolor{red}{a}_2 \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda^k \right)^\zeta \Lambda^l \beta \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \Phi^+ \\
&\quad - \frac{1}{768} ig^6 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-5\textcolor{red}{a}_2 + 18g^2 \textcolor{red}{a}_3) \\
&\quad \quad \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) (D^2 \Phi) \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
&\quad + \frac{1}{576} (-72g^4 \textcolor{red}{a}_1 + 92g^6 \textcolor{red}{a}_2 - 189g^8 \textcolor{red}{a}_3) \\
&\quad \quad \epsilon^{\alpha\beta} \eta_{kl} \left( \sigma \Lambda^{ln} \right)^{o\zeta} \Lambda^k \beta \theta^4 \partial_n (D_\alpha \Phi) \partial_o (D_\zeta \Phi) \Phi^+ \Phi^+ \\
&\quad + \frac{1}{1152} (-36g^4 \textcolor{red}{a}_1 + 92g^6 \textcolor{red}{a}_2 - 167g^8 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
&\quad + \frac{1}{2304} (76g^6 \textcolor{red}{a}_2 - 145g^8 \textcolor{red}{a}_3) \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \Phi^+
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{288} (-36g^4 \textcolor{red}{a}_1 + 57g^6 \textcolor{red}{a}_2 - 106g^8 \textcolor{red}{a}_3) \\
& \quad \epsilon^{\alpha\beta} \eta_{kl} \left( \sigma \Lambda^{ln} \right)^{\circ\zeta} \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \partial_n \partial_o (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{1152} (36g^6 \textcolor{red}{a}_2 - 61g^8 \textcolor{red}{a}_3) \left( \eta \sigma \Lambda^\kappa \right)^l \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2304} (4g^6 \textcolor{red}{a}_2 - 23g^8 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \eta_{kl} \left( \eta \sigma \Lambda^l \right)^\zeta \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \square (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{576} (6g^6 \textcolor{red}{a}_2 - 23g^8 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 (D_\alpha \Phi) \partial_k \partial_o (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + \left( \frac{3g^4 \textcolor{red}{a}_1}{32} - \frac{g^6 \textcolor{red}{a}_2}{9} + \frac{13g^8 \textcolor{red}{a}_3}{64} \right) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{4608} i (-4g^6 \textcolor{red}{a}_2 + 23g^8 \textcolor{red}{a}_3) \eta_{kl} \left( \bar{\sigma}^l \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda^\kappa{}^n)^k \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{4608} i (-4g^6 \textcolor{red}{a}_2 + 23g^8 \textcolor{red}{a}_3) \eta_{kl} \left( \bar{\sigma}^l \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda^\kappa{}^n)^k \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{4608} i (-4g^6 \textcolor{red}{a}_2 + 23g^8 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{np} \eta_{oq} \Lambda^\rho{}_\beta \Lambda^q{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{1152} (28g^6 \textcolor{red}{a}_2 + 23g^8 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_o (D_\beta \Phi) \Phi^+ \Phi^+ \\
& - \frac{1}{2304} i (36g^4 \textcolor{red}{a}_1 - 52g^6 \textcolor{red}{a}_2 + 83g^8 \textcolor{red}{a}_3) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+)
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{2304} i (36g^4 a_1 - 52g^6 a_2 + 83g^8 a_3) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{1152} (72g^4 a_1 - 76g^6 a_2 + 151g^8 a_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi \partial_k \partial_l (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2304} (72g^4 a_1 - 76g^6 a_2 + 151g^8 a_3) \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{576} (72g^4 a_1 - 76g^6 a_2 + 151g^8 a_3) \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2304} (144g^4 a_1 - 140g^6 a_2 + 233g^8 a_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \partial_k \Phi \partial_l (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{1152} (144g^4 a_1 - 140g^6 a_2 + 233g^8 a_3) \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2304} (144g^4 a_1 - 180g^6 a_2 + 317g^8 a_3) \Lambda^{kl} \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{4608} i (144g^4 a_1 - 220g^6 a_2 + 401g^8 a_3) \\
& \quad \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& - \frac{1}{4608} i (144g^4 a_1 - 220g^6 a_2 + 401g^8 a_3) \\
& \quad \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{2304} (144g^4 a_1 - 220g^6 a_2 + 401g^8 a_3)
\end{aligned}$$

$$\begin{aligned}
& \epsilon^{\alpha\beta}\epsilon^{\zeta\iota}\Lambda^k{}_\beta\Lambda^l{}_\iota\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\zeta\Phi)\Phi^+\Phi^+ \\
& + \frac{1}{4608}(288g^4\textcolor{red}{a}_1 - 588g^6\textcolor{red}{a}_2 + 1069g^8\textcolor{red}{a}_3) \\
& \quad \epsilon^{\alpha\beta}\Lambda^{kl}\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\beta\Phi)\Phi^+\Phi^+ \\
& + \frac{1}{9216}g^6((-68\Lambda^2 + 152\sigma\Lambda\Lambda)\textcolor{red}{a}_2 + g^2(521\Lambda^2 - 542\sigma\Lambda\Lambda)\textcolor{red}{a}_3) \\
& \quad \eta^{kl}\epsilon^{\alpha\beta}\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\beta\Phi)\Phi^+\Phi^+ \\
& + \frac{1}{9216}g^4(144\Lambda^2\textcolor{red}{a}_1 - 36g^2(5\Lambda^2 - 2\sigma\Lambda\Lambda)\textcolor{red}{a}_2 + g^4(673\Lambda^2 - 418\sigma\Lambda\Lambda)\textcolor{red}{a}_3) \\
& \quad \theta^4\Box\Phi(D^2\Phi)\Phi^+\Phi^+ \\
& + \frac{1}{8192}g^4(16\Lambda^2\textcolor{red}{a}_1 - 4g^2(5\Lambda^2 - 2\sigma\Lambda\Lambda)\textcolor{red}{a}_2 + 5g^4(11\Lambda^2 - 6\sigma\Lambda\Lambda)\textcolor{red}{a}_3) \\
& \quad \epsilon^{\dot{\alpha}\dot{\beta}}\theta^4(D^2\Phi)(D^2\Phi)(\bar{D}_{\dot{\alpha}}\Phi^+)\left(\bar{D}_{\dot{\beta}}\Phi^+\right) \\
& + \frac{1}{24576}g^4(48\Lambda^2\textcolor{red}{a}_1 - 8g^2(15\Lambda^2 + 2\sigma\Lambda\Lambda)\textcolor{red}{a}_2 + 3g^4(127\Lambda^2 + 18\sigma\Lambda\Lambda)\textcolor{red}{a}_3) \\
& \quad \theta^4(D^2\Phi)(D^2\Phi)\Phi^+(\bar{D}^2\Phi^+) \\
& + \frac{1}{1152}g^4(-36\Lambda^2\textcolor{red}{a}_1 - 2g^2(\Lambda^2 + 20\sigma\Lambda\Lambda)\textcolor{red}{a}_2 + 5g^4(5\Lambda^2 + 19\sigma\Lambda\Lambda)\textcolor{red}{a}_3) \\
& \quad \epsilon^{\alpha\beta}\theta^4(D_\alpha\Phi)(D_\beta\Phi)\Phi^+\Box\Phi^+ \\
& + \frac{1}{9216}g^6(4(37\Lambda^2 + 4\sigma\Lambda\Lambda)\textcolor{red}{a}_2 - g^2(333\Lambda^2 + 136\sigma\Lambda\Lambda)\textcolor{red}{a}_3)
\end{aligned}$$

$$\begin{aligned}
& \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{4608} (148g^6 \Lambda^2 \textcolor{red}{a}_2 + g^8 (-689\Lambda^2 + 252\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \\
& \quad \left( \sigma^{kl} \right)^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{18432} i (288g^4 \Lambda^2 \textcolor{red}{a}_1 + g^6 ((-508\Lambda^2 + 136\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (1679\Lambda^2 - 746\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
& \quad \left( \bar{\sigma}^k \right)^{\dot{\alpha}\dot{\beta}} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{18432} i (288g^4 \Lambda^2 \textcolor{red}{a}_1 + g^6 (-4 (53\Lambda^2 - 38\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (301\Lambda^2 - 334\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
& \quad \left( \bar{\sigma}^k \right)^{\dot{\alpha}\dot{\beta}} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{9216} (288g^4 \Lambda^2 \textcolor{red}{a}_1 + g^6 (-4 (73\Lambda^2 + 2\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (469\Lambda^2 + 2\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
& \quad \eta^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{1152} (36g^4 \Lambda^2 \textcolor{red}{a}_1 + g^6 ((-43\Lambda^2 + 10\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (137\Lambda^2 + 13\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
& \quad \theta^4 \Phi (D^2 \Phi) \Phi^+ \square \Phi^+ \\
& + \frac{1}{2304} (36g^4 \Lambda^2 \textcolor{red}{a}_1 - g^6 (4 (2\Lambda^2 - 5\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (4\Lambda^2 + 53\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
& \quad \theta^4 \Phi \square (D^2 \Phi) \Phi^+ \Phi^+,
\end{aligned}$$

$$\begin{aligned}
f_{22} &= \frac{1}{9216} g^4 m^2 (20 (\Lambda^2 + 2\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (47\Lambda^2 - 158\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi \square (D^2 \Phi) \\
&\quad + \frac{1}{9216} g^4 m^2 (20 (\Lambda^2 + 2\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (47\Lambda^2 - 158\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi), \\
f_{23} &= \frac{1}{768} ig^4 m^3 (12\Lambda^2 \textcolor{red}{a}_2 - g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
&\quad + \frac{1}{384} g^4 m^3 (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi \square \Phi^+ \\
&\quad + \frac{1}{6144} g^4 m^3 (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) (\bar{D}^2 \Phi^+), \\
f_{24} &= \frac{1}{128} ig^5 m^2 (12\Lambda^2 \textcolor{red}{a}_2 - g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
&\quad + \frac{1}{64} g^5 m^2 (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi \Phi^+ \square \Phi^+ \\
&\quad + \frac{1}{1024} g^5 m^2 (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \Phi^+ (\bar{D}^2 \Phi^+), \\
f_{25} &= \frac{1}{64} ig^6 m (12\Lambda^2 \textcolor{red}{a}_2 - g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
&\quad + \frac{1}{32} g^6 m (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi \Phi^+ \Phi^+ \square \Phi^+ \\
&\quad + \frac{1}{512} g^6 m (-12\Lambda^2 \textcolor{red}{a}_2 + g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ (\bar{D}^2 \Phi^+), \\
f_{26} &= \frac{1}{96} ig^7 (12\Lambda^2 \textcolor{red}{a}_2 - g^2 (69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+)
\end{aligned}$$

$$+\frac{1}{768}g^7(-12\Lambda^2 \textcolor{red}{a}_2 + g^2(69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3)\theta^4(D^2\Phi)\Phi^+\Phi^+\Phi^+(\bar{D}^2\Phi^+)$$

$$+\left(-\frac{1}{4}g^7\Lambda^2 \textcolor{red}{a}_2 + \frac{1}{48}g^9(69\Lambda^2 + 14\sigma\Lambda\Lambda) \textcolor{red}{a}_3\right)\theta^4\Phi\Phi^+\Phi^+\Phi^+\square\Phi^+,$$

$$f_{27} = \frac{1}{110592}g^5(-72(4\Lambda^2 - \sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2(287\Lambda^2 - 398\sigma\Lambda\Lambda) \textcolor{red}{a}_3)$$

$$\theta^4\Phi(D^2\Phi)\square(D^2\Phi)$$

$$+\frac{1}{36864}g^5(-72\Lambda^2 \textcolor{red}{a}_2 + g^2(107\Lambda^2 - 74\sigma\Lambda\Lambda) \textcolor{red}{a}_3)$$

$$\eta^{kl}\theta^4\Phi\partial_k(D^2\Phi)\partial_l(D^2\Phi)$$

$$-\frac{1}{27648}g^5(36(\Lambda^2 - \sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2(17\Lambda^2 + 88\sigma\Lambda\Lambda) \textcolor{red}{a}_3)$$

$$\epsilon^{\alpha\beta}\theta^4(D_\beta\Phi)\square(D_\alpha\Phi)(D^2\Phi)$$

$$+\frac{1}{110592}g^5(-72(\Lambda^2 + 2\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2(389\Lambda^2 + 130\sigma\Lambda\Lambda) \textcolor{red}{a}_3)$$

$$\eta^{kl}\epsilon^{\alpha\beta}\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\beta\Phi)(D^2\Phi),$$

$$f_{28} = \frac{1}{2304}(9g^5 \textcolor{red}{a}_2 - 13g^7 \textcolor{red}{a}_3)\left(\eta\sigma\Lambda\Lambda^k\right)^l\theta^4\Phi\partial_k(D^2\Phi)\partial_l(D^2\Phi)$$

$$-\frac{3}{256}(-2g^5 \textcolor{red}{a}_2 + 3g^7 \textcolor{red}{a}_3)\epsilon^{\alpha\beta}\eta_{kl}\left(\sigma\Lambda^{ln}\right)^{o\zeta}\Lambda^k{}_\beta\theta^4\partial_n(D_\alpha\Phi)\partial_o(D_\zeta\Phi)(D^2\Phi)$$

$$+\frac{1}{6912}5(-18g^5 \textcolor{red}{a}_2 + 23g^7 \textcolor{red}{a}_3)\epsilon^{\alpha\beta}\left(\eta\sigma\Lambda\Lambda^k\right)^l\theta^4(D_\beta\Phi)\partial_k\partial_l(D_\alpha\Phi)(D^2\Phi)$$

$$\begin{aligned}
& + \frac{1}{13824} (-36g^5 \textcolor{red}{a}_2 + 37g^7 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi (D^2 \Phi) \partial_k \partial_l (D^2 \Phi) \\
& + \frac{1}{13824} (-396g^5 \textcolor{red}{a}_2 + 551g^7 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) (D^2 \Phi),
\end{aligned}$$

$$\begin{aligned}
f_{29} = & \frac{1}{13824} 5 (-18g^5 \textcolor{red}{a}_2 + 23g^7 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) (D^2 \Phi) \\
& + \frac{1}{3072} (-192g \textcolor{red}{a}_0 - 36g^5 \textcolor{red}{a}_2 + 55g^7 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\zeta \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\
& + \frac{1}{4608} (-144g \textcolor{red}{a}_0 - 45g^5 \textcolor{red}{a}_2 + 68g^7 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
& + \frac{1}{27648} (-864g \textcolor{red}{a}_0 - 360g^5 \textcolor{red}{a}_2 + 523g^7 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \\
& + \frac{1}{55296} (-3456g \textcolor{red}{a}_0 - 504g^5 \textcolor{red}{a}_2 + 851g^7 \textcolor{red}{a}_3) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi),
\end{aligned}$$

$$f_{30} = \frac{1}{2048} g^3 m^5 (3\Lambda^2 + 2\sigma \Lambda \Lambda) (-10 \textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 (D^2 \Phi),$$

$$f_{31} = -\frac{g \textcolor{red}{a}_0}{3} (\sigma \Lambda \Lambda^{kl})^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+,$$

$$f_{32} = -\frac{37g^7 \Lambda^2 \textcolor{red}{a}_3}{6144} (\sigma^{kl})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi),$$

$$f_{33} = \frac{7g^7 \textcolor{red}{a}_3}{54} \eta^{kl} (\eta \sigma \Lambda \Lambda^n)^o \theta^4 \Phi^+ \partial_l \partial_n \Phi^+ \partial_k \partial_o \Phi^+,$$

$$f_{34} = \frac{1}{192} g^8 m \textcolor{red}{a}_3 (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+,$$

$$\begin{aligned}
f_{35} &= \frac{1}{576} g^8 m a_3 \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi^+ \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+, \\
f_{36} &= \frac{g^7 a_3}{1536} \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_o (D_\beta \Phi) (D^2 \Phi), \\
f_{37} &= -\frac{ig^7 a_3}{6144} \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{np} \eta_{oq} \Lambda^p{}_\beta \Lambda^q{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi), \\
f_{38} &= \frac{1}{2048} g^4 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2a_2 + 15g^2 a_3) \theta^4 (D^2 \Phi) (D^2 \Phi), \\
f_{39} &= \frac{1}{128} g^4 m^3 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2a_2 + 15g^2 a_3) \theta^4 \Phi^+ \square \Phi^+, \\
f_{40} &= \frac{1}{1024} g^5 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2a_2 + 15g^2 a_3) \theta^4 (D^2 \Phi) (D^2 \Phi) \Phi^+, \\
f_{41} &= \frac{1}{64} g^5 m^2 (3\Lambda^2 + 2\sigma\Lambda\Lambda) (-2a_2 + 15g^2 a_3) \theta^4 \Phi^+ \Phi^+ \square \Phi^+, \\
f_{42} &= \frac{1}{27648} 5g^4 m (-18a_2 + 23g^2 a_3) \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \partial_k \partial_l (D^2 \Phi), \\
f_{43} &= \frac{1}{1728} 5g^4 m (-18a_2 + 23g^2 a_3) \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi^+ \square \partial_k \partial_l \Phi^+, \\
f_{44} &= \frac{1}{55296} 5g^4 m (-18a_2 + 23g^2 a_3) \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_l \partial_k (D^2 \Phi), \\
f_{45} &= \frac{1}{3456} 5g^4 m (-18a_2 + 23g^2 a_3) \Lambda^{kl} \theta^4 \Phi^+ \square \partial_k \partial_l \Phi^+,
\end{aligned}$$

$$f_{46} = \frac{1}{1728} g^5 \Lambda^2 (9 \textcolor{red}{a}_2 + 32g^2 \textcolor{red}{a}_3) \eta^{kl} \eta^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+,$$

$$f_{47} = \frac{1}{96} g^6 m (-21 \textcolor{red}{a}_2 + 47g^2 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+,$$

$$f_{48} = \frac{1}{288} g^6 m (-21 \textcolor{red}{a}_2 + 47g^2 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+,$$

$$f_{49} = \frac{1}{1024} 3g^4 m^4 (3\Lambda^2 + 2\sigma \Lambda \Lambda) (-10 \textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \Phi^+,$$

$$f_{50} = \frac{3}{512} g^5 m^3 (3\Lambda^2 + 2\sigma \Lambda \Lambda) (-10 \textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+,$$

$$f_{51} = \frac{1}{256} g^6 m^2 (3\Lambda^2 + 2\sigma \Lambda \Lambda) (-10 \textcolor{red}{a}_2 + 71g^2 \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+,$$

$$f_{52} = \frac{1}{864} g^5 (-54 \textcolor{red}{a}_2 + 143g^2 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi^+ \square \Phi^+ \partial_k \partial_l \Phi^+,$$

$$f_{53} = \frac{1}{1152} g^3 m (72 \textcolor{red}{a}_1 - 76g^2 \textcolor{red}{a}_2 + 151g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+,$$

$$f_{54} = \frac{1}{2304} g^3 m (72 \textcolor{red}{a}_1 - 76g^2 \textcolor{red}{a}_2 + 151g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+,$$

$$f_{55} = \frac{1}{1152} g^2 m^2 (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D^2 \Phi) \partial_k \partial_l \Phi^+,$$

$$f_{56} = \frac{1}{2304} g^2 m^2 (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_k \partial_l \Phi^+,$$

$$f_{57} = \frac{1}{576} g^3 m (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+,$$

$$\begin{aligned}
f_{58} &= \frac{1}{1152} g^3 m (72 \textcolor{red}{a}_1 - 96g^2 \textcolor{red}{a}_2 + 193g^4 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+, \\
f_{59} &= \frac{1}{192} (-2g^2 \textcolor{red}{a}_1 + g^6 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 (D^2 \Phi) \square \partial_k \partial_l \Phi^+, \\
f_{60} &= \frac{1}{384} (-2g^2 \textcolor{red}{a}_1 + g^6 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 (D^2 \Phi) \square \partial_k \partial_l \Phi^+, \\
f_{61} &= \frac{1}{432} (-9g^5 \textcolor{red}{a}_2 - 35g^7 \textcolor{red}{a}_3) (\eta \sigma \Lambda \Lambda^k)^l \theta^4 \Phi^+ \Phi^+ \square \partial_k \partial_l \Phi^+, \\
f_{62} &= \left( \frac{g \textcolor{red}{a}_0}{6} + \frac{g^5 \textcolor{red}{a}_2}{96} - \frac{2g^7 \textcolor{red}{a}_3}{27} \right) \eta^{kl} \Lambda^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+, \\
f_{63} &= \left( -\frac{7}{384} g^5 \textcolor{red}{a}_2 + \frac{55g^7 \textcolor{red}{a}_3}{864} \right) \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \square \partial_k \partial_l \Phi^+, \\
f_{64} &= \frac{1}{1728} (-288g \textcolor{red}{a}_0 - 45g^5 \textcolor{red}{a}_2 + 23g^7 \textcolor{red}{a}_3) \Lambda^{kl} \theta^4 \Phi^+ \square \Phi^+ \partial_k \partial_l \Phi^+, \\
f_{65} &= \frac{1}{3456} g^5 (-45\Lambda^2 \textcolor{red}{a}_2 + g^2 (29\Lambda^2 - 60\sigma \Lambda \Lambda) \textcolor{red}{a}_3) \theta^4 \Phi^+ \square \Phi^+ \square \Phi^+, \\
f_{66} &= \frac{1}{384} g^6 m (2 (53\Lambda^2 - 12\sigma \Lambda \Lambda) \textcolor{red}{a}_2 + g^2 (68\Lambda^2 - 37\sigma \Lambda \Lambda) \textcolor{red}{a}_3) \eta^{kl} \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+, \\
f_{67} &= -\frac{1}{1536} g^2 (4\Lambda^2 \textcolor{red}{a}_1 + g^4 (\Lambda^2 + 2\sigma \Lambda \Lambda) \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \square \square \Phi^+, \\
f_{68} &= -\frac{1}{6912} g^5 (9 (\Lambda^2 - 4\sigma \Lambda \Lambda) \textcolor{red}{a}_2 + 2g^2 (55\Lambda^2 + 14\sigma \Lambda \Lambda) \textcolor{red}{a}_3) \theta^4 \Phi^+ \Phi^+ \square \square \Phi^+,
\end{aligned}$$

$$\begin{aligned}
f_{69} &= \frac{1}{1152} g^6 m ((34\Lambda^2 - 72\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + 19g^2 (32\Lambda^2 + 17\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi^+ \Phi^+ \Phi^+ \square \Phi^+, \\
f_{70} &= \frac{1}{2304} g^3 m (4 (9\Lambda^2 \textcolor{red}{a}_1 + g^2 (-2\Lambda^2 + 5\sigma\Lambda\Lambda) \textcolor{red}{a}_2) - g^4 (4\Lambda^2 + 53\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \\
&\quad \eta^{kl} \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+, \\
f_{71} &= -\frac{1}{110592} g^4 m (36 (\Lambda^2 - \sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (17\Lambda^2 + 88\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 (D^2 \Phi) \square (D^2 \Phi), \\
f_{72} &= -\frac{1}{6912} g^4 m (36 (\Lambda^2 - \sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (17\Lambda^2 + 88\sigma\Lambda\Lambda) \textcolor{red}{a}_3) \theta^4 \Phi^+ \square \square \Phi^+, \\
f_{73} &= \frac{1}{4608} g^2 m^2 (72\Lambda^2 \textcolor{red}{a}_1 + g^2 ((-51\Lambda^2 + 30\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (133\Lambda^2 - 40\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
&\quad \theta^4 (D^2 \Phi) \square \Phi^+, \\
f_{74} &= \frac{1}{2304} g^3 m (72\Lambda^2 \textcolor{red}{a}_1 + g^2 ((-51\Lambda^2 + 30\sigma\Lambda\Lambda) \textcolor{red}{a}_2 + g^2 (133\Lambda^2 - 40\sigma\Lambda\Lambda) \textcolor{red}{a}_3)) \\
&\quad \theta^4 (D^2 \Phi) \Phi^+ \square \Phi^+.
\end{aligned}$$

# Basis of Supersymmetry Invariant Subset

Based on the analysis made to the 74 supersymmetry invariant subsets, we try to construct more general  $1/2$  supersymmetry invariant subsets in order to deduce the one-loop renormalizable Wess-Zumino action on the BFNC superspace.

$$f_i = \sum_{j=1}^{n_i} C_{ij} L_j \quad \rightarrow \quad A_i \equiv \sum_{j=1}^{n_i} (x_{i,j} + y_{i,j} \Lambda^2 + z_{i,j} \sigma \Lambda \Lambda) L_j \quad \rightarrow \quad A'_i, \quad (i = 1, 2, \dots, 74)$$

$$\delta A'_i = \sum_{k=1}^{n'_i} G_{i,k}(x, y, z) L'_k, \quad (G_{i,k}(x, y, z) \sim x_{i,j}, y_{i,j}, z_{i,j})$$

$$\delta A'_i = 0 \quad \rightarrow \quad G_{i,k}(x, y, z) = 0, \quad (L'_k \text{ independent to each other})$$

$$A'_i \quad \rightarrow \quad B_i, \quad (\text{eliminate the dependent parameters})$$

We list the 74 bases  $B_i$ 's below, each of them is invariant under the 1/2 supersymmetry transformation.

$$\begin{aligned}
 B_1 &= (-\Lambda^2 y_{1,2} - \sigma \Lambda \Lambda z_{1,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \\
 &\quad + (\Lambda^2 y_{1,2} + \sigma \Lambda \Lambda z_{1,2}) \theta^4 \Phi (D^2 \Phi), \\
 B_2 &= (-2\Lambda^2 y_{2,2} - 2\sigma \Lambda \Lambda z_{2,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \\
 &\quad + (\Lambda^2 y_{2,2} + \sigma \Lambda \Lambda z_{2,2}) \theta^4 \Phi \Phi (D^2 \Phi), \\
 B_3 &= (-\Lambda^2 y_{3,2} - \sigma \Lambda \Lambda z_{3,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \\
 &\quad + (\Lambda^2 y_{3,2} + \sigma \Lambda \Lambda z_{3,2}) \theta^4 \Phi (D^2 \Phi) \Phi^+, \\
 B_4 &= (-2\Lambda^2 y_{4,2} - 2\sigma \Lambda \Lambda z_{4,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \\
 &\quad + (\Lambda^2 y_{4,2} + \sigma \Lambda \Lambda z_{4,2}) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+, \\
 B_5 &= (-\Lambda^2 y_{5,2} - \sigma \Lambda \Lambda z_{5,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \\
 &\quad + (\Lambda^2 y_{5,2} + \sigma \Lambda \Lambda z_{5,2}) \theta^4 \Phi (D^2 \Phi) \Phi^+ \Phi^+, \\
 B_6 &= (-2\Lambda^2 y_{6,2} - 2\sigma \Lambda \Lambda z_{6,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \\
 &\quad + (\Lambda^2 y_{6,2} + \sigma \Lambda \Lambda z_{6,2}) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+ \Phi^+, \\
 B_7 &= (-\Lambda^2 y_{7,2} - \sigma \Lambda \Lambda z_{7,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+ \\
 &\quad + (\Lambda^2 y_{7,2} + \sigma \Lambda \Lambda z_{7,2}) \theta^4 \Phi (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+, \\
 B_8 &= (-2\Lambda^2 y_{8,2} - 2\sigma \Lambda \Lambda z_{8,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+
 \end{aligned}$$

$$\begin{aligned}
& + (\Lambda^2 y_{8,2} + \sigma \Lambda \Lambda z_{8,2}) \theta^4 \Phi \Phi (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+, \\
B_9 &= (-\Lambda^2 y_{9,2} - \sigma \Lambda \Lambda z_{9,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \\
& + (\Lambda^2 y_{9,2} + \sigma \Lambda \Lambda z_{9,2}) \theta^4 \Phi (D^2 \Phi) (D^2 \Phi), \\
B_{10} &= (-2\Lambda^2 y_{10,2} - 2\sigma \Lambda \Lambda z_{10,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \\
& + (\Lambda^2 y_{10,2} + \sigma \Lambda \Lambda z_{10,2}) \theta^4 \Phi \Phi (D^2 \Phi) (D^2 \Phi), \\
B_{11} &= (-\Lambda^2 y_{11,2} - \sigma \Lambda \Lambda z_{11,2}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \Phi^+ \\
& + (\Lambda^2 y_{11,2} + \sigma \Lambda \Lambda z_{11,2}) \theta^4 \Phi (D^2 \Phi) (D^2 \Phi) \Phi^+, \\
B_{12} &= (-2\Lambda^2 y_{12,2} - 2\sigma \Lambda \Lambda z_{12,2}) \epsilon^{\alpha\beta} \theta^4 \Phi (D_\alpha \Phi) (D_\beta \Phi) (D^2 \Phi) \Phi^+ \\
& + (\Lambda^2 y_{12,2} + \sigma \Lambda \Lambda z_{12,2}) \theta^4 \Phi \Phi (D^2 \Phi) (D^2 \Phi) \Phi^+, \\
B_{13} &= (-8i\Lambda^2 y_{13,3} - 8i\sigma \Lambda \Lambda z_{13,3}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\dot{\beta}} \theta^4 (D_\beta \Phi) \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (16\Lambda^2 y_{13,3} + 16\sigma \Lambda \Lambda z_{13,3}) \eta^{kl} \theta^4 \Phi \partial_k \Phi^+ \partial_l \Phi^+ \\
& + (\Lambda^2 y_{13,3} + \sigma \Lambda \Lambda z_{13,3}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \left( \bar{D}_{\dot{\beta}} \Phi^+ \right), \\
B_{14} &= (-8i\Lambda^2 y_{14,3} - 8i\sigma \Lambda \Lambda z_{14,3}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\dot{\beta}} \theta^4 (D_\beta \Phi) \Phi^+ \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (16\Lambda^2 y_{14,3} + 16\sigma \Lambda \Lambda z_{14,3}) \eta^{kl} \theta^4 \Phi \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+ \\
& + (\Lambda^2 y_{14,3} + \sigma \Lambda \Lambda z_{14,3}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \left( \bar{D}_{\dot{\beta}} \Phi^+ \right),
\end{aligned}$$

$$\begin{aligned}
B_{15} &= (-8i\Lambda^2 y_{15,3} - 8i\sigma\Lambda\Lambda z_{15,3}) \left(\bar{\sigma}^k\right)^{\dot{\alpha}\beta} \theta^4 (D_\beta\Phi) \Phi^+ \Phi^+ \partial_k \Phi^+ (\bar{D}_{\dot{\alpha}}\Phi^+) \\
&\quad + (16\Lambda^2 y_{15,3} + 16\sigma\Lambda\Lambda z_{15,3}) \eta^{kl} \theta^4 \Phi \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+ \\
&\quad + (\Lambda^2 y_{15,3} + \sigma\Lambda\Lambda z_{15,3}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2\Phi) \Phi^+ \Phi^+ (\bar{D}_{\dot{\alpha}}\Phi^+) \left(\bar{D}_{\dot{\beta}}\Phi^+\right),
\end{aligned}$$

$$\begin{aligned}
B_{16} &= x_{16,2} \left(\eta\sigma\Lambda\Lambda^k\right)' \theta^4 \Phi \partial_k \partial_l (D^2\Phi) \\
&\quad + x_{16,2} \epsilon^{\alpha\beta} \left(\eta\sigma\Lambda\Lambda^k\right)' \theta^4 (D_\beta\Phi) \partial_k \partial_l (D_\alpha\Phi),
\end{aligned}$$

$$\begin{aligned}
B_{17} &= (4x_{17,16} + x_{17,21} - 2x_{17,22} + x_{17,26} + 4z_{17,30} + 8iz_{17,34} - 2z_{17,35}) \\
&\quad \epsilon^{\alpha\beta} \left(\eta\sigma\Lambda^k\right)^\zeta \Lambda'{}_\beta \theta^4 (D_\alpha\Phi) \partial_k \partial_l (D_\zeta\Phi) \Phi^+ \\
&\quad + (x_{17,14} + 2x_{17,21} - 8z_{17,30} - 16iz_{17,34} + 4z_{17,35}) \\
&\quad \epsilon^{\alpha\beta} \left(\eta\sigma\Lambda^k\right)^\zeta \Lambda'{}_\beta \theta^4 \partial_k (D_\alpha\Phi) \partial_l (D_\zeta\Phi) \Phi^+ \\
&\quad + \left(iz_{17,30} - 2z_{17,34} - \frac{1}{2}iz_{17,35}\right) \\
&\quad \eta_{kl} \left(\bar{\sigma}^l\right)^{\dot{\alpha}\beta} (\eta\sigma\Lambda\Lambda^n)^k \theta^4 (D_\beta\Phi) \partial_n (D^2\Phi) (\bar{D}_{\dot{\alpha}}\Phi^+) \\
&\quad + \left(-iz_{17,30} + 2z_{17,34} + \frac{1}{2}iz_{17,35}\right) \\
&\quad \eta_{kl} \left(\bar{\sigma}^l\right)^{\dot{\alpha}\beta} (\eta\sigma\Lambda\Lambda^n)^k \theta^4 \partial_n (D_\beta\Phi) (D^2\Phi) (\bar{D}_{\dot{\alpha}}\Phi^+)
\end{aligned}$$

$$\begin{aligned}
& + (-2iz_{17,30} + 4z_{17,34} + iz_{17,35}) \\
& \quad \epsilon^{\alpha\beta}\epsilon^{\zeta\iota}\epsilon^{klno}\eta_{np}\eta_{oq}\Lambda^p{}_\beta\Lambda^q{}_\iota\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\zeta\Phi)\Phi^+ \\
& + (-x_{17,14} + 4x_{17,16} - x_{17,21} - 2x_{17,22} + 4z_{17,30} + 8iz_{17,34} - 2z_{17,35}) \\
& \quad \Lambda^{kl}\eta_{ln}(\sigma^{no})^{\alpha\beta}\theta^4\partial_k(D_\alpha\Phi)\partial_o(D_\beta\Phi)\Phi^+ \\
& + \left(-x_{17,8} + \frac{x_{17,21}}{2}\right)\epsilon^{\alpha\beta}\Lambda^{kl}\theta^4\partial_k(D_\alpha\Phi)\partial_l(D_\beta\Phi)\Phi^+ \\
& + x_{17,8}\Lambda^{kl}\theta^4\partial_l\Phi\partial_k(D^2\Phi)\Phi^+ \\
& + (-x_{17,16} + x_{17,22})\Lambda^{kl}\theta^4\partial_k\partial_l\Phi(D^2\Phi)\Phi^+ \\
& + \left(\frac{1}{2}ix_{17,16} - \frac{1}{4}ix_{17,22}\right)\Lambda^{kl}\eta_{ln}(\bar{\sigma}^n)^{\dot{\alpha}\beta}\theta^4(D_\beta\Phi)\partial_k(D^2\Phi)(\bar{D}_{\dot{\alpha}}\Phi^+) \\
& + \left(-\frac{1}{2}ix_{17,16} + \frac{1}{4}ix_{17,22}\right)\Lambda^{kl}\eta_{ln}(\bar{\sigma}^n)^{\dot{\alpha}\beta}\theta^4\partial_k(D_\beta\Phi)(D^2\Phi)(\bar{D}_{\dot{\alpha}}\Phi^+) \\
& + \left(\frac{x_{17,17}}{2} - x_{17,21} - 4z_{17,30} - 8iz_{17,34} + 2z_{17,35}\right) \\
& \quad \left(\eta\sigma\Lambda^k\right)^l\theta^4\partial_k\partial_l\Phi(D^2\Phi)\Phi^+ \\
& + (4x_{17,16} - x_{17,21} - 2x_{17,22} + x_{17,26} - 4z_{17,30} - 8iz_{17,34} + 2z_{17,35}) \\
& \quad \epsilon^{\alpha\beta}\eta_{kl}\left(\sigma\Lambda^{ln}\right)^{\alpha\zeta}\Lambda^k{}_\beta\theta^4(D_\alpha\Phi)\partial_n\partial_o(D_\zeta\Phi)\Phi^+ \\
& + x_{17,14}\epsilon^{\alpha\beta}\eta_{kl}\left(\sigma\Lambda^{ln}\right)^{\alpha\zeta}\Lambda^k{}_\beta\theta^4\partial_n(D_\alpha\Phi)\partial_o(D_\zeta\Phi)\Phi^+
\end{aligned}$$

$$\begin{aligned}
& + \frac{1}{2} x_{17,17} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi \partial_k \partial_l (D^2 \Phi) \Phi^+ \\
& + x_{17,16} \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \Phi^+ \\
& + x_{17,17} \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi) \Phi^+ \\
& + \left( -x_{17,21} + \frac{x_{17,24}}{2} + 4z_{17,30} + 8iz_{17,34} - 2z_{17,35} \right) \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \\
& + \frac{1}{4} (ix_{17,21}) \eta_{kl} \left( \bar{\sigma}' \right)^{\dot{\alpha}\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^n \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{4} (-ix_{17,21}) \eta_{kl} \left( \bar{\sigma}' \right)^{\dot{\alpha}\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^n \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + x_{17,21} \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\nu \theta^4 \partial_k (D_\alpha \Phi) \partial_\iota (D_\zeta \Phi) \Phi^+ \\
& + x_{17,22} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) \Phi^+ \\
& + \frac{1}{2} x_{17,24} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \partial_k \Phi \partial_l (D^2 \Phi) \Phi^+ \\
& + x_{17,24} \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) \Phi^+ \\
& + (-4z_{17,30} - 8iz_{17,34} + 2z_{17,35}) \epsilon^{\alpha\beta} \eta_{kl} \left( \eta \sigma \Lambda' \right)^\zeta \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \square (D_\zeta \Phi) \Phi^+ \\
& + x_{17,26} \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 (D_\alpha \Phi) \partial_k \partial_o (D_\beta \Phi) \Phi^+ \\
& + \left( \Lambda^2 \left( -2iy_{17,32} + \frac{y_{17,35}}{2} \right) + \sigma \Lambda \Lambda (z_{17,30} - 2iz_{17,32} + 2iz_{17,34}) \right)
\end{aligned}$$

$$\begin{aligned}
& \theta^4 \square \Phi (D^2 \Phi) \Phi^+ \\
& + \left( \Lambda^2 \left( -\frac{1}{16} iy_{17,32} - \frac{1}{16} iy_{17,34} \right) + \sigma \Lambda \Lambda \left( -\frac{1}{16} iz_{17,32} - \frac{1}{16} iz_{17,34} \right) \right) \\
& \quad \theta^4 (D^2 \Phi) (D^2 \Phi) (\bar{D}^2 \Phi^+) \\
& + (\Lambda^2 (4iy_{17,32} - 4iy_{17,34}) + \sigma \Lambda \Lambda (4z_{17,30} + 4iz_{17,32} + 4iz_{17,34} - 2z_{17,35})) \\
& \quad \left( \sigma^{kl} \right)^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \\
& + \left( \Lambda^2 \left( -2iy_{17,34} + \frac{y_{17,35}}{2} \right) + \sigma \Lambda \Lambda z_{17,30} \right) \theta^4 \Phi \square (D^2 \Phi) \Phi^+ \\
& + (\Lambda^2 (-2iy_{17,32} - y_{17,33} - 2iy_{17,34}) + \sigma \Lambda \Lambda (-2iz_{17,32} - z_{17,33} - 2iz_{17,34})) \\
& \quad \eta^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \\
& + (\Lambda^2 y_{17,32} + \sigma \Lambda \Lambda z_{17,32}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (\Lambda^2 y_{17,33} + \sigma \Lambda \Lambda z_{17,33}) \eta^{kl} \epsilon^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \\
& + (\Lambda^2 y_{17,34} + \sigma \Lambda \Lambda z_{17,34}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (\Lambda^2 y_{17,35} + \sigma \Lambda \Lambda z_{17,35}) \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi) \Phi^+, \\
B_{18} &= x_{18,2} \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \\
& + x_{18,2} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi),
\end{aligned}$$

$$\begin{aligned}
B_{19} &= -x_{19,2}\epsilon^{\alpha\beta}\left(\eta\sigma\Lambda\Lambda^k\right)^I\theta^4(D_\alpha\Phi)(D_\beta\Phi)\Phi^+\partial_k\partial_I\Phi^+ \\
&\quad +x_{19,2}\left(\eta\sigma\Lambda\Lambda^k\right)^I\theta^4\Phi(D^2\Phi)\Phi^+\partial_k\partial_I\Phi^+, \\
B_{20} &= -x_{20,2}\epsilon^{\alpha\beta}\Lambda^{kl}\theta^4(D_\alpha\Phi)(D_\beta\Phi)\Phi^+\partial_k\partial_l\Phi^+ \\
&\quad +x_{20,2}\Lambda^{kl}\theta^4\Phi(D^2\Phi)\Phi^+\partial_k\partial_l\Phi^+, \\
B_{21} &= (x_{21,10}+2x_{21,19}-2x_{21,23}+x_{21,26}+z_{21,34}-2iz_{21,35}+2iz_{21,36}) \\
&\quad \epsilon^{\alpha\beta}\left(\eta\sigma\Lambda^k\right)^\zeta\Lambda^I{}_\beta\theta^4(D_\alpha\Phi)\partial_k\partial_I(D_\zeta\Phi)\Phi^+\Phi^+ \\
&\quad +(-x_{21,15}+2x_{21,19}-2x_{21,23}+x_{21,26}-z_{21,34}+2iz_{21,35}-2iz_{21,36}) \\
&\quad \epsilon^{\alpha\beta}\left(\eta\sigma\Lambda^k\right)^\zeta\Lambda^I{}_\beta\theta^4\partial_k(D_\alpha\Phi)\partial_I(D_\zeta\Phi)\Phi^+\Phi^+ \\
&\quad +\left(\Lambda^2\left(-\frac{1}{2}iy_{21,32}-\frac{1}{2}iy_{21,38}\right)+\sigma\Lambda\Lambda\left(-\frac{1}{2}iz_{21,32}-\frac{1}{2}iz_{21,38}\right)\right) \\
&\quad \left(\bar{\sigma}^k\right)^{\dot{\alpha}\beta}\theta^4(D_\beta\Phi)(D^2\Phi)\Phi^+\partial_k(\bar{D}_{\dot{\alpha}}\Phi^+) \\
&\quad +(-x_{21,15}+2x_{21,19}-2x_{21,23}-x_{21,26}+z_{21,34}-2iz_{21,35}+2iz_{21,36}) \\
&\quad \epsilon^{\alpha\beta}\eta_{kl}\left(\sigma\Lambda^{ln}\right)^{o\zeta}\Lambda^k{}_\beta\theta^4\partial_n(D_\alpha\Phi)\partial_o(D_\zeta\Phi)\Phi^+\Phi^+ \\
&\quad +\left(\frac{x_{21,26}}{2}-x_{21,27}\right)\Lambda^{kl}\theta^4\partial_l\Phi\partial_k(D^2\Phi)\Phi^+\Phi^+ \\
&\quad +\left(\frac{x_{21,22}}{2}-x_{21,26}+z_{21,34}-2iz_{21,35}+2iz_{21,36}\right)
\end{aligned}$$

$$\begin{aligned}
& \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
& + (x_{21,10} + 2x_{21,19} - 2x_{21,23} - x_{21,26} - z_{21,34} + 2iz_{21,35} - 2iz_{21,36}) \\
& \quad \epsilon^{\alpha\beta} \eta_{kl} \left( \sigma \Lambda^{ln} \right)^{\alpha\zeta} \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \partial_n \partial_o (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + \left( \frac{x_{21,20}}{2} - x_{21,26} - z_{21,34} + 2iz_{21,35} - 2iz_{21,36} \right) \\
& \quad \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \Phi^+ \\
& + (-z_{21,34} + 2iz_{21,35} - 2iz_{21,36}) \epsilon^{\alpha\beta} \eta_{kl} \left( \eta \sigma \Lambda^l \right)^\zeta \Lambda^k{}_\beta \theta^4 (D_\alpha \Phi) \square (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + x_{21,10} \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 (D_\alpha \Phi) \partial_k \partial_o (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + (x_{21,19} + x_{21,23}) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \left( \frac{1}{2} iz_{21,34} + z_{21,35} - z_{21,36} \right) \\
& \quad \eta_{kl} \left( \bar{\sigma}^l \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^n)^k \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \left( -\frac{1}{2} iz_{21,34} - z_{21,35} + z_{21,36} \right) \\
& \quad \eta_{kl} \left( \bar{\sigma}^l \right)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^n)^k \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \left( -\frac{1}{2} iz_{21,34} - z_{21,35} + z_{21,36} \right)
\end{aligned}$$

$$\begin{aligned}
& \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{np} \eta_{oq} \Lambda^p{}_\beta \Lambda^q{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \Phi^+ \\
& + x_{21,15} \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_o (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + \left( \frac{1}{2} i x_{21,19} - \frac{1}{2} i x_{21,23} \right) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \left( -\frac{1}{2} i x_{21,19} + \frac{1}{2} i x_{21,23} \right) \Lambda^{kl} \eta_{ln} (\bar{\sigma}^n)^{\dot{\alpha}\beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{2} x_{21,20} (\eta \sigma \Lambda \Lambda^k)' \theta^4 \Phi \partial_k \partial_l (D^2 \Phi) \Phi^+ \Phi^+ \\
& + x_{21,19} \Lambda^{kl} \theta^4 \Phi \partial_l \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
& + x_{21,20} \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)' \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2} x_{21,22} (\eta \sigma \Lambda \Lambda^k)' \theta^4 \partial_k \Phi \partial_l (D^2 \Phi) \Phi^+ \Phi^+ \\
& + x_{21,22} \epsilon^{\alpha\beta} (\eta \sigma \Lambda \Lambda^k)' \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + x_{21,23} \Lambda^{kl} \theta^4 \partial_k \partial_l \Phi (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \frac{1}{2} (i x_{21,26}) \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 (D_\beta \Phi) \partial_n (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \frac{1}{2} (-i x_{21,26}) \eta_{kl} (\bar{\sigma}^l)^{\dot{\alpha}\beta} (\eta \sigma \Lambda \Lambda^k)^n \theta^4 \partial_n (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + x_{21,26} \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^l{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) \Phi^+ \Phi^+
\end{aligned}$$

$$\begin{aligned}
& + x_{21,27} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + (\Lambda^2 (-iy_{21,35} - iy_{21,36} - y_{21,37}) + \sigma \Lambda \Lambda (-iz_{21,35} - iz_{21,36} - z_{21,37})) \\
& \quad \eta^{kl} \epsilon^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \Phi^+ \\
& + (\Lambda^2 (-iy_{21,35} + iy_{21,36} + y_{21,39}) + \sigma \Lambda \Lambda (-iz_{21,35} + iz_{21,36} + z_{21,39})) \\
& \quad \theta^4 \square \Phi (D^2 \Phi) \Phi^+ \Phi^+ \\
& + \left( \Lambda^2 \left( -\frac{1}{16} iy_{21,35} - \frac{1}{16} iy_{21,36} \right) + \sigma \Lambda \Lambda \left( -\frac{1}{16} iz_{21,35} - \frac{1}{16} iz_{21,36} \right) \right) \\
& \quad \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (D^2 \Phi) (D^2 \Phi) (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+) \\
& + \left( \Lambda^2 \left( \frac{y_{21,32}}{16} - \frac{1}{16} iy_{21,35} - \frac{1}{16} iy_{21,36} + \frac{y_{21,38}}{16} \right) \right. \\
& \quad \left. + \sigma \Lambda \Lambda \left( \frac{z_{21,32}}{16} - \frac{1}{16} iz_{21,35} - \frac{1}{16} iz_{21,36} + \frac{z_{21,38}}{16} \right) \right) \\
& \quad \theta^4 (D^2 \Phi) (D^2 \Phi) \Phi^+ (\bar{D}^2 \Phi^+) \\
& + (\Lambda^2 y_{21,32} + \sigma \Lambda \Lambda z_{21,32}) \epsilon^{\alpha\beta} \theta^4 (D_\alpha \Phi) (D_\beta \Phi) \Phi^+ \square \Phi^+ \\
& + \left( \Lambda^2 (2iy_{21,36} + 2y_{21,39}) + \sigma \Lambda \Lambda \left( -\frac{z_{21,34}}{2} + iz_{21,35} + iz_{21,36} + 2z_{21,39} \right) \right) \\
& \quad \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi) \Phi^+ \Phi^+ \\
& + (\Lambda^2 (2iy_{21,35} - 2iy_{21,36}) + \sigma \Lambda \Lambda z_{21,34}) \left( \sigma^{kl} \right)^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) \Phi^+ \Phi^+
\end{aligned}$$

$$\begin{aligned}
& + (\Lambda^2 y_{21,35} + \sigma \Lambda \Lambda z_{21,35}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 \partial_k (D_\beta \Phi) (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (\Lambda^2 y_{21,36} + \sigma \Lambda \Lambda z_{21,36}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (D^2 \Phi) \Phi^+ (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (\Lambda^2 y_{21,37} + \sigma \Lambda \Lambda z_{21,37}) \eta^{kl} \theta^4 \partial_l \Phi \partial_k (D^2 \Phi) \Phi^+ \Phi^+ \\
& + (\Lambda^2 y_{21,38} + \sigma \Lambda \Lambda z_{21,38}) \theta^4 \Phi (D^2 \Phi) \Phi^+ \square \Phi^+ \\
& + (\Lambda^2 y_{21,39} + \sigma \Lambda \Lambda z_{21,39}) \theta^4 \Phi \square (D^2 \Phi) \Phi^+ \Phi^+,
\end{aligned}$$

$$\begin{aligned}
B_{22} = & (\Lambda^2 y_{22,2} + \sigma \Lambda \Lambda z_{22,2}) \theta^4 \Phi \square (D^2 \Phi) \\
& + (\Lambda^2 y_{22,2} + \sigma \Lambda \Lambda z_{22,2}) \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi),
\end{aligned}$$

$$\begin{aligned}
B_{23} = & (-8i\Lambda^2 y_{23,3} - 8i\sigma \Lambda \Lambda z_{23,3}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (16\Lambda^2 y_{23,3} + 16\sigma \Lambda \Lambda z_{23,3}) \theta^4 \Phi \square \Phi^+ \\
& + (\Lambda^2 y_{23,3} + \sigma \Lambda \Lambda z_{23,3}) \theta^4 (D^2 \Phi) (\bar{D}^2 \Phi^+),
\end{aligned}$$

$$\begin{aligned}
B_{24} = & (-8i\Lambda^2 y_{24,3} - 8i\sigma \Lambda \Lambda z_{24,3}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (16\Lambda^2 y_{24,3} + 16\sigma \Lambda \Lambda z_{24,3}) \theta^4 \Phi \Phi^+ \square \Phi^+ \\
& + (\Lambda^2 y_{24,3} + \sigma \Lambda \Lambda z_{24,3}) \theta^4 (D^2 \Phi) \Phi^+ (\bar{D}^2 \Phi^+),
\end{aligned}$$

$$\begin{aligned}
B_{25} = & (-8i\Lambda^2 y_{25,3} - 8i\sigma \Lambda \Lambda z_{25,3}) \left( \bar{\sigma}^k \right)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + (16\Lambda^2 y_{25,3} + 16\sigma \Lambda \Lambda z_{25,3}) \theta^4 \Phi \Phi^+ \Phi^+ \square \Phi^+
\end{aligned}$$

$$\begin{aligned}
& + (\Lambda^2 y_{25,3} + \sigma \Lambda \Lambda z_{25,3}) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ (\bar{D}^2 \Phi^+) , \\
B_{26} = & \left( -\frac{1}{2} i \Lambda^2 y_{26,3} - \frac{1}{2} i \sigma \Lambda \Lambda z_{26,3} \right) (\bar{\sigma}^k)^{\dot{\alpha}\beta} \theta^4 (D_\beta \Phi) \Phi^+ \Phi^+ \Phi^+ \partial_k (\bar{D}_{\dot{\alpha}} \Phi^+) \\
& + \left( \frac{1}{16} \Lambda^2 y_{26,3} + \frac{1}{16} \sigma \Lambda \Lambda z_{26,3} \right) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+ (\bar{D}^2 \Phi^+) \\
& + (\Lambda^2 y_{26,3} + \sigma \Lambda \Lambda z_{26,3}) \theta^4 \Phi \Phi^+ \Phi^+ \Phi^+ \square \Phi^+ , \\
B_{27} = & \left( \Lambda^2 \left( \frac{3y_{27,3}}{2} + y_{27,4} \right) + \sigma \Lambda \Lambda \left( \frac{3z_{27,3}}{2} + z_{27,4} \right) \right) \theta^4 \Phi (D^2 \Phi) \square (D^2 \Phi) \\
& + (\Lambda^2 (y_{27,3} + y_{27,4}) + \sigma \Lambda \Lambda (z_{27,3} + z_{27,4})) \eta^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
& + (\Lambda^2 y_{27,3} + \sigma \Lambda \Lambda z_{27,3}) \epsilon^{\alpha\beta} \theta^4 (D_\beta \Phi) \square (D_\alpha \Phi) (D^2 \Phi) \\
& + (\Lambda^2 y_{27,4} + \sigma \Lambda \Lambda z_{27,4}) \eta^{kl} \epsilon^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi) , \\
B_{28} = & \left( -\frac{x_{28,3}}{2} + x_{28,4} \right) \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
& + (3x_{28,3} - 2x_{28,4} - 2x_{28,5}) \epsilon^{\alpha\beta} \eta_{kl} \left( \sigma \Lambda^{ln} \right)^{o\zeta} \Lambda^k{}_\beta \theta^4 \partial_n (D_\alpha \Phi) \partial_o (D_\zeta \Phi) (D^2 \Phi) \\
& + x_{28,3} \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 (D_\beta \Phi) \partial_k \partial_l (D_\alpha \Phi) (D^2 \Phi) \\
& + x_{28,4} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \Phi (D^2 \Phi) \partial_k \partial_l (D^2 \Phi) \\
& + x_{28,5} \epsilon^{\alpha\beta} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \partial_k (D_\beta \Phi) \partial_l (D_\alpha \Phi) (D^2 \Phi) ,
\end{aligned}$$

$$\begin{aligned}
B_{29} &= (-2x_{29,3} + 2x_{29,4}) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) (D^2 \Phi) \\
&\quad + (-6x_{29,3} + 4x_{29,4} + 2x_{29,5}) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\nu \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\
&\quad + x_{29,3} \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
&\quad + x_{29,4} \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \\
&\quad + x_{29,5} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi), \\
B_{30} &= (\Lambda^2 y_{30,1} + \sigma \Lambda \Lambda z_{30,1}) \theta^4 (D^2 \Phi), \\
B_{31} &= x_{31,1} \left( \sigma \Lambda \Lambda^{kl} \right)^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+, \\
B_{32} &= (\Lambda^2 y_{32,1} + \sigma \Lambda \Lambda z_{32,1}) \left( \sigma^{kl} \right)^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi), \\
B_{33} &= x_{33,1} \eta^{kl} (\eta \sigma \Lambda \Lambda^n)^o \theta^4 \Phi^+ \partial_l \partial_n \Phi^+ \partial_k \partial_o \Phi^+, \\
B_{34} &= x_{34,1} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+, \\
B_{35} &= x_{35,1} \left( \eta \sigma \Lambda \Lambda^k \right)^l \theta^4 \Phi^+ \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+, \\
B_{36} &= x_{36,1} \Lambda^{kl} \eta_{ln} (\sigma^{no})^{\alpha\beta} \theta^4 \partial_k (D_\alpha \Phi) \partial_o (D_\beta \Phi) (D^2 \Phi), \\
B_{37} &= x_{37,1} \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \epsilon^{klno} \eta_{np} \eta_{oq} \Lambda^p{}_\beta \Lambda^q{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi), \\
B_{38} &= (\Lambda^2 y_{38,1} + \sigma \Lambda \Lambda z_{38,1}) \theta^4 (D^2 \Phi) (D^2 \Phi), \\
B_{39} &= (\Lambda^2 y_{39,1} + \sigma \Lambda \Lambda z_{39,1}) \theta^4 \Phi^+ \square \Phi^+,
\end{aligned}$$

$$\begin{aligned}
B_{40} &= (\Lambda^2 y_{40,1} + \sigma \Lambda \Lambda z_{40,1}) \theta^4 (D^2 \Phi) (D^2 \Phi) \Phi^+, \\
B_{41} &= (\Lambda^2 y_{41,1} + \sigma \Lambda \Lambda z_{41,1}) \theta^4 \Phi^+ \Phi^+ \square \Phi^+, \\
B_{42} &= x_{42,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \partial_k \partial_l (D^2 \Phi), \\
B_{43} &= x_{43,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi^+ \square \partial_k \partial_l \Phi^+, \\
B_{44} &= x_{44,1} \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_l \partial_k (D^2 \Phi), \\
B_{45} &= x_{45,1} \Lambda^{kl} \theta^4 \Phi^+ \square \partial_k \partial_l \Phi^+, \\
B_{46} &= (\Lambda^2 y_{46,1} + \sigma \Lambda \Lambda z_{46,1}) \eta^{kl} \eta^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+, \\
B_{47} &= x_{47,1} \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+, \\
B_{48} &= x_{48,1} \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+, \\
B_{49} &= (\Lambda^2 y_{49,1} + \sigma \Lambda \Lambda z_{49,1}) \theta^4 (D^2 \Phi) \Phi^+, \\
B_{50} &= (\Lambda^2 y_{50,1} + \sigma \Lambda \Lambda z_{50,1}) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+, \\
B_{51} &= (\Lambda^2 y_{51,1} + \sigma \Lambda \Lambda z_{51,1}) \theta^4 (D^2 \Phi) \Phi^+ \Phi^+ \Phi^+, \\
B_{52} &= x_{52,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi^+ \square \Phi^+ \partial_k \partial_l \Phi^+, \\
B_{53} &= x_{53,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+, \\
B_{54} &= x_{54,1} \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+,
\end{aligned}$$

$$B_{55} = x_{55,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \partial_k \partial_l \Phi^+,$$

$$B_{56} = x_{56,1} \Lambda^{kl} \theta^4 (D^2 \Phi) \partial_k \partial_l \Phi^+,$$

$$B_{57} = x_{57,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+,$$

$$B_{58} = x_{58,1} \Lambda^{kl} \theta^4 (D^2 \Phi) \Phi^+ \partial_k \partial_l \Phi^+,$$

$$B_{59} = x_{59,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 (D^2 \Phi) \square \partial_k \partial_l \Phi^+,$$

$$B_{60} = x_{60,1} \Lambda^{kl} \theta^4 (D^2 \Phi) \square \partial_k \partial_l \Phi^+,$$

$$B_{61} = x_{61,1} \left( \eta \sigma \Lambda \Lambda^k \right)' \theta^4 \Phi^+ \Phi^+ \square \partial_k \partial_l \Phi^+,$$

$$B_{62} = x_{62,1} \eta^{kl} \Lambda^{no} \theta^4 \Phi^+ \partial_k \partial_n \Phi^+ \partial_l \partial_o \Phi^+,$$

$$B_{63} = x_{63,1} \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \square \partial_k \partial_l \Phi^+,$$

$$B_{64} = x_{64,1} \Lambda^{kl} \theta^4 \Phi^+ \square \Phi^+ \partial_k \partial_l \Phi^+,$$

$$B_{65} = (\Lambda^2 y_{65,1} + \sigma \Lambda \Lambda z_{65,1}) \theta^4 \Phi^+ \square \Phi^+ \square \Phi^+,$$

$$B_{66} = (\Lambda^2 y_{66,1} + \sigma \Lambda \Lambda z_{66,1}) \eta^{kl} \theta^4 \Phi^+ \Phi^+ \partial_k \Phi^+ \partial_l \Phi^+,$$

$$B_{67} = (\Lambda^2 y_{67,1} + \sigma \Lambda \Lambda z_{67,1}) \theta^4 (D^2 \Phi) \square \square \Phi^+,$$

$$B_{68} = (\Lambda^2 y_{68,1} + \sigma \Lambda \Lambda z_{68,1}) \theta^4 \Phi^+ \Phi^+ \square \square \Phi^+,$$

$$B_{69} = (\Lambda^2 y_{69,1} + \sigma \Lambda \Lambda z_{69,1}) \theta^4 \Phi^+ \Phi^+ \Phi^+ \square \Phi^+,$$

$$\begin{aligned}B_{70} &= (\Lambda^2 y_{70,1} + \sigma \Lambda \Lambda z_{70,1}) \eta^{kl} \theta^4 (D^2 \Phi) \partial_k \Phi^+ \partial_l \Phi^+, \\B_{71} &= (\Lambda^2 y_{71,1} + \sigma \Lambda \Lambda z_{71,1}) \theta^4 (D^2 \Phi) \square (D^2 \Phi), \\B_{72} &= (\Lambda^2 y_{72,1} + \sigma \Lambda \Lambda z_{72,1}) \theta^4 \Phi^+ \square \square \Phi^+, \\B_{73} &= (\Lambda^2 y_{73,1} + \sigma \Lambda \Lambda z_{73,1}) \theta^4 (D^2 \Phi) \square \Phi^+, \\B_{74} &= (\Lambda^2 y_{74,1} + \sigma \Lambda \Lambda z_{74,1}) \theta^4 (D^2 \Phi) \Phi^+ \square \Phi^+.\end{aligned}$$

## Invariant subset No. 29.

$$\begin{aligned}
f_{29} = & \frac{5(-18g^5 a_2 + 23g^7 a_3)}{13824} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) (D^2 \Phi) \\
& + \frac{-192g a_0 - 36g^5 a_2 + 55g^7 a_3}{3072} \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\
& + \frac{-144g a_0 - 45g^5 a_2 + 68g^7 a_3}{4608} \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
& + \frac{-864g a_0 - 360g^5 a_2 + 523g^7 a_3}{27648} \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \\
& + \frac{-3456g a_0 - 504g^5 a_2 + 851g^7 a_3}{55296} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi).
\end{aligned}$$

$$\begin{aligned}
B_{29} = & (-2x_{29,3} + 2x_{29,4}) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) (D^2 \Phi) \\
& + (-6x_{29,3} + 4x_{29,4} + 2x_{29,5}) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^\iota{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\
& + x_{29,3} \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) \\
& + x_{29,4} \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \\
& + x_{29,5} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi),
\end{aligned}$$

$$x_{29,3} \rightarrow -\frac{1}{32}, \quad x_{29,4} \rightarrow -\frac{1}{32}, \quad x_{29,5} \rightarrow -\frac{1}{16}; \quad (\mathcal{S}_\Lambda(\Lambda^2))$$

$$x_{29,3} \rightarrow -\frac{5}{512}, \quad x_{29,4} \rightarrow -\frac{5}{384}, \quad x_{29,5} \rightarrow -\frac{7}{768}; \quad (\Gamma_{2\text{nd}}(\Lambda^2))$$

$$x_{29,3} \rightarrow \frac{17}{1152}, \quad x_{29,4} \rightarrow \frac{523}{27648}, \quad x_{29,5} \rightarrow \frac{851}{55296}. \quad (\Gamma_{3\text{rd}}(\Lambda^2))$$

# Renormalizable Action

$$\mathcal{S}_{(3)} = \mathcal{S}_{\text{WZ}} + \int d^8 z \left( \sum_{i=1}^{74} B_i \right), \quad (\text{Its effective action is defined as } \Gamma_{4\text{th}}(\Lambda^2))$$

$$\begin{aligned} B'_{29} &= (-2x'_{29,3} + 2x'_{29,4}) \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 (D_\beta \Phi) \partial_l \partial_k (D_\alpha \Phi) (D^2 \Phi) \\ &\quad + (-6x'_{29,3} + 4x'_{29,4} + 2x'_{29,5}) \epsilon^{\alpha\beta} \epsilon^{\zeta\iota} \Lambda^k{}_\beta \Lambda^l{}_\iota \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\zeta \Phi) (D^2 \Phi) \\ &\quad + x'_{29,3} \Lambda^{kl} \theta^4 \Phi \partial_k (D^2 \Phi) \partial_l (D^2 \Phi) + x'_{29,4} \Lambda^{kl} \theta^4 \Phi (D^2 \Phi) \partial_l \partial_k (D^2 \Phi) \\ &\quad + x'_{29,5} \epsilon^{\alpha\beta} \Lambda^{kl} \theta^4 \partial_k (D_\alpha \Phi) \partial_l (D_\beta \Phi) (D^2 \Phi), \end{aligned}$$

$$x'_{29,3} = \frac{-g}{32\pi^2 \epsilon} (4x_{21,23} - x_{21,26} + 2x_{21,27}),$$

$$x'_{29,4} = \frac{-g}{96\pi^2 \epsilon} (2x_{20,2} + 6x_{21,19} + 12x_{21,23} - 3x_{21,26} + 6x_{21,27}),$$

$$x'_{29,5} = \frac{g}{48\pi^2 \epsilon} (2x_{20,2} + 6x_{21,19} - 6x_{21,23} - 3x_{21,26} - 3x_{21,27}),$$

$$(x_0)_{29,3} = \textcolor{blue}{x_{29,3}} \left( 1 - \frac{x'_{29,3}}{\textcolor{blue}{x_{29,3}}} \right) \left( \frac{1}{\sqrt{Z}} \right)^3.$$

Renormalization of all the parameters  $m$ ,  $g$ ,  $\textcolor{blue}{x_{i,j}}$ ,  $\textcolor{blue}{y_{i,j}}$ , and  $\textcolor{blue}{z_{i,j}}$  is compatible.

## Comments

- Through analyzing the Wess-Zumino model on the BFNC superspace, we know that the action obtained by replacing the ordinary product by the star product is not renormalizable in general.
- To make it renormalizable one should add to it correction terms. For the NAC superspace, which is a simpler case, one just needs to add the terms from the primary one-loop effective action, and then provides the renormalizable action to all orders in perturbation theory.
- However, for the BFNC superspace the situation is much more complicated. The iterative process should go up to the third time.
- Moreover, the complexity also includes that the obtained renormalizable action has so many terms that can be classified on the one hand into 74 subsets each of which has the  $1/2$  supersymmetry invariance, and on the other hand into 74 bases that correspond to the 74 subsets.
- In particular, in light of the invariant bases we construct the one-loop renormalizable action up to the second order of the BFNC parameters  $\Lambda^{k\alpha}$ 's.

- BFNC Wess-Zumino Model Renormalizable to All Orders

# Description of Idea and Treatment

- The method we take is similar to the one used to construct NAC Wess-Zumino action. [R. Britto et al, hep-th/0307165, A. Romagnoni, hep-th/0307209]
- The one loop renormalizable BFNC Wess-Zumino action  $S_{(3)}$  has only 1/2 supersymmetry but not global  $U(1)$  symmetries, because the mass and interaction parameters are real numbers.
- If we want to use the symmetry analysis method that is very powerful for the construction of renormalizable NAC Wess-Zumino action, we have to introduce two global  $U(1)$  symmetries, such as  $U(1)_R$   $R$ -symmetry and  $U(1)_\Phi$  flavor symmetry for  $S_{(3)}$ .
- At first, we generalize the mass and interaction parameters to complex numbers, and define the  $U(1)_R$   $R$ -symmetry and  $U(1)_\Phi$  flavor symmetry charges for operators as well as mass and interaction parameters, exactly following the NAC case.
- Then, we define the global  $U(1)$  symmetry charges for BFNC parameter  $\Lambda^k_\alpha$ .

# Modify $\mathcal{S}_{(3)}$

- The undeformed part of  $\mathcal{S}_{(3)}$ ,

$$\begin{aligned} \mathcal{S}'_{\text{WZ}} = & \int d^8 z \left\{ \Phi^+ \Phi - \frac{m}{8} \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{m^*}{8} \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) \right. \\ & \left. - \frac{g}{12} \Phi \Phi \left( \frac{D^2}{\square} \Phi \right) - \frac{g^*}{12} \Phi^+ \Phi^+ \left( \frac{\bar{D}^2}{\square} \Phi^+ \right) \right\}. \end{aligned}$$

- The deformed part of  $\mathcal{S}_{(3)}$ ,

$$\int d^8 z m^{a_1} (m^*)^{a_2} g^{a_3} (g^*)^{a_4} X$$

Its mass dimension,  $U(1)_R$  charge,  $U(1)_\Phi$  charge should be zero.

- We deduce from  $\mathcal{S}_{(3)}$  the modified action,

$$\mathcal{S}'_{(3)} = \mathcal{S}'_{\text{WZ}} + \int d^8 z \left( \sum_{i=1}^{74} c_i B_i \right).$$

# The Coefficients $c_i$ 's I

The coefficients  $c_i$ 's, where  $i = 1, \dots, 89$ , are listed below.

$$\begin{array}{llll}
c_1 = g^2 m (m^*)^3, & c_2 = g^3 (m^*)^3, & c_3 = g m (m^*)^2, & c_4 = g^2 (m^*)^2, \\
c_5 = m m^*, & c_6 = g m^*, & c_7 = m g^*, & c_8 = 1, \\
c_9 = g m m^*, & c_{10} = g^2 m^*, & c_{11} = m, & c_{12} = g, \\
c_{13} = g (m^*)^2, & c_{14} = m^*, & c_{15} = g^*, & c_{16} = g^4 (m^*)^5, \\
c_{17} = g m^*, & c_{18} = g^2 (m^*)^2, & c_{19} = g^2 (m^*)^3, & c_{20} = 1, \\
c_{21} = 1, & c_{22} = g^2 (m^*)^2, & c_{23} = g^2 (m^*)^3, & c_{24} = g (m^*)^2, \\
c_{25} = m^*, & c_{26} = g^*, & c_{27} = g, & c_{28} = g^3 (m^*)^3, \\
c_{29} = g, & c_{30} = g m^2 (m^*)^3, & c_{31} = g (m^*)^3, & c_{32} = g, \\
c_{33} = g (m^*)^3, & c_{34} = m (m^*)^3, & c_{35} = m (m^*)^3, & c_{36} = g, \\
c_{37} = g, & c_{38} = m^2 m^*, & c_{39} = m (m^*)^2, & c_{40} = m^2 g^*, \\
c_{41} = m g^* m^*, & c_{42} = g^2 m (m^*)^3, & c_{43} = g^2 (m^*)^4, & c_{44} = m, \\
c_{45} = m^*, & c_{46} = g^*, & c_{47} = m (g^*)^2, & c_{48} = m (g^*)^2, \\
c_{49} = m^2 (m^*)^2, & c_{50} = m^2 g^* m^*, & c_{51} = m^2 (g^*)^2, & c_{52} = g (m^*)^3, \\
c_{53} = g m (m^*)^3, & c_{54} = m g^*, & c_{55} = g^2 m (m^*)^4, & c_{56} = m m^*, \\
\end{array}$$

# The Coefficients $c_i$ 's II

$$\begin{array}{llll}
 c_{57} = gm(m^*)^3, & c_{58} = mg^*, & c_{59} = g^2(m^*)^3, & c_{60} = 1, \\
 c_{61} = g(m^*)^3, & c_{62} = g^*, & c_{63} = g^*, & c_{64} = g^*, \\
 c_{65} = g^*, & c_{66} = m(g^*)^2, & c_{67} = 1, & c_{68} = g^*, \\
 c_{69} = m(g^*)^2, & c_{70} = mg^*, & c_{71} = m, & c_{72} = m^*, \\
 c_{73} = mm^*, & c_{74} = mg^*, & c_{75} = gm^2(m^*)^4, & c_{76} = m^2(m^*)^3, \\
 c_{77} = m^2g^*(m^*)^2, & c_{78} = m^2(g^*)^2m^*, & c_{79} = m^2(g^*)^3, & c_{80} = g^3(m^*)^5, \\
 c_{81} = g^2(m^*)^4, & c_{82} = g(m^*)^3, & c_{83} = (m^*)^2, & c_{84} = g^*m^*, \\
 c_{85} = (g^*)^2, & c_{86} = m(m^*)^2, & c_{87} = g^2m(m^*)^5, & c_{88} = mg^*m^*, \\
 c_{89} = gm(m^*)^4. & & & 
 \end{array}$$

# Symmetry Charges

	dim	$U(1)_R$	$U(1)_\Phi$		dim	$U(1)_R$	$U(1)_\Phi$
$m$	1	0	-2	$m^*$	1	0	2
$g$	0	-1	-3	$g^*$	0	1	3
$(\Lambda^k{}_\alpha)^2$	-3	2	0	$V$	-5	2	0
$d^4\theta$	2	0	0	$\theta^4$	-2	0	0
$\Phi$	1	1	1	$\Phi^+$	1	-1	-1
$D_\alpha$	$\frac{1}{2}$	-1	0	$\bar{D}_{\dot{\alpha}}$	$\frac{1}{2}$	1	0
$D^2$	1	-2	0	$\bar{D}^2$	1	2	0
$\partial_k$	1	0	0	$d^4x$	-4	0	0

Table : Mass dimensions and symmetry charges of parameters and operators.

# Constraints on Divergent Operators from Symmetries

$$\begin{aligned}
 \Gamma &= \int d^4x \lambda \mathcal{O}, \quad \lambda \sim \Lambda_{UV}^d g^{x-R} g^{*x} \left( \frac{m}{\Lambda_{UV}} \right)^y \left( \frac{m^*}{\Lambda_{UV}} \right)^{y+\frac{S-3R}{2}}, \\
 \mathcal{O} &= d^4 \theta (D^2)^\gamma (\bar{D}^2)^\delta (\partial D \bar{D})^\eta (\partial \partial)^\zeta V^\rho \Phi^\alpha (\Phi^+)^{\beta}, \quad V \equiv (\Lambda^k{}_\alpha)^2 \theta^4, \\
 d &= 2 - \alpha - \beta - \gamma - \delta - 2\zeta - 2\eta + 5\rho, \quad R = -\alpha + \beta + 2\gamma - 2\delta - 2\rho, \quad S = -\alpha + \beta, \\
 P &= d + \frac{3R}{2} - \frac{S}{2} - 2y = 2 - 2y - 2\alpha + 2\gamma - 4\delta - 2\zeta - 2\eta + 2\rho \geq 0, \\
 \gamma &\leq \alpha - \eta, \quad \delta \leq \beta - \eta, \\
 \gamma &\geq 0, \quad \delta \geq 0, \quad \alpha \geq 0, \quad \eta \geq 0, \quad \rho \geq 0, \quad \zeta \geq 0, \quad \beta \geq 0, \\
 \rho &= 1, \\
 y &\geq 0, \quad x \geq 0, \quad x + \alpha - \beta - 2\gamma + 2\delta + 2\rho \geq 0, \quad y + \alpha - \beta - 3\gamma + 3\delta + 3\rho \geq 0.
 \end{aligned}$$

They are just linear equations and can be solved easily.

# Divergent Operators

$$\begin{aligned} \Phi, \quad \Phi\Phi, \quad \Phi\Phi^+, \quad \Phi\Phi^+\Phi^+, \quad \Phi\Phi^+\Phi^+\Phi^+, \quad \Phi\Phi^+\Phi^+\Phi^+\Phi^+, \quad \Phi\Phi^+\Phi^+\Phi^+\Phi^+\Phi^+, \\ \Phi\Phi\Phi^+, \quad \Phi\Phi\Phi^+\Phi^+, \quad \Phi\Phi\Phi^+\Phi^+\Phi^+, \quad \Phi\Phi\Phi^+\Phi^+\Phi^+\Phi^+, \quad \Phi\Phi\Phi^+\Phi^+\Phi^+\Phi^+\Phi^+; \end{aligned} \quad (1)$$

$$\partial\partial\Phi, \quad \partial\partial\Phi^+, \quad \partial\partial\partial\Phi^+, \quad D^2\partial\partial\Phi, \quad D^2\partial\partial\partial\Phi; \quad (2)$$

$$\begin{aligned} \Phi^+, \quad \Phi^+\Phi^+, \quad \Phi^+\Phi^+\Phi^+, \quad \Phi^+\Phi^+\Phi^+\Phi^+, \quad \Phi^+\Phi^+\Phi^+\Phi^+\Phi^+, \quad \bar{D}^2\Phi^+, \quad \bar{D}^2\Phi^+\Phi^+, \\ \bar{D}^2\Phi^+\Phi^+\Phi^+, \quad \bar{D}^2\Phi^+\Phi^+\Phi^+\Phi^+, \quad \bar{D}^2\Phi^+\Phi^+\Phi^+\Phi^+\Phi^+, \quad \bar{D}^2\Phi^+\Phi^+\Phi^+\Phi^+\Phi^+\Phi^+. \end{aligned} \quad (3)$$

$$\begin{aligned} D^2\Phi; \quad (4.1) \quad D^2\Phi\Phi, \quad D^2D^2\Phi\Phi, \quad \partial\partial\Phi^+\Phi^+, \quad \partial\partial\partial\Phi^+\Phi^+, \quad D^2\partial\partial\Phi\Phi, \quad D^2\Phi\Phi^+, \\ D^2D^2\partial\partial\Phi\Phi, \quad \partial\partial\Phi\Phi^+, \quad \partial D\bar{D}\Phi\Phi^+, \quad D^2\partial\partial\Phi\Phi^+, \quad D^2\partial\partial\partial\Phi\Phi^+, \quad D^2\bar{D}^2\Phi\Phi^+; \end{aligned} \quad (4.2)$$

$$\begin{aligned} D^2\Phi\Phi\Phi, \quad D^2D^2\Phi\Phi\Phi, \quad \partial\partial\Phi^+\Phi^+\Phi^+, \quad \partial\partial\partial\Phi^+\Phi^+\Phi^+, \quad D^2\Phi\Phi^+\Phi^+, \quad D^2\Phi\Phi\Phi^+, \\ D^2D^2\partial\partial\Phi\Phi\Phi, \quad D^2D^2\Phi\Phi\Phi^+, \quad \partial\partial\Phi\Phi^+\Phi^+, \quad \partial D\bar{D}\Phi\Phi^+\Phi^+, \quad D^2\partial\partial\Phi\Phi^+\Phi^+, \\ D^2\partial\partial\Phi\Phi\Phi^+, \quad D^2\partial D\bar{D}\Phi\Phi\Phi^+, \quad D^2\bar{D}^2\Phi\Phi^+\Phi^+, \quad D^2D^2\bar{D}^2\Phi\Phi\Phi^+; \end{aligned} \quad (4.3)$$

$$\begin{aligned} D^2D^2\Phi\Phi\Phi\Phi, \quad \partial\partial\Phi^+\Phi^+\Phi^+\Phi^+, \quad D^2\Phi\Phi^+\Phi^+\Phi^+, \quad D^2\Phi\Phi\Phi^+\Phi^+, \quad D^2\Phi\Phi\Phi\Phi^+, \\ D^2D^2\Phi\Phi\Phi\Phi^+, \quad \partial\partial\Phi\Phi^+\Phi^+\Phi^+, \quad \partial D\bar{D}\Phi\Phi^+\Phi^+\Phi^+, \quad D^2\partial\partial\Phi\Phi\Phi^+\Phi^+, \end{aligned}$$

$$D^2\partial D\bar{D}\Phi\Phi\Phi^+\Phi^+, \quad D^2\bar{D}^2\Phi\Phi^+\Phi^+\Phi^+, \quad D^2D^2\bar{D}^2\Phi\Phi\Phi^+\Phi^+; \quad (4.4)$$

$$\begin{aligned} D^2\Phi\Phi\Phi^+\Phi^+\Phi^+, \quad D^2\Phi\Phi\Phi^+\Phi^+, \quad D^2D^2\Phi\Phi\Phi\Phi\Phi^+, \quad \partial\partial\Phi\Phi^+\Phi^+\Phi^+\Phi^+, \\ \partial D\bar{D}\Phi\Phi^+\Phi^+\Phi^+\Phi^+, \quad D^2\bar{D}^2\Phi\Phi^+\Phi^+\Phi^+\Phi^+; \quad (4.5) \quad D^2\Phi\Phi\Phi\Phi^+\Phi^+\Phi^+ \quad (4.6). \end{aligned}$$

# BFNC Parameters

By using the following symbols,

$$\epsilon_{\alpha\beta}, \quad \epsilon^{\alpha\beta}, \quad \epsilon_{\dot{\alpha}\dot{\beta}}, \quad \epsilon^{\dot{\alpha}\dot{\beta}}, \quad \eta_{kl}, \quad \eta^{kl}, \quad \epsilon^{klmn}, \quad (\sigma^{kl})^{\alpha\beta}, \quad (\bar{\sigma}^k)^{\dot{\alpha}\beta}, \quad \Lambda^k{}_\alpha.$$

we can construct various possible forms of BFNC parameters,

$$\Lambda^2, \quad \sigma\Lambda\Lambda; \quad (\eta\sigma\Lambda\Lambda^k)^l, \quad \Lambda^{kl}, \quad \Lambda^2\eta^{kl}, \quad \sigma\Lambda\Lambda\eta^{kl};$$

$$\Lambda^2\epsilon^{\alpha\beta}, \quad \sigma\Lambda\Lambda\epsilon^{\alpha\beta}; \quad \Lambda^2\epsilon^{\dot{\alpha}\dot{\beta}}, \quad \sigma\Lambda\Lambda\epsilon^{\dot{\alpha}\dot{\beta}};$$

$$\Lambda^2(\bar{\sigma}^k)^{\dot{\alpha}\beta}, \quad \sigma\Lambda\Lambda(\bar{\sigma}^k)^{\dot{\alpha}\beta}, \quad \Lambda^{kl}\eta_{ln}(\bar{\sigma}^n)^{\dot{\alpha}\beta}, \quad \eta_{nl}(\bar{\sigma}^l)^{\dot{\alpha}\beta}(\eta\sigma\Lambda\Lambda^n)^k, \quad \eta_{nl}(\bar{\sigma}^l)^{\dot{\alpha}\beta}(\eta\sigma\Lambda\Lambda^k)^n;$$

$$\Lambda^2\eta^{kl}\eta^{no}, \quad \sigma\Lambda\Lambda\eta^{kl}\eta^{no}, \quad \eta^{kl}\Lambda^{no}, \quad (\sigma\Lambda\Lambda^{kl})^{no}, \quad \eta^{kl}(\eta\sigma\Lambda\Lambda^n)^o;$$

$$\epsilon^{\alpha\beta}(\eta\sigma\Lambda\Lambda^k)^l, \quad \epsilon^{\alpha\beta}\Lambda^{kl}, \quad \Lambda^2\eta^{kl}\epsilon^{\alpha\beta}, \quad \sigma\Lambda\Lambda\eta^{kl}\epsilon^{\alpha\beta}, \quad \Lambda^2(\sigma^{kl})^{\alpha\beta}, \quad \sigma\Lambda\Lambda(\sigma^{kl})^{\alpha\beta},$$

$$\Lambda^{ko}\eta_{on}(\sigma^{nl})^{\alpha\beta}, \quad \epsilon^{\alpha\zeta}\epsilon^{\beta\iota}\epsilon^{klno}\eta_{np}\eta_{oq}\Lambda^p{}_\zeta\Lambda^q{}_\iota, \quad \epsilon^{\alpha\zeta}\eta_{no}(\sigma\Lambda^{ok})^{l\beta}\Lambda^n{}_\zeta, \quad \epsilon^{\alpha\zeta}(\eta\sigma\Lambda^k)^\beta\Lambda^l{}_\zeta,$$

$$\epsilon^{\alpha\zeta}\epsilon^{\beta\iota}\Lambda^k{}_\zeta\Lambda^l{}_\iota, \quad \eta^{kl}\epsilon^{\alpha\zeta}\eta_{no}(\eta\sigma\Lambda^n)^\beta\Lambda^o{}_\zeta.$$

# Construction of the Effective Action of $S'_{(3)}$

$$\begin{aligned}
 B_{75} &= (\Lambda^2 y_{75,1} + \sigma \Lambda \Lambda z_{75,1}) \theta^4 \Phi^+, \quad B_{76} = (\Lambda^2 y_{76,1} + \sigma \Lambda \Lambda z_{76,1}) \theta^4 \Phi^+ \Phi^+, \\
 B_{77} &= (\Lambda^2 y_{77,1} + \sigma \Lambda \Lambda z_{77,1}) \theta^4 \Phi^+ \Phi^+ \Phi^+, \quad B_{78} = (\Lambda^2 y_{78,1} + \sigma \Lambda \Lambda z_{78,1}) \theta^4 \Phi^+ \Phi^+ \Phi^+ \Phi^+, \\
 B_{79} &= (\Lambda^2 y_{79,1} + \sigma \Lambda \Lambda z_{79,1}) \theta^4 \Phi^+ \Phi^+ \Phi^+ \Phi^+ \Phi^+, \\
 B_{80} &= (\Lambda^2 y_{80,1} + \sigma \Lambda \Lambda z_{80,1}) \theta^4 (\bar{D}^2 \Phi^+), \\
 B_{81} &= (\Lambda^2 y_{81,2} + \sigma \Lambda \Lambda z_{81,2}) \theta^4 (\bar{D}^2 \Phi^+) \Phi^+ + (\Lambda^2 y_{81,2} + \sigma \Lambda \Lambda z_{81,2}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+), \\
 B_{82} &= \left(\frac{1}{2} \Lambda^2 y_{82,2} + \frac{1}{2} \sigma \Lambda \Lambda z_{82,2}\right) \theta^4 (\bar{D}^2 \Phi^+) \Phi^+ \Phi^+ + (\Lambda^2 y_{82,2} + \sigma \Lambda \Lambda z_{82,2}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+) \Phi^+, \\
 B_{83} &= \left(\frac{1}{3} \Lambda^2 y_{83,2} + \frac{1}{3} \sigma \Lambda \Lambda z_{83,2}\right) \theta^4 (\bar{D}^2 \Phi^+) \Phi^+ \Phi^+ \Phi^+ + (\Lambda^2 y_{83,2} + \sigma \Lambda \Lambda z_{83,2}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+) \Phi^+ \Phi^+, \\
 B_{84} &= \left(\frac{1}{4} \Lambda^2 y_{84,2} + \frac{1}{4} \sigma \Lambda \Lambda z_{84,2}\right) \theta^4 (\bar{D}^2 \Phi^+) \Phi^+ \Phi^+ \Phi^+ \Phi^+ \\
 &\quad + (\Lambda^2 y_{84,2} + \sigma \Lambda \Lambda z_{84,2}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+) \Phi^+ \Phi^+ \Phi^+, \\
 B_{85} &= \left(\frac{1}{5} \Lambda^2 y_{85,2} + \frac{1}{5} \sigma \Lambda \Lambda z_{85,2}\right) \theta^4 (\bar{D}^2 \Phi^+) \Phi^+ \Phi^+ \Phi^+ \Phi^+ \Phi^+ \\
 &\quad + (\Lambda^2 y_{85,2} + \sigma \Lambda \Lambda z_{85,2}) \epsilon^{\dot{\alpha}\dot{\beta}} \theta^4 (\bar{D}_{\dot{\alpha}} \Phi^+) (\bar{D}_{\dot{\beta}} \Phi^+) \Phi^+ \Phi^+ \Phi^+ \Phi^+, \\
 B_{86} &= x_{86,1} \Lambda^{kl} \theta^4 \Phi^+ \partial_k \partial_l \Phi^+, \quad B_{87} = x_{87,1} (\eta \sigma \Lambda^k)^l \theta^4 \Phi^+ \partial_k \partial_l \Phi^+, \\
 B_{88} &= x_{88,1} \Lambda^{kl} \theta^4 \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+, \quad B_{89} = x_{89,1} (\eta \sigma \Lambda^k)^l \theta^4 \Phi^+ \Phi^+ \partial_k \partial_l \Phi^+.
 \end{aligned}$$

# Construct Action Renormalizable to All Orders

We now deduce that  $\mathcal{S}'_{(3)}$  plus these terms is renormalizable to all orders in perturbation theory,

$$\mathcal{S}'_{(3)} + \int d^8 z \left( \sum_{i=75}^{89} c_i B_i \right).$$

# Conclusion and Outlook

- One-loop renormalizable BFNC Wess-Zumino model.
- BFNC Wess-Zumino model Renormalizable to all orders.
- BFNC Wess-Zumino renormalizable at a higher order of BFNC parameters.
- NAC Yang-Mills model is renormalizable in Wess-Zumino gauge based on dimensional analysis, [O. Lunin et al, [hep-th/0307275](#), D. Berenstein, [hep-th/0308049](#)].
- Check the dimensional analysis result for NAC Yang-Mills model in terms of components form in the WZ gauge. [M. Alishahiha et al, [hep-th/0309037](#), I. Jack et al, [hep-th/0412009](#), [hep-th/0505248](#), [hep-th/0509089](#), [hep-th/0701096](#), arXiv:0808.0400, arXiv:0901.2876, arXiv:0909.1929, arXiv:1012.2000].
- Do perturbation analysis for NAC Yang-Mills model directly in superspace without expanding in components in a particular gauge, [S. Penati, [hep-th/0412041](#), arXiv:0901.3094, M. T. Grisaru, [hep-th/0510175](#), M. S. Bianchi et al, arXiv:0904.3260].