

# Jet productions in “little bang”



张本威


(Ben-Wei Zhang)

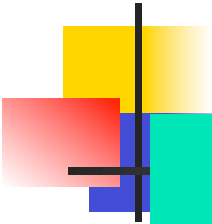
华中师范大学粒子物理研究所  
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中国科大交叉学科理论研究中心

中国合肥 2012年5月10日

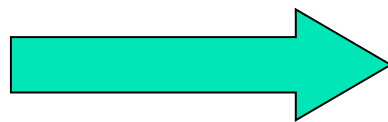
# Outline

- 
- Introduction
  - Jet observables in HIC
    - 1) jet shape
    - 2) inclusive jet cross section
    - 3) tagged jet production
    - 4) di-jet momentum imbalance
  - Summary



# Jet quenching: From hadrons to jets

QCD



QGP

It would be interesting to explore new phenomena by distributing high energy or high nuclear density over a relatively large volume.

T. D. Lee (1978)

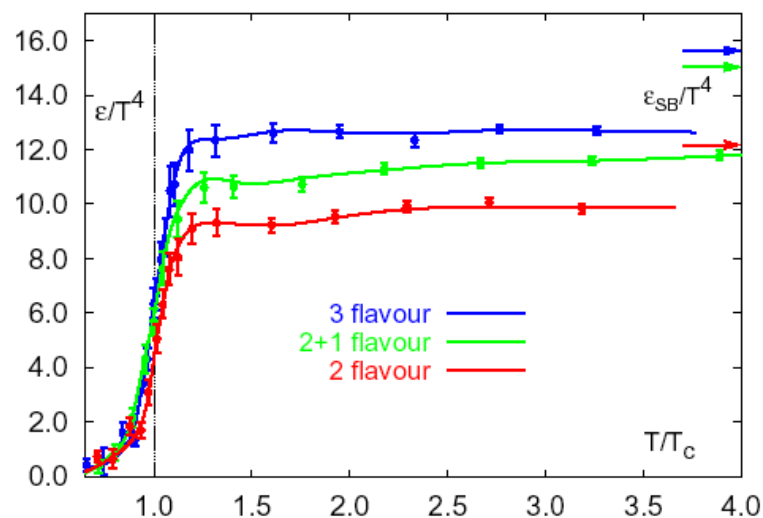
Lattice QCD predicts phase of thermal QCD matter with sharp rise in number of degrees of freedom near  $T_c=170\text{MeV}$ .

對撞生新能心

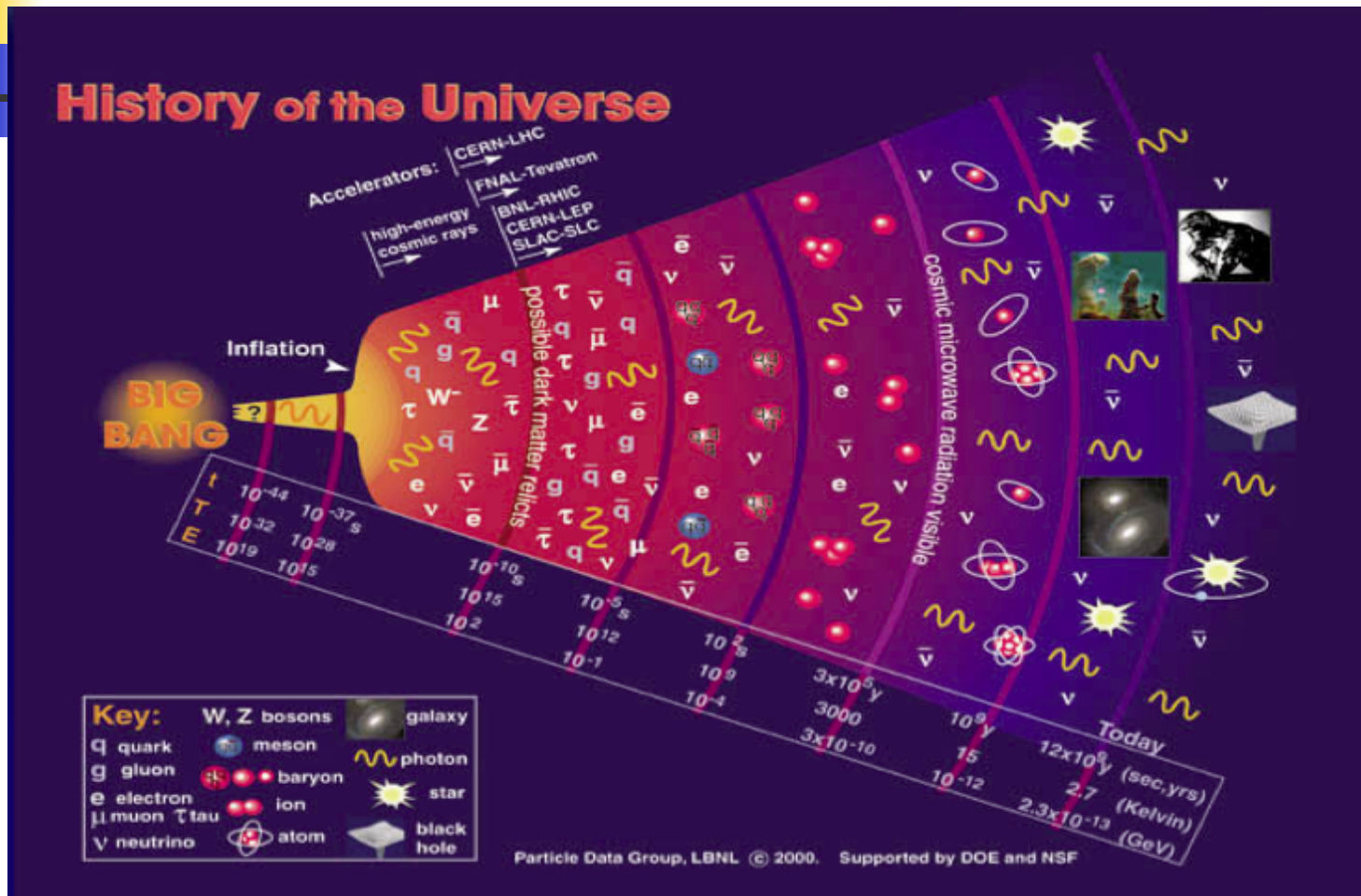


Nuclei as heavy as bulls  
Through collision  
Generate new states of matter

核子重如牛

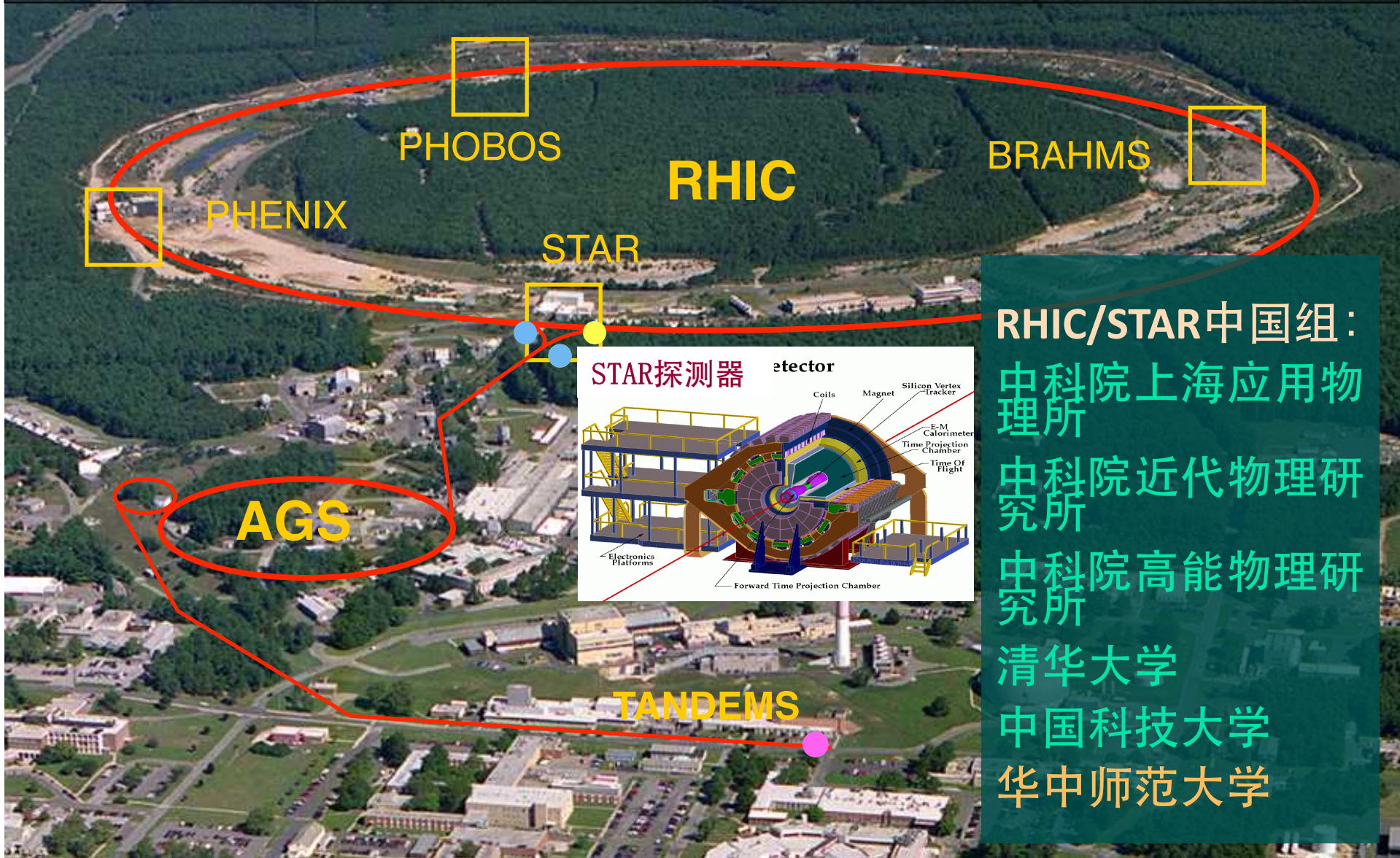


# QGP & Big Bang



Investigations of the QGP help us understand the evolution of the early Universe

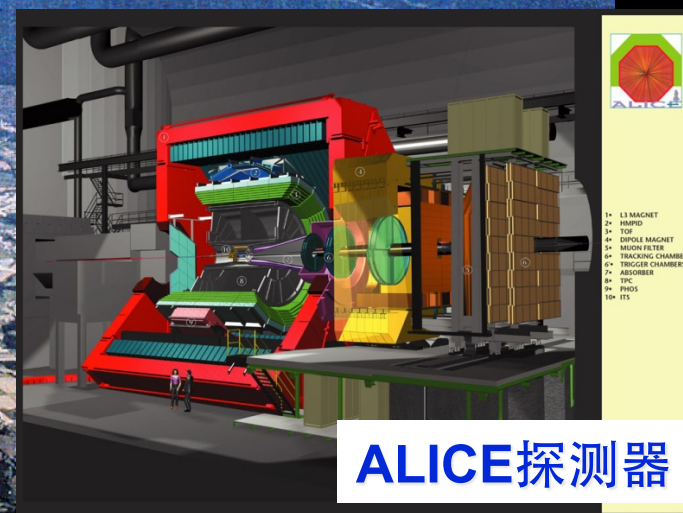
# “Little Bang” at RHIC (2000年-)



**RHIC/STAR中国组:**  
中科院上海应用物理所  
中科院近代物理研究所  
中科院高能物理研究所  
清华大学  
中国科技大学  
华中师范大学

# “Little Bang” at LHC (2008年 - )

## Heavy ion实验@ CERN/LHC (27km)

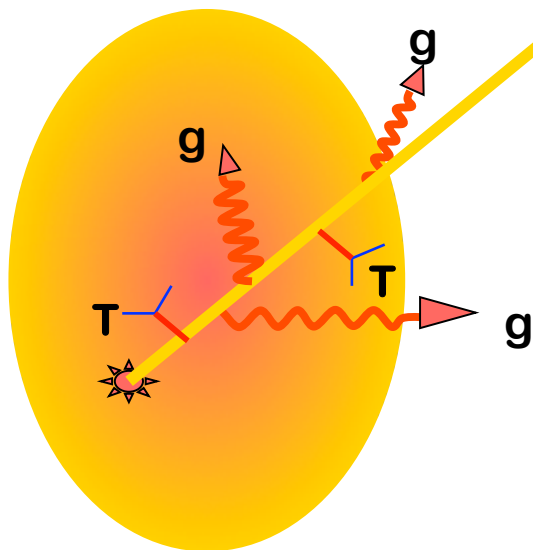


LHC/ALICE中国组：  
华中师范大学  
中国原子能研究院  
华中科技大学

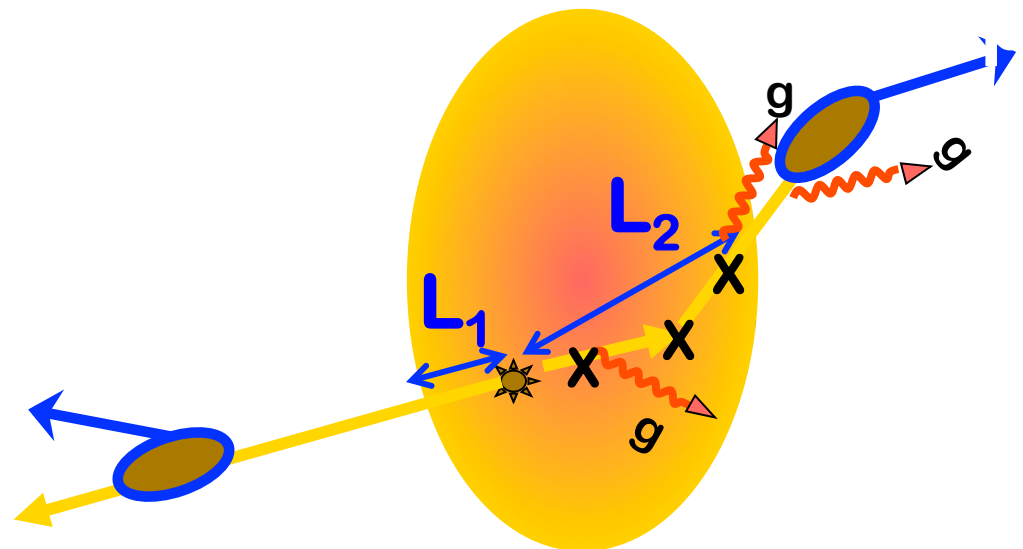
# Jet quenching as a hard probe

Jet quenching has been proposed as an excellent probe of the hot/dense matter created at HIC.

Single Hadron Tomography



Di-Hadron Tomography



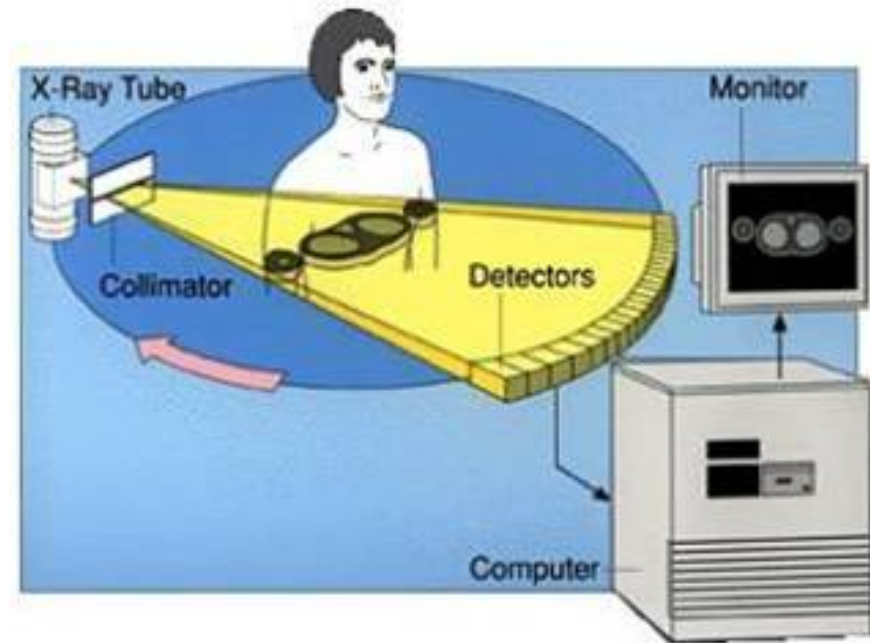
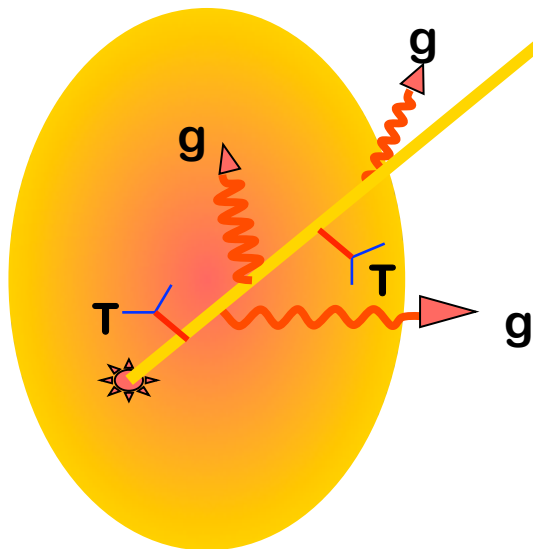
Xin-Nian Wang, M. Gyulassy, PRL68(1992)1480



# Jet quenching as a hard probe

Jet quenching has been proposed as an excellent probe of the hot/dense matter created at HIC.

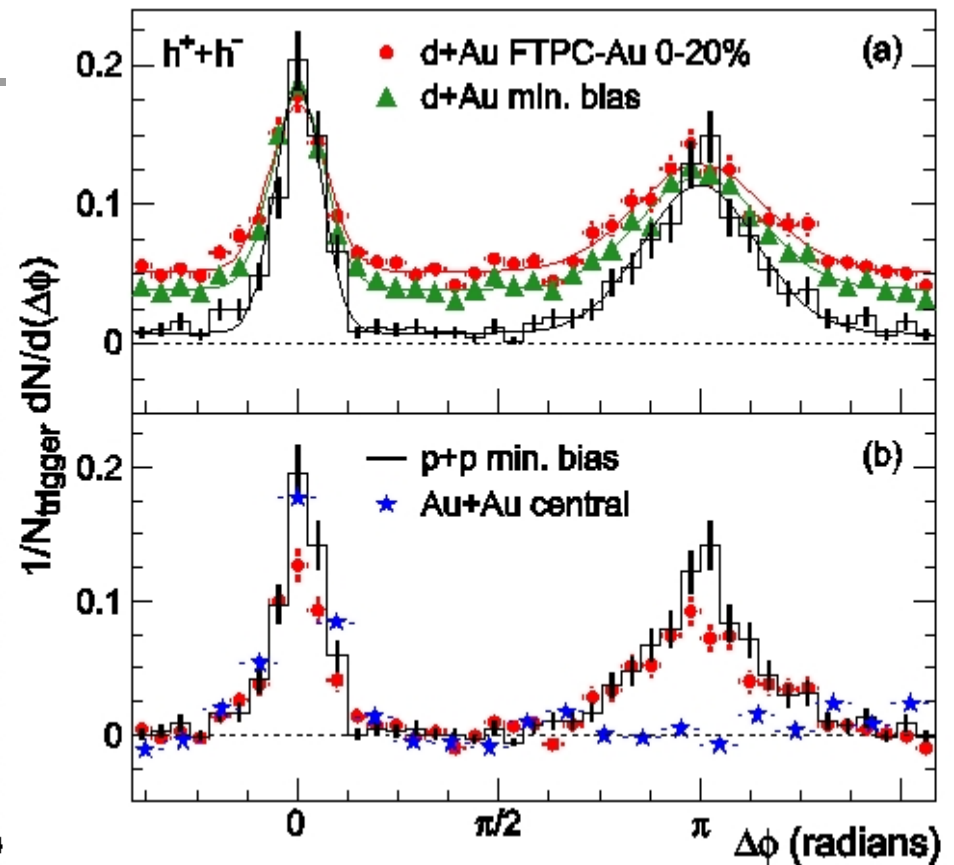
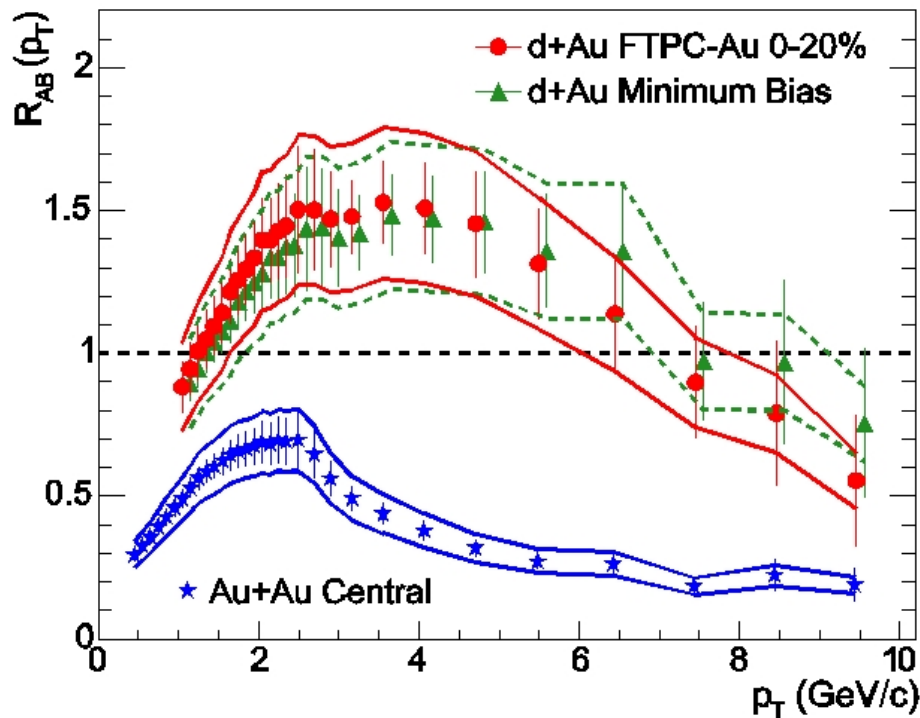
## Single Hadron Tomography



Xin-Nian Wang, M. Gyulassy, PRL68(1992)1480

# Jet quenching at RHIC

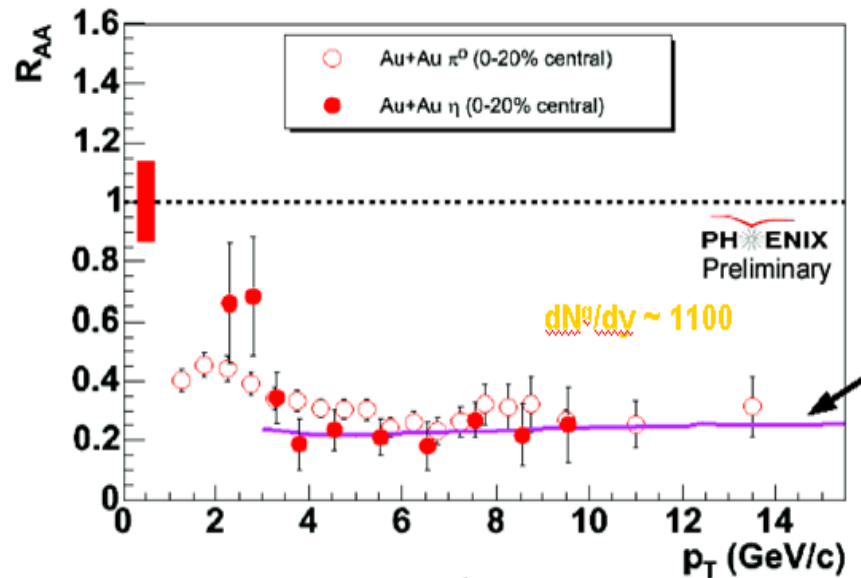
$$R_{AA} = \frac{\text{Yield}_{\text{AuAu}} / \langle N_{\text{binary}} \rangle_{\text{AuAu}}}{\text{Yield}_{\text{pp}}}$$



Finding of the jet quenching effect in A+A collisions has been regarded as one of the most important discoveries made at RHIC.

Gyulassy, Vitev, X.N.Wang, BWZ, «QGP3» p123-191 (2004); nucl-th/0302077.

# Jet quenching with $R_{AA}$



Gyulassy-Levai-Vitev(GLV) formalism

Gyulassy, Levai, Vitev, NPB 594(2001)371

$$\epsilon \approx \frac{p_0}{\tau_0 \pi R^2} \frac{dN_g}{dy} \quad \epsilon_A \simeq 0.16 \frac{\text{GeV}}{\text{fm}^3}.$$

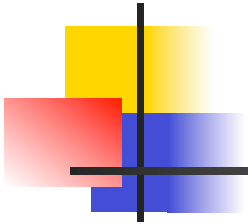
$$\approx 15 - 20 \frac{\text{GeV}}{\text{fm}^3},$$

- Advantage of  $R_{AA}$  : providing useful information of the hot/dense medium, with a simple physics picture.
- Disadvantage of  $R_{AA}$ : unable to resolve the order of magnitude systematic discrepancy in the extracted medium properties.

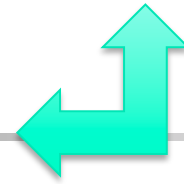
Medium transport coefficient:

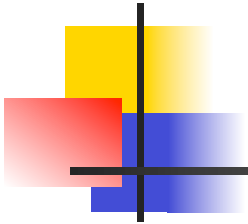
$$\hat{q}$$

1-2.5 GeV<sup>2</sup>/fm (GLV, HT), 4-5 GeV<sup>2</sup>/fm(AMY), 10-15 GeV<sup>2</sup>/fm(ASW)

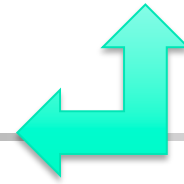


领头强子





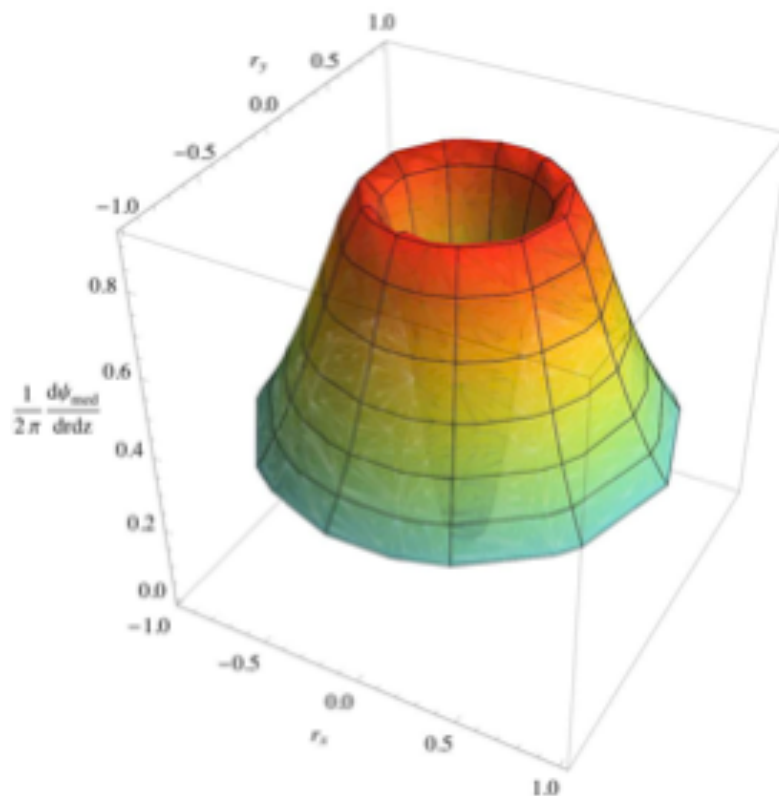
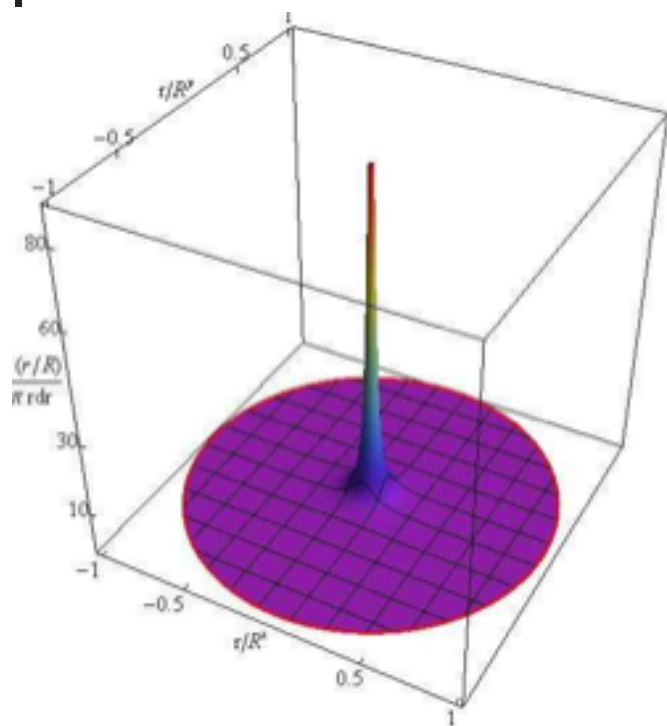
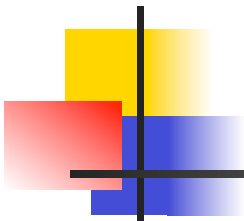
领头强子



整体喷注



# From leading hadrons to jets: Th

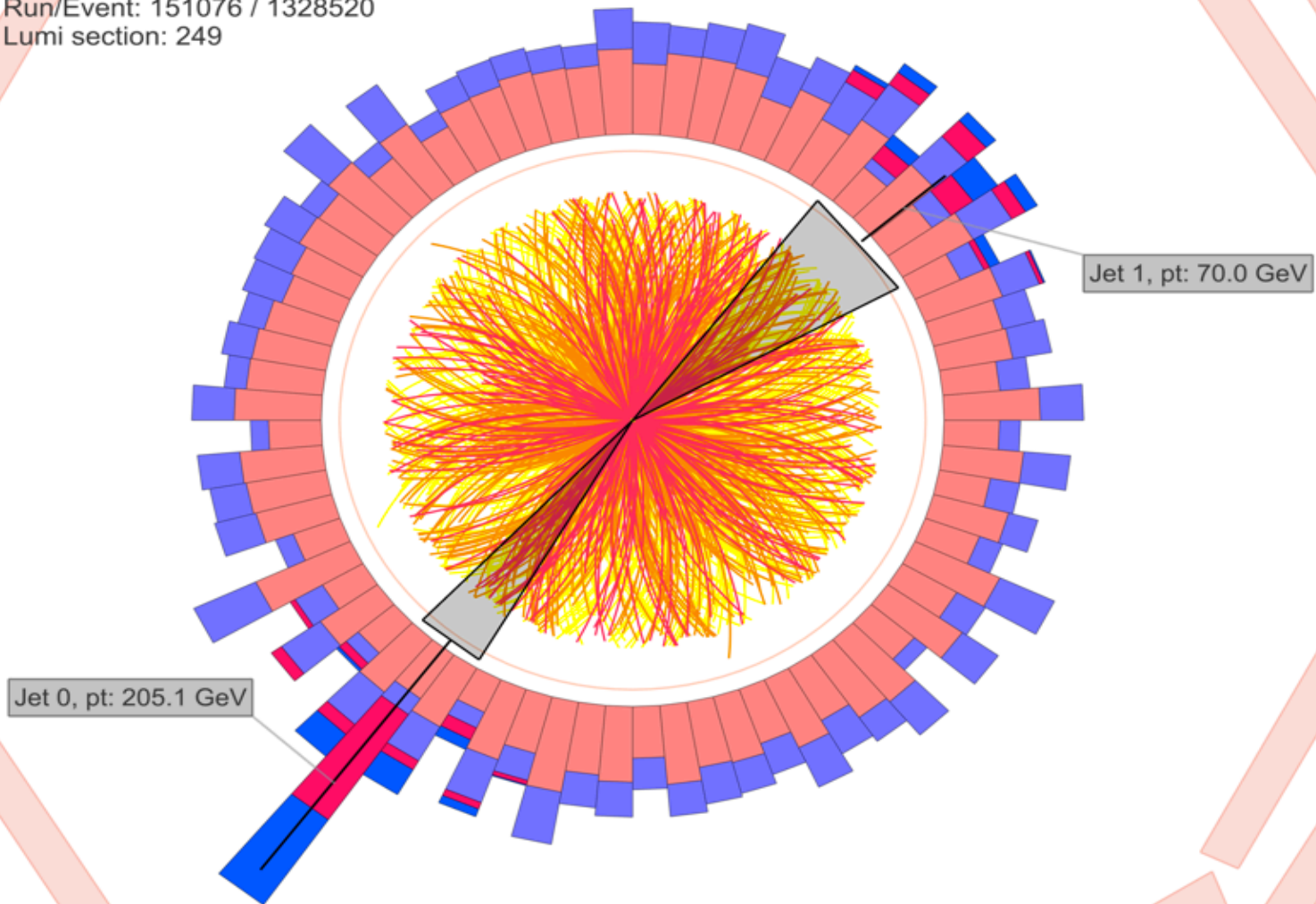


I Vitev, S Wicks, BWZ, JHEP 0811,093 (2008)

# From leading hadrons to jets: Exp

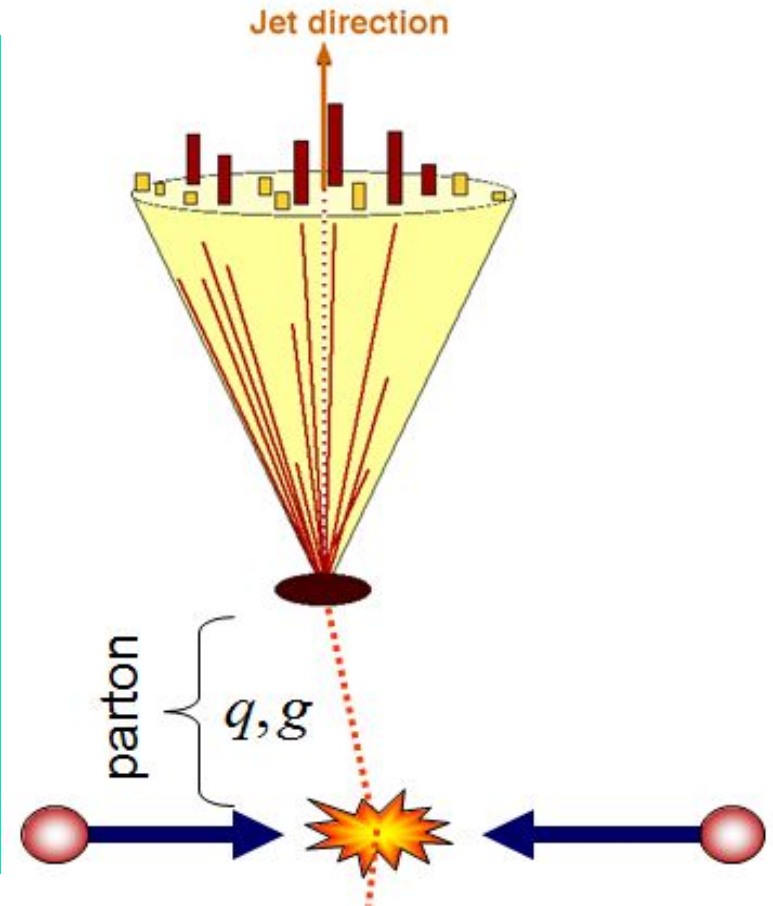


CMS Experiment at LHC, CERN  
Data recorded: Sun Nov 14 19:31:39 2010 CEST  
Run/Event: 151076 / 1328520  
Lumi section: 249



# What is a jet?

- At LO pQCD, jet  $\approx$  parton.
- A jet is a spray of final-state particles roughly moving in the same direction and defined by jet finding algorithms.
- In pQCD local-parton-hadron duality (LPHD) is used; more precise calculations.



$$E_T = \sum_{i \in \text{jet}} E_{T,i}$$

$$y = \sum_{i \in \text{jet}} y_i E_{T,i} / E_T$$

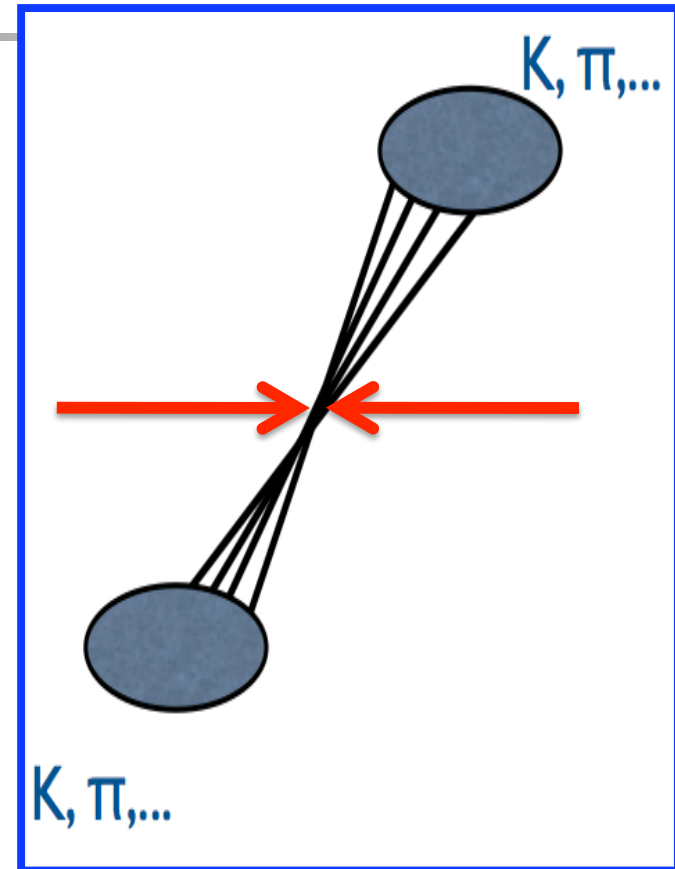
$$\phi = \sum_{i \in \text{jet}} \phi_i E_{T,i} / E_T$$

$$R_{ij} = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}$$



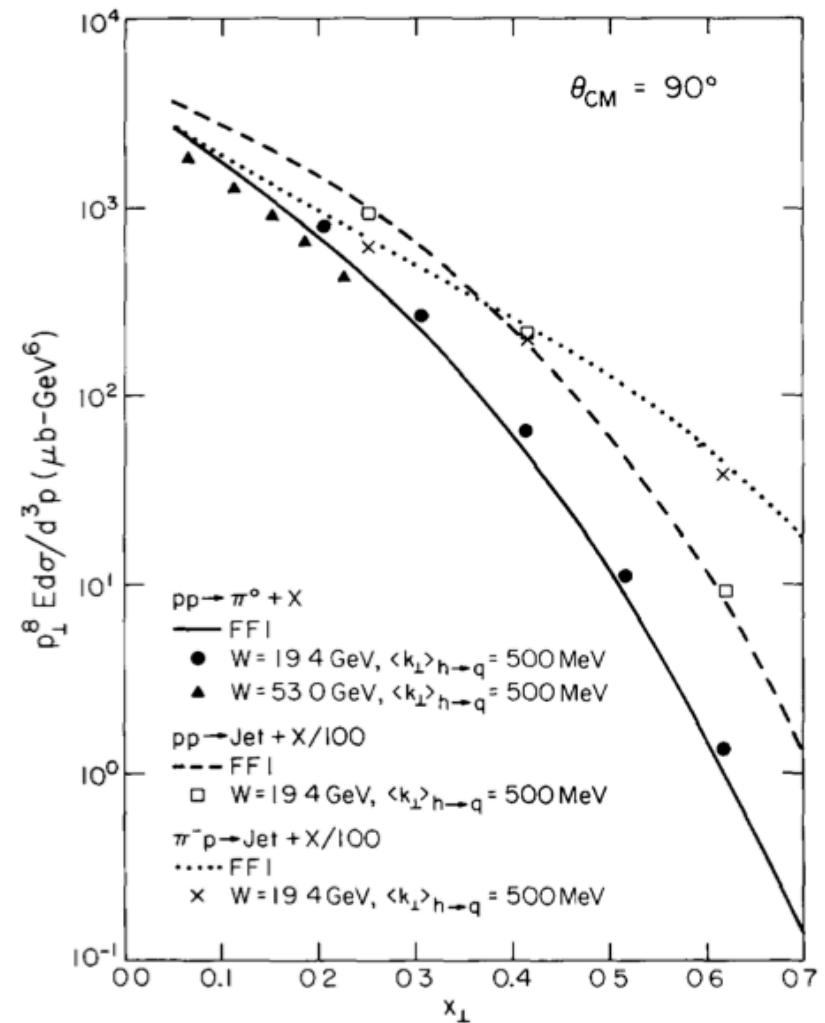
# Briefing: jets at HEP

- Stermann & Weinberg ('77) defined a two-jet event and made an analytic calculation.
- Feynman, Field, Fox ('77) made a numerical calculation of the inclusive jet prod.
- Discovery of three-jet events in  $e^+e^-$  gave a first evidence of gluons.
- Precise extraction of  $\alpha_s$  is made by measuring jet event shapes.
- New physics beyond Standard Model by studying jets.



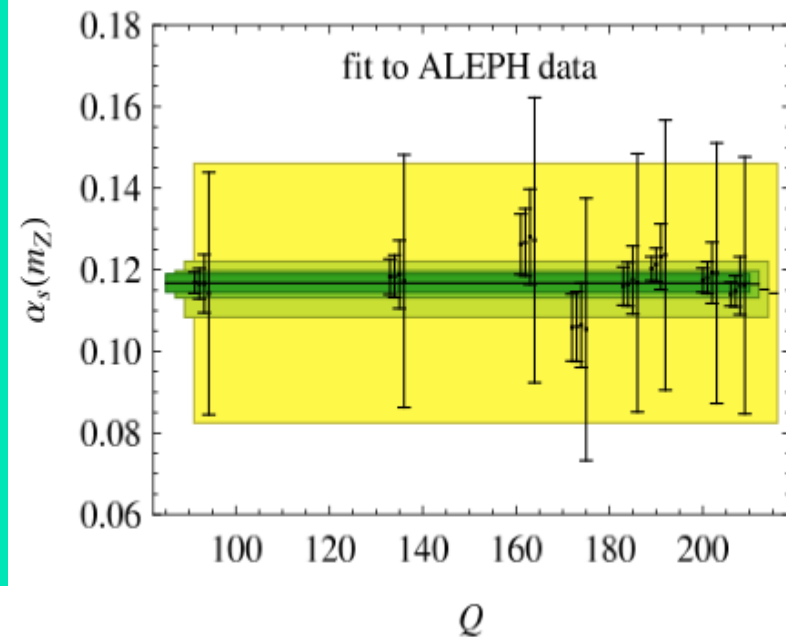
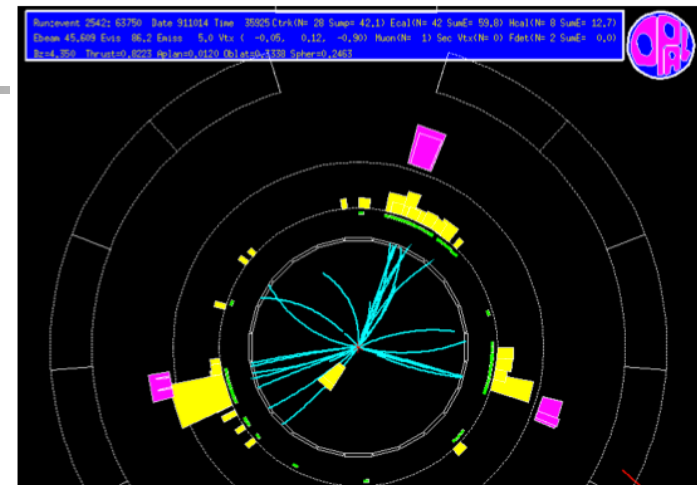
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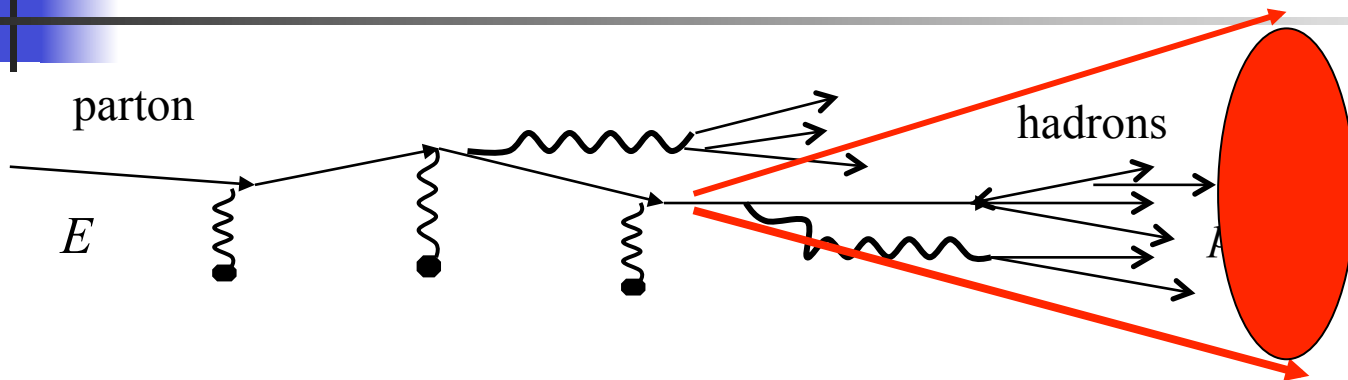


# Briefing: jets at HEP

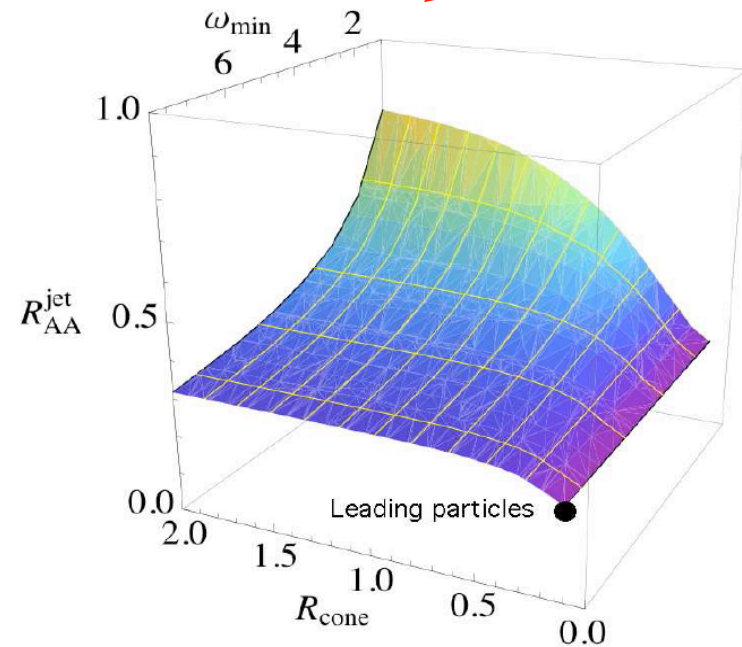
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# How a "jet" quenches in HIC?



- Radiated gluon can fall inside the jet area.
- Two leverage variables: jet size  $R$  & minimum momentum cut  $p_{T_{\min}}$ .





# Full jets in HIC

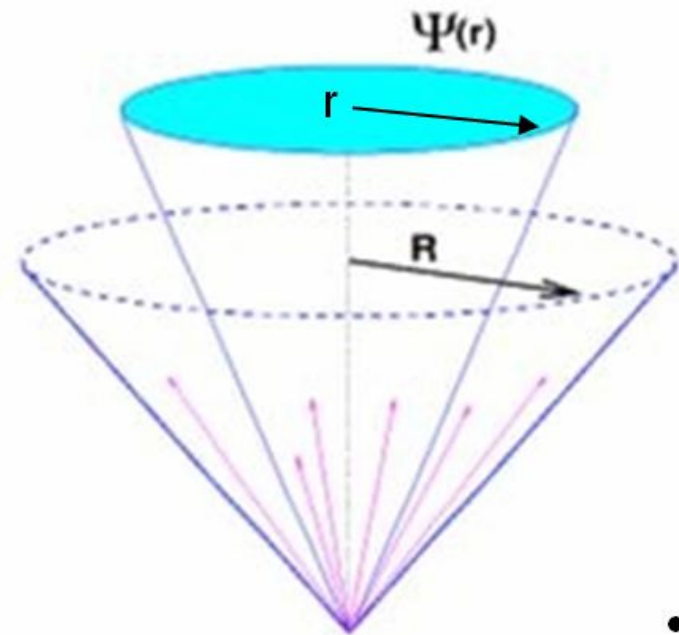
- 1) jet shape
- 2) inclusive jet spectrum
- 3) tagged jet production
- 4) dijet correlation

# Jet shape in HIC

$$\Psi_{\text{int}}(r; R) = \frac{\sum_i (E_T)_i \Theta(r - (R_{\text{jet}})_i)}{\sum_i (E_T)_i \Theta(R - (R_{\text{jet}})_i)},$$

$$\psi(r; R) = \frac{d\Psi_{\text{int}}(r; R)}{dr}.$$

$$\Psi_{\text{int}}(r = R, R) = 1$$



I Vitev, S Wicks, BWZ,

JHEP 0811,093 (2008); EPJC 62, 139 (2009).

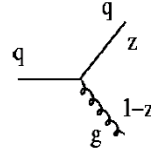
# LO & Resummation: p+p

An analytic approach to the energy distribution of jet

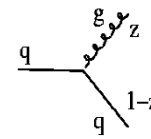
Seymour, M. (1998)

Jet shape at LO with the acceptance cut

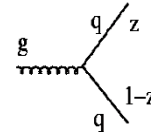
$$\psi_a(r; R) = \sum_b \frac{\alpha_s}{2\pi} \frac{2}{r} \int_{z_{min}}^{1-Z} dz z P_{a \rightarrow bc}(z).$$



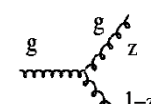
$$P_{qq}^{(1)}(x) = C_2(F) \left[ (1+x^2) \left( \frac{1}{1-x} \right)_+ + \frac{3}{2} \delta(1-x) \right]$$



$$P_{gq}^{(1)}(x) = C_2(F) \frac{(1-x)^2 + 1}{x}$$



$$P_{qg}^{(1)}(x) = T(F) \left[ (1-x)^2 + x^2 \right]$$



$$P_{gg}^{(1)}(x) = 2C_2(A) \left[ \frac{x}{(1-x)_+} + \frac{1-x}{x} + x(1-x) \right] + \left( \frac{11}{6} C_2(A) - \frac{2}{3} T(F) n_f \right) \delta(1-x),$$

$$z_{min} = \omega^{min} / E_T$$

Collinear divergence requires Sudakov resummation:

$$P(< r) = \exp(-P_1(> r)) = \exp\left(-\int_r^R dr' \psi_{coll}(r')\right)$$

$$\psi_{RS}(r) = \frac{dP(r)}{dr}$$

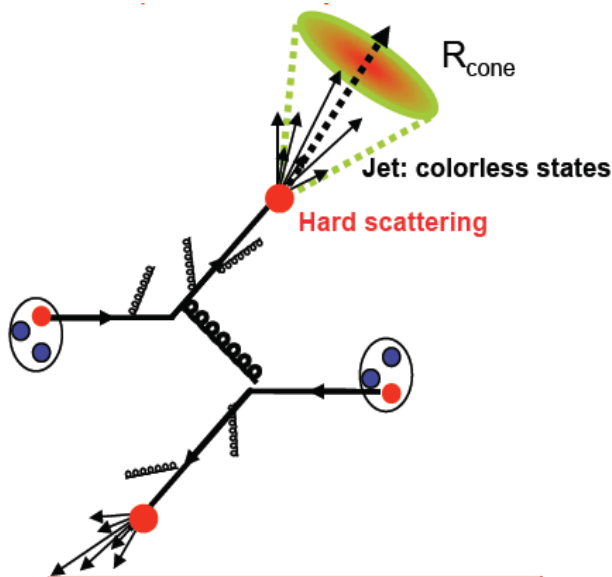
# Power corr. & IS radia.

- Power correction: include running coupling inside the  $z$  integration and integrate over the Landau pole.

$$\bar{\alpha}_0'(Q_0, k_{min}) = \frac{1}{Q_0} \int_{k_{min}}^{Q_0} dk \alpha_s(k)$$

non-perturbative scale  $Q_0$ .

$$\bar{\alpha}_0'(2 \text{ GeV}, 0) = 0.52, \quad \bar{\alpha}_0'(3 \text{ GeV}, 0) = 0.42$$



- Initial-state radiation should be included, which gives:

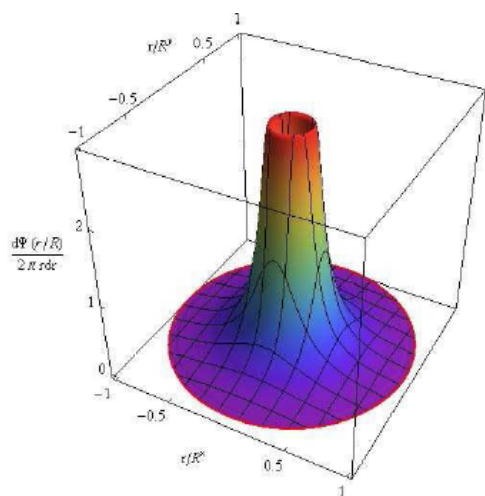
$$\psi_i(r) = \frac{C\alpha_s}{2\pi} 2r \left( \frac{1}{Z^2} - \frac{1}{(1 - z_{min})^2} \right)$$



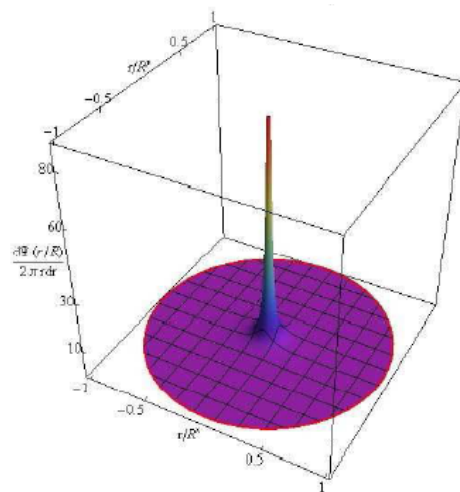
# Jet shape p+p: baseline

$$\psi(r) = \psi_{\text{coll}}(r) (P(r) - 1) + \psi_{\text{LO}}(r) + \psi_{i,\text{LO}}(r) + \psi_{\text{PC}}(r) + \psi_{i,\text{PC}}(r),$$

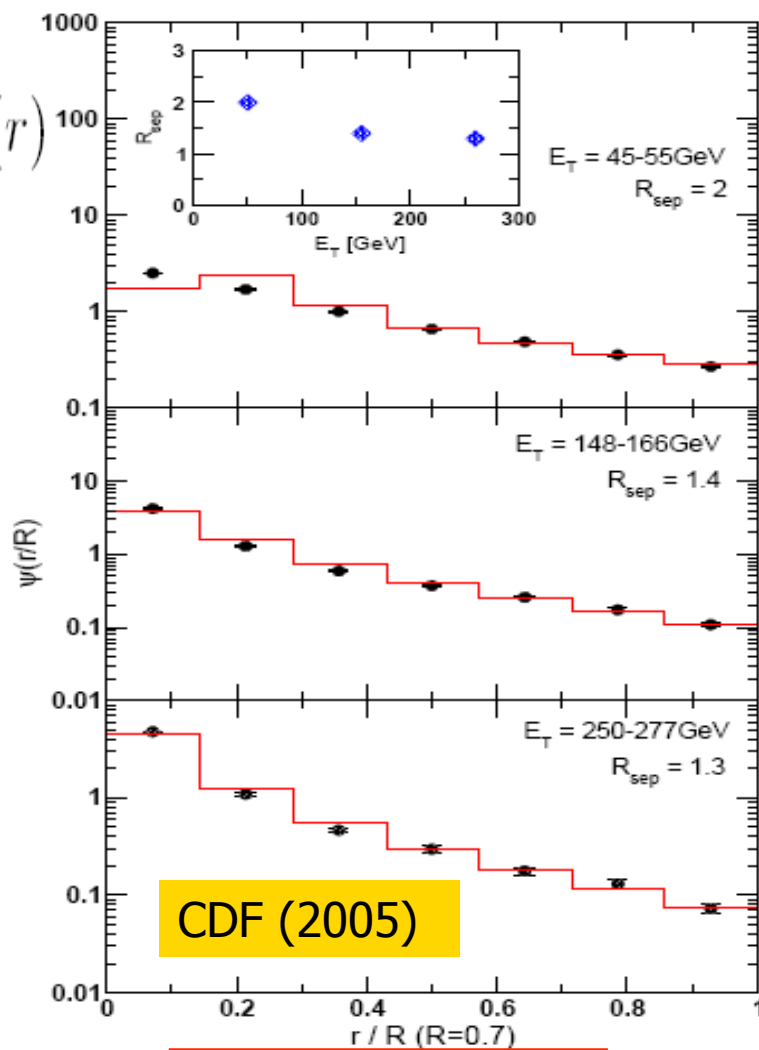
20 GeV



500 GeV

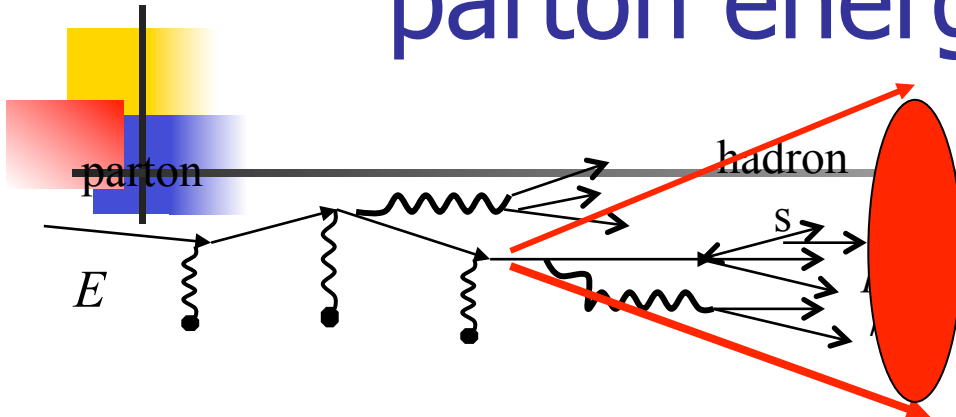


LHC



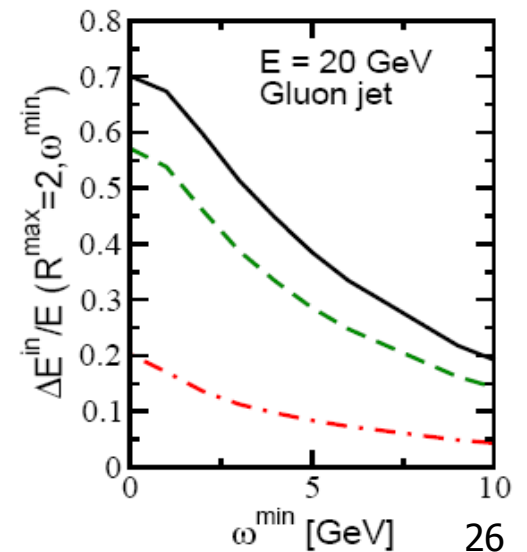
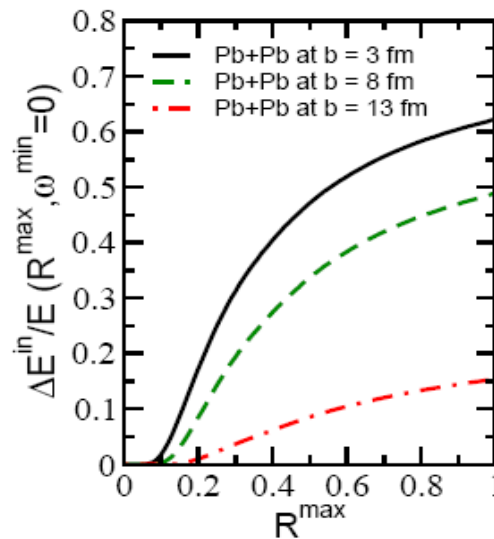
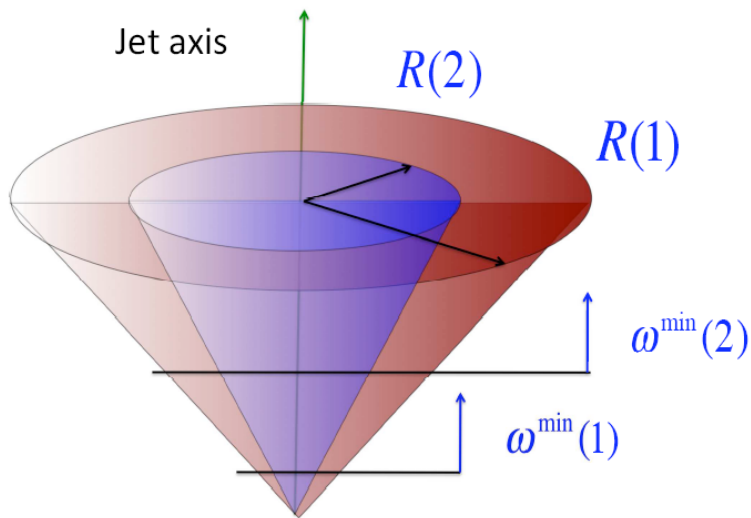
$\sqrt{s} = 1960 \text{ GeV}$

# parton energy loss in QGP



Gyulassy-Levai-Vitev

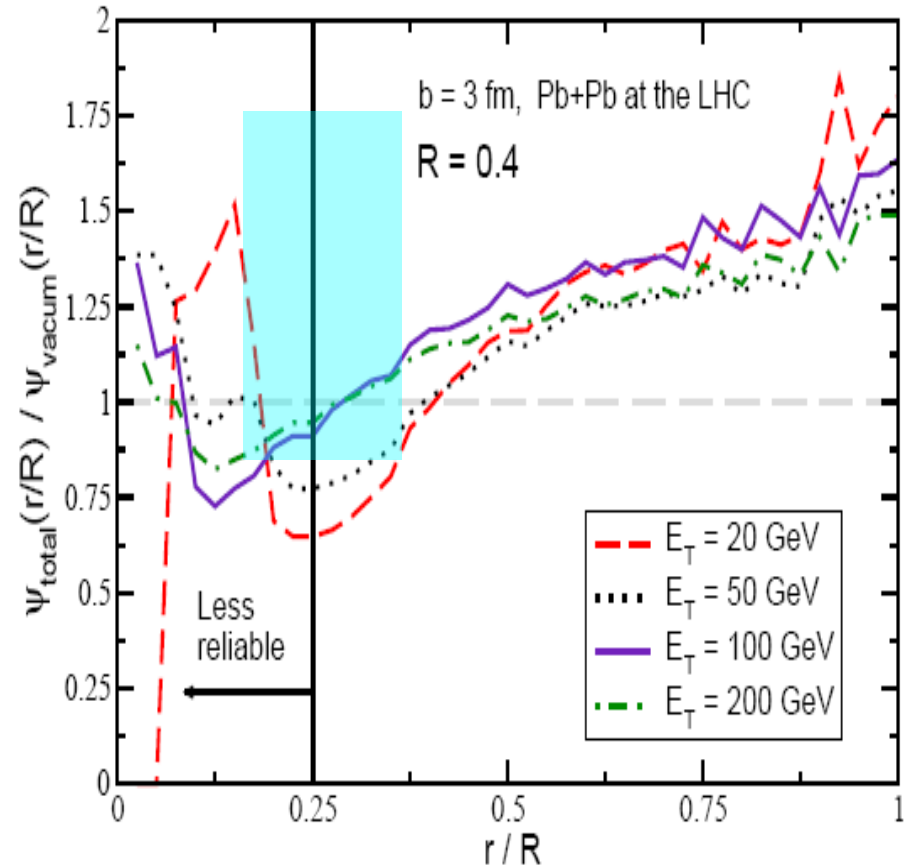
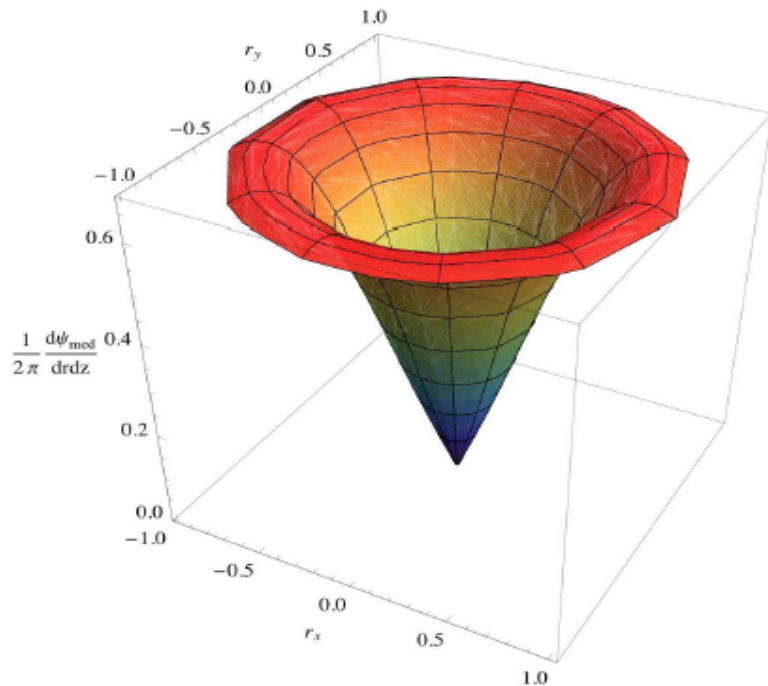
$$\frac{\Delta E^{in}}{E}(R^{\max}, \omega^{\min}) = \frac{1}{E} \int_{\omega^{\min}}^E d\omega \int_0^{R^{\max}} dr \frac{dI^g}{d\omega dr}(\omega, r)$$



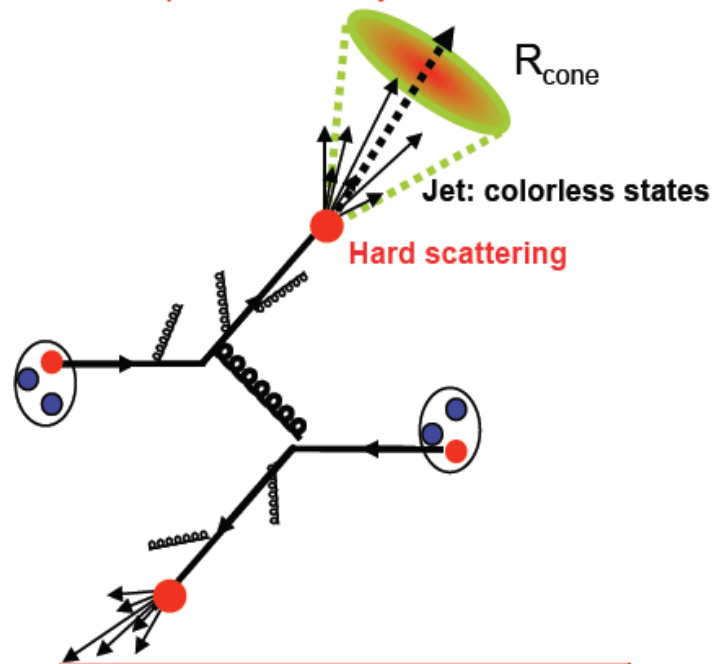
# Total jet shape in HIC

- Medium-induced jet shape is much broader than the jet shape in p+p

$$\psi_{\text{tot.}}(r/R) = \frac{1}{\text{Norm}} \int_{\epsilon=0}^1 d\epsilon \sum_{q,g} P_{q,g}(\epsilon) \frac{1}{(1 - (1 - f_{q,g}) \cdot \epsilon)^3} \times \frac{\sigma_{q,g}^{NN}(R, \omega^{\min})}{d^2 E'_T dy} \left[ (1 - \epsilon) \psi_{\text{vac.}}^{q,g}(r/R) + f_{q,g} \cdot \epsilon \psi_{\text{med.}}^{q,g}(r/R) \right]$$



# Inclusive jet cross section in HIC at NLO



I Vitev, BWZ, PRL 104,132001 (2010), arXiv: 0910.1090.

# Jet cross section at NLO in p+p

- Jet cross sections at NLO in p+p :

$$\begin{aligned} \frac{d\sigma^{\text{jet}}}{dE_T dy} &= \frac{1}{2!} \int d\{E_T, y, \phi\}_2 \frac{d\sigma[2 \rightarrow 2]}{d\{E_T, y, \phi\}_2} S_2(\{E_T, y, \phi\}_2) \\ &+ \frac{1}{3!} \int d\{E_T, y, \phi\}_3 \frac{d\sigma[2 \rightarrow 3]}{d\{E_T, y, \phi\}_3} S_3(\{E_T, y, \phi\}_3) \end{aligned}$$

- Function  $S_2$  and  $S_3$  contain jet find algorithm:

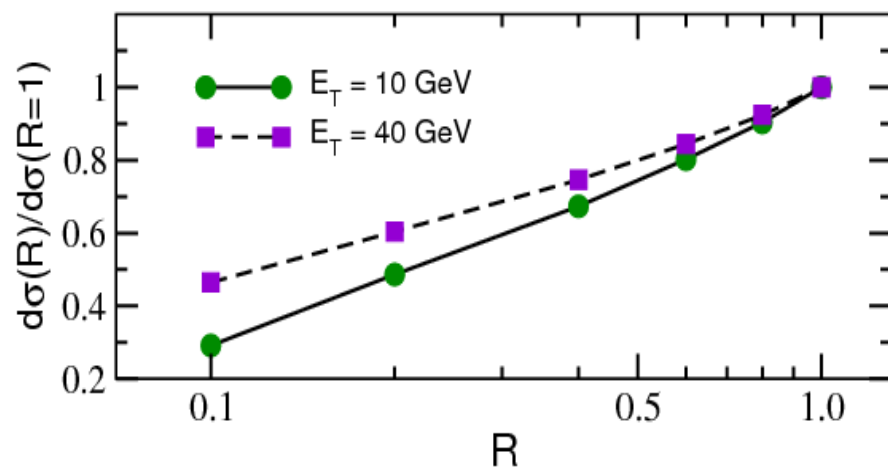
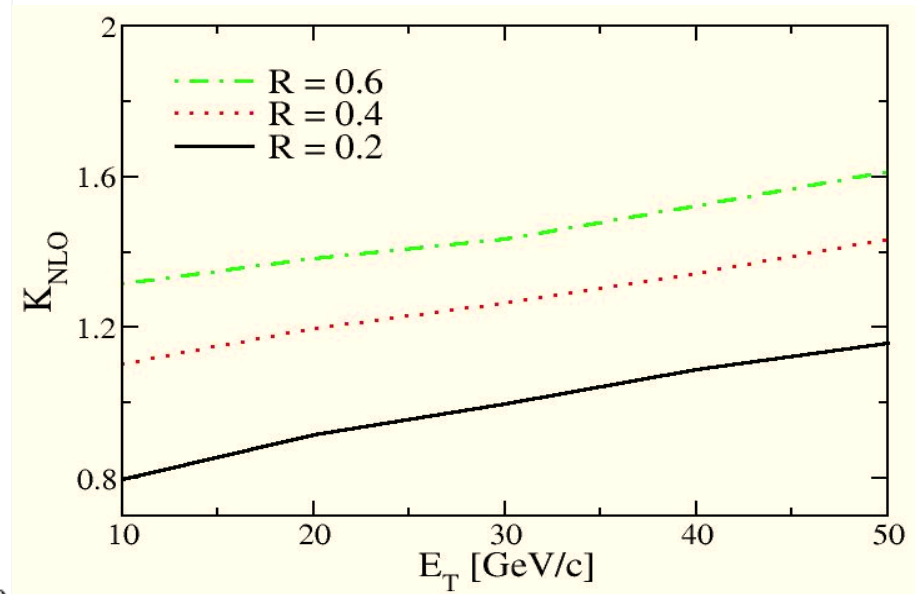
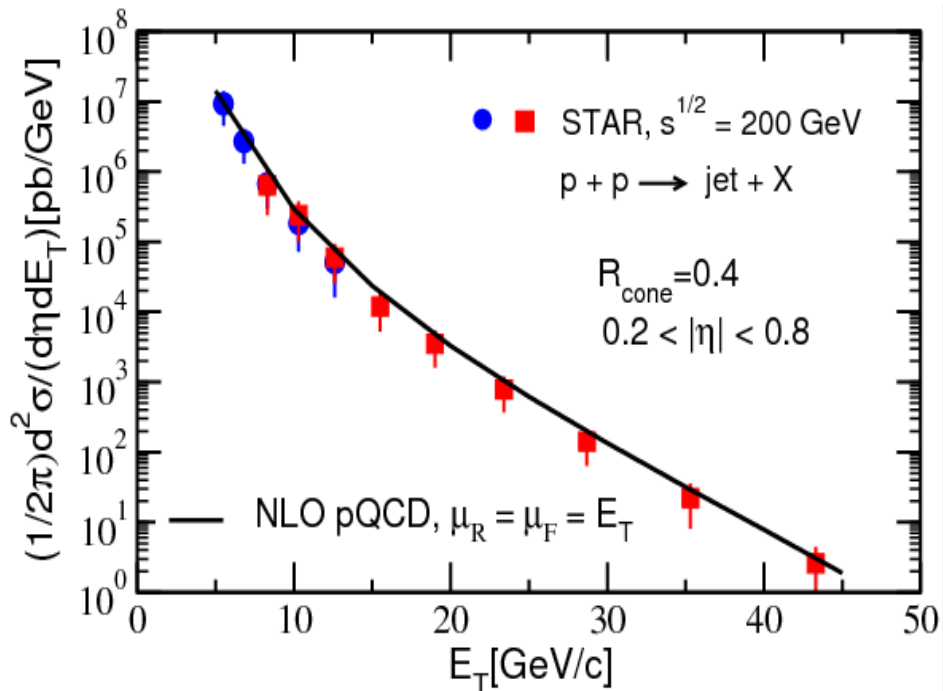
2  $\rightarrow$  2

$$S_2 = \sum_{i=1}^2 S(i) = \sum_{i=1}^2 \delta(E_{T_i} - E_T) \delta(y_i - y)$$

2  $\rightarrow$  3

$$\begin{aligned} S_3 &= \sum_i \delta(p_i - p_J) \delta(y_i - y_J) \prod_{j(j \neq i)} \theta \left( R_{ij} > \frac{p_i + p_j}{\max(p_i, p_j)} R \right) \\ &+ \sum_{i,j(i < j)} \delta(p_i + p_j - p_J) \delta \left( \frac{p_i y_i + p_j y_j}{p_i + p_j} - y_J \right) \theta(R_{ij} < R_{\text{rc}}) \end{aligned}$$

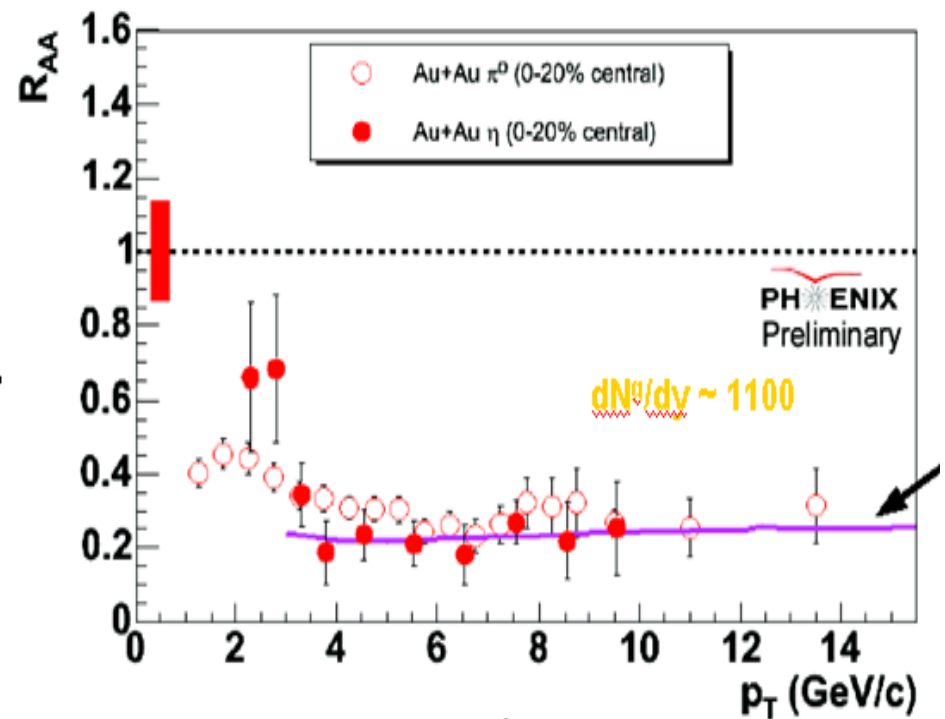
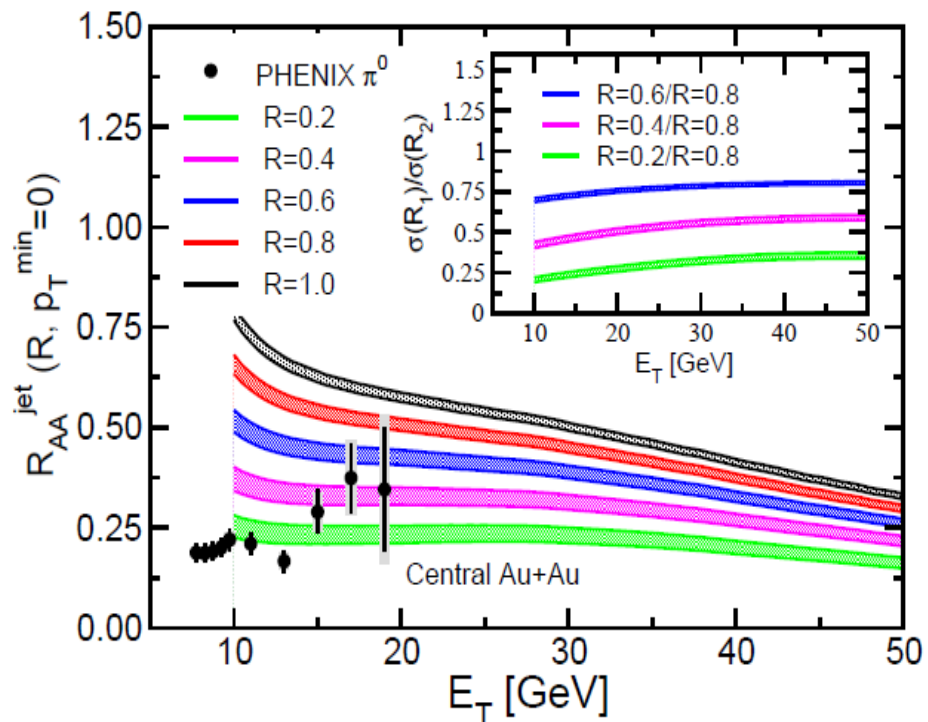
# Jets in p+p at RHIC



- Very good agreement between data and theory is achieved;
- $K_{\text{NLO}} = \text{NLO}/\text{LO}$  can be smaller than 1 at small cone radius.

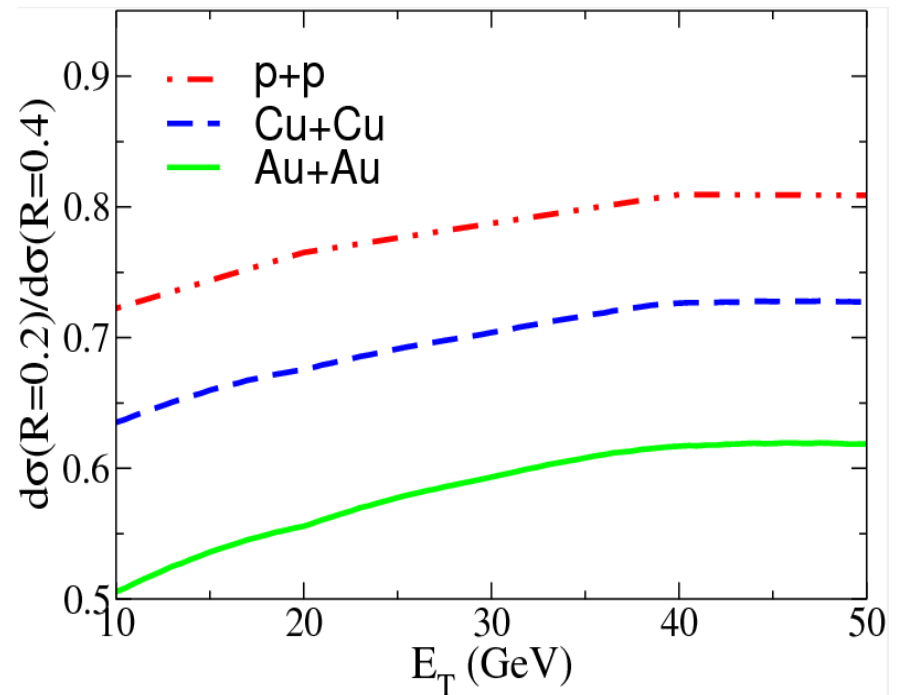
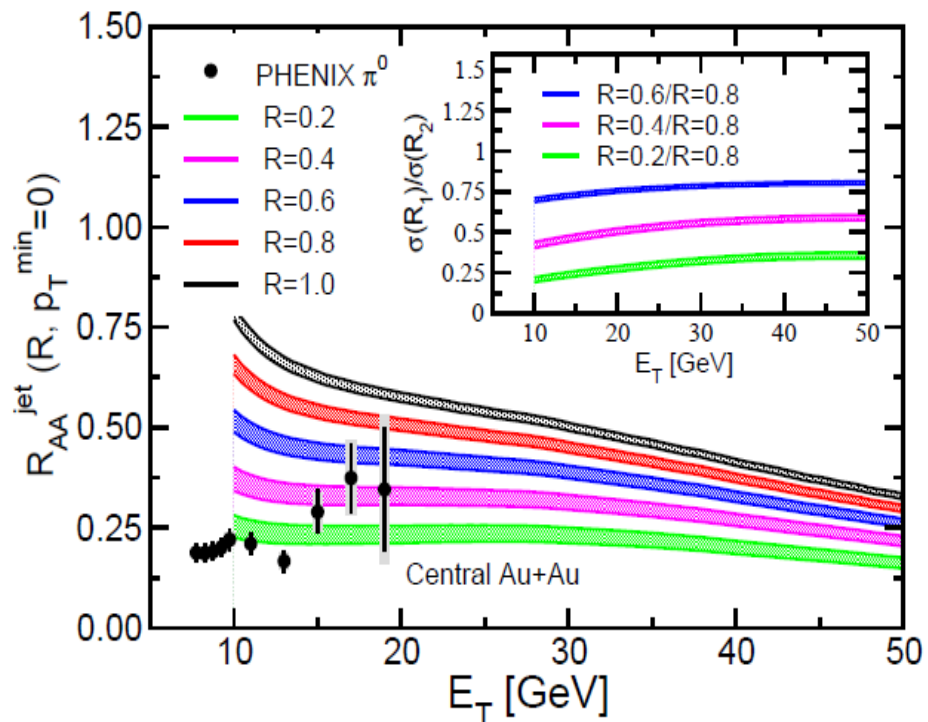
# Inclusive jets in A+A at RHIC

- $R_{AA}$  for inclusive jets evolves continuously with cone size  $R$ ;
- Ratios of jet cross sections at different  $R$  in p+p, Cu+Cu and Au+Au have a similar trend with different magnitudes.



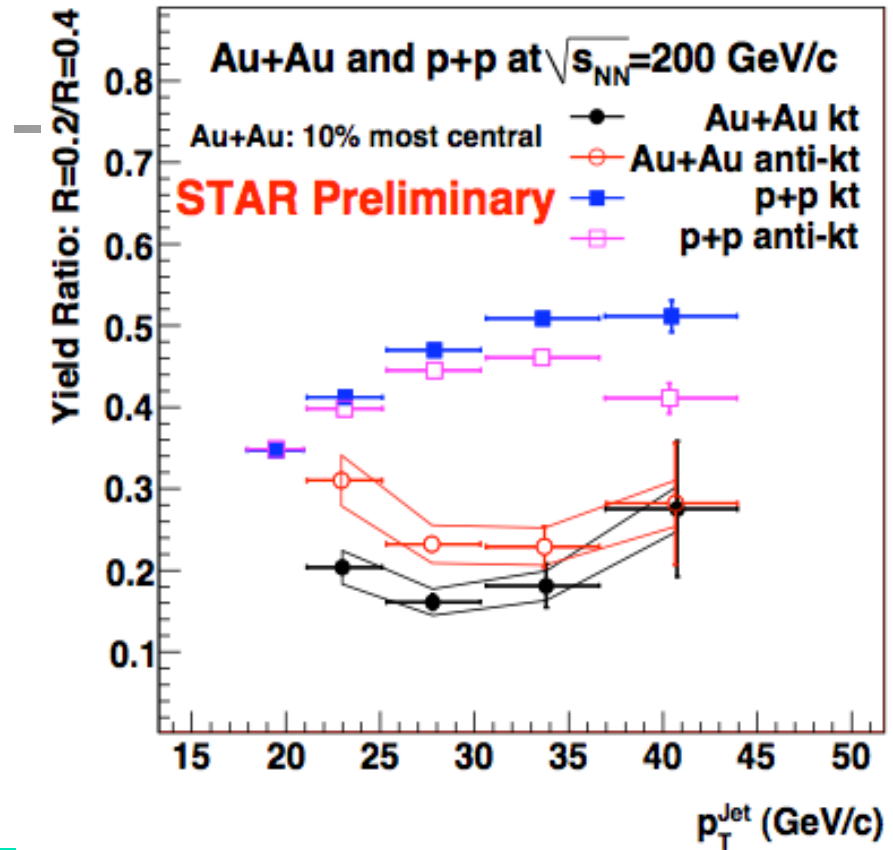
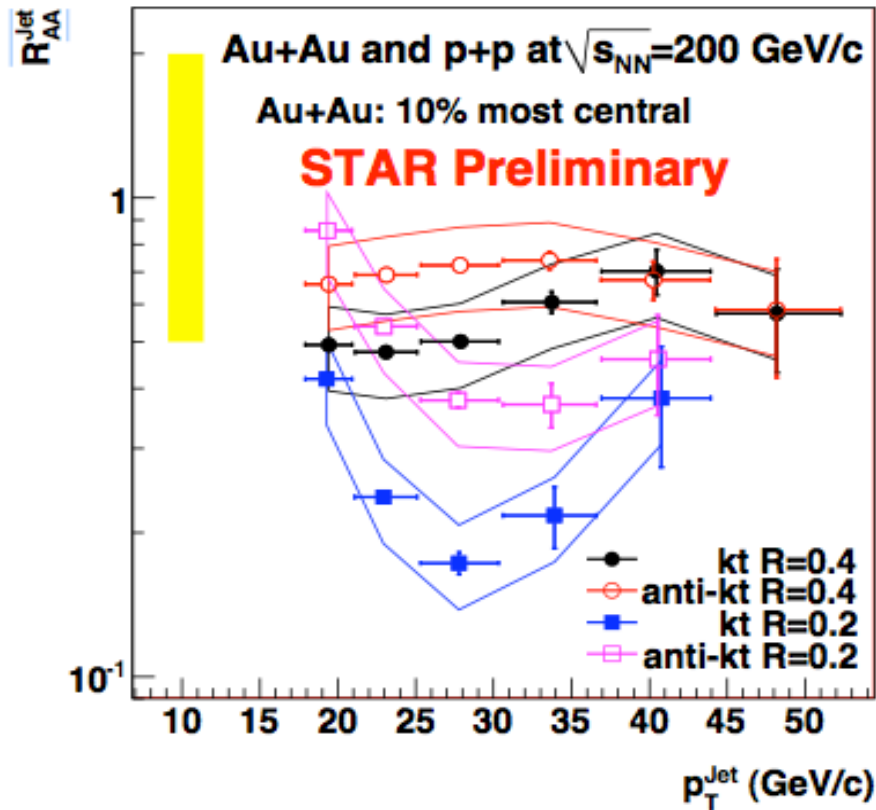
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# Jet measuring at RHIC

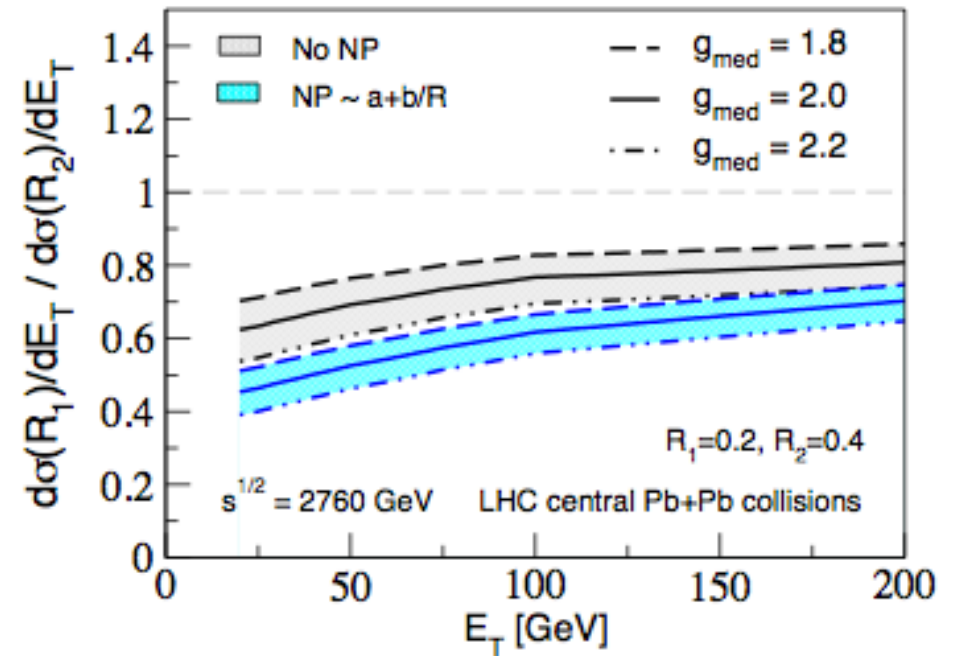
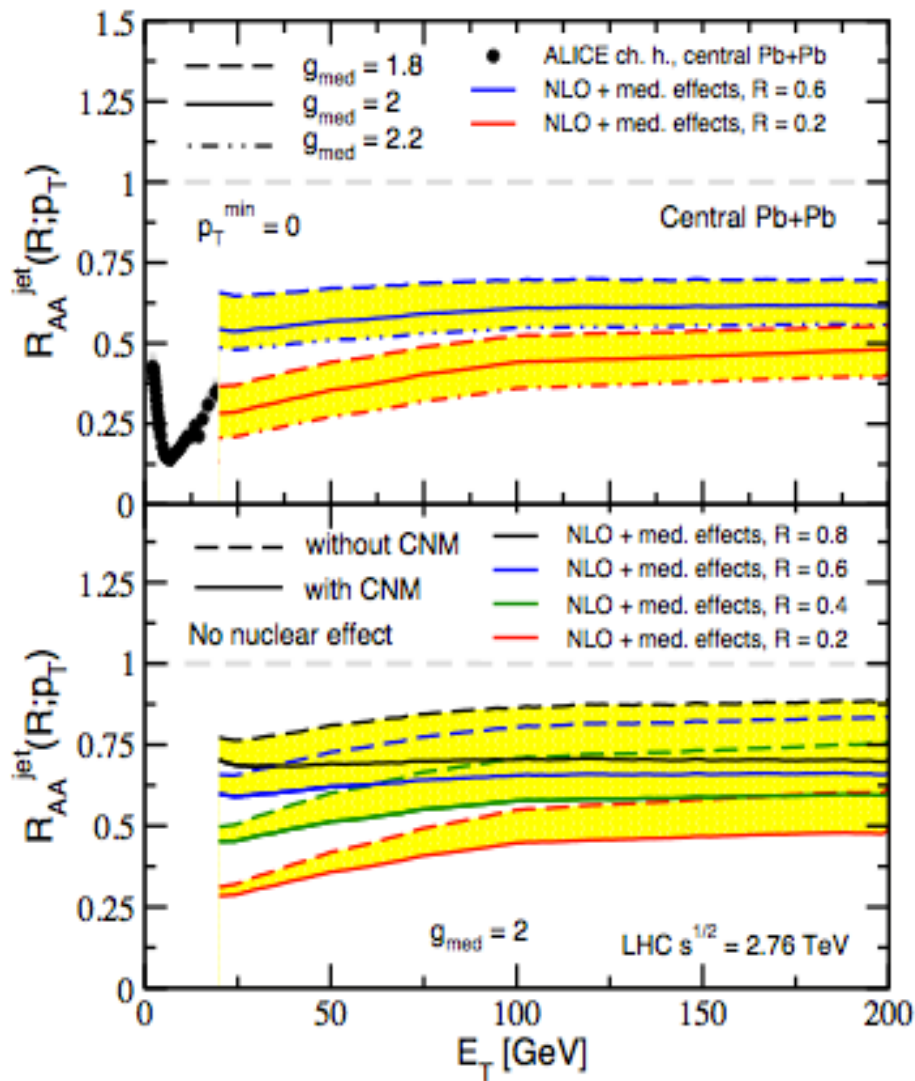


## Jets in Au+Au by STAR

M. Poloszkon et al, (2010)

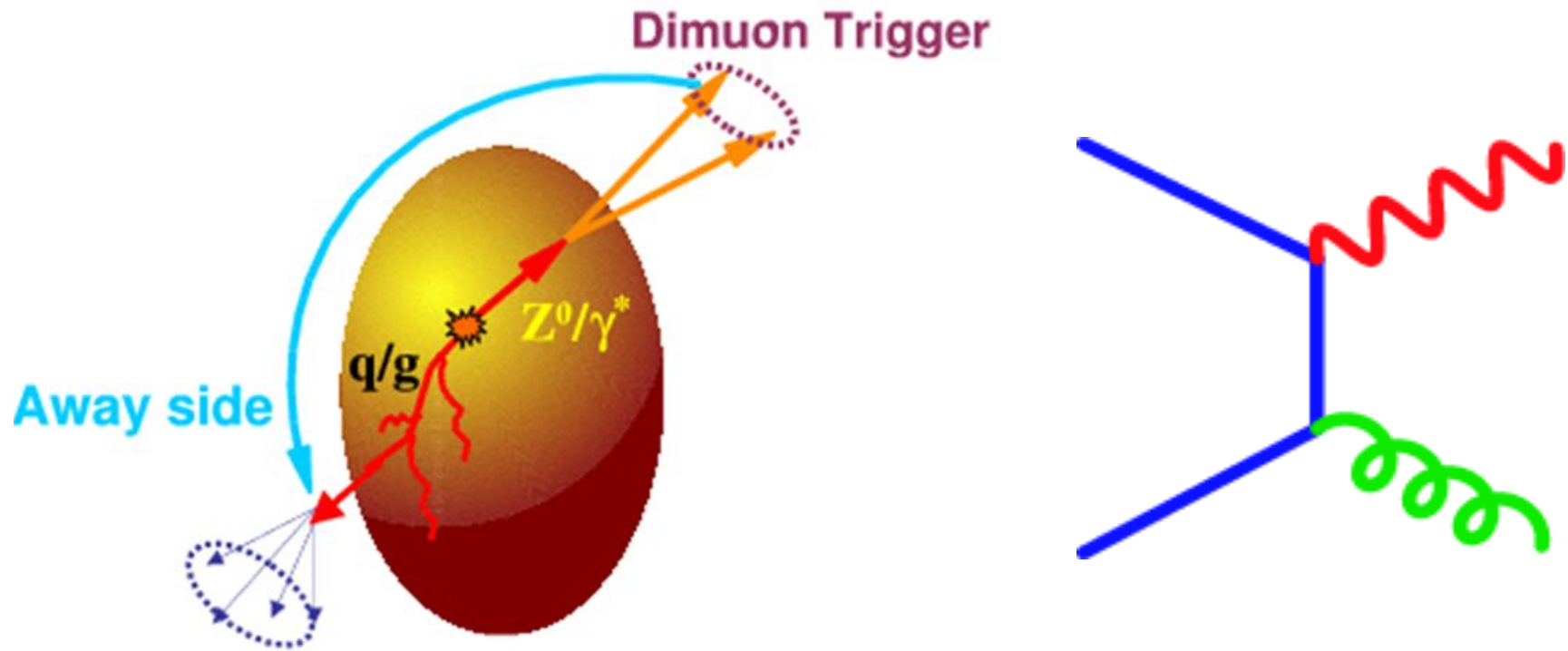
S. Salur et al, (2010)

# Inclusive jets in Pb+Pb at LHC



Y He, Vitev, BWZ, arXiv:1105.2566

# Tagged jet production in HIC at NLO



Neufeld, Vitev, BWZ, PRC 83, 034902 (2011).

# Tagged jet production in HIC

photon + jet

$Z^0$  + jet

- Advantage: large yield
- Disadvantage: final-state effects

Dai, Vitev, BWZ, in progress

- Disadvantage: small cross section
- Advantage: no final-state effects

Neufeld, Vitev, BWZ, PRC (2011)

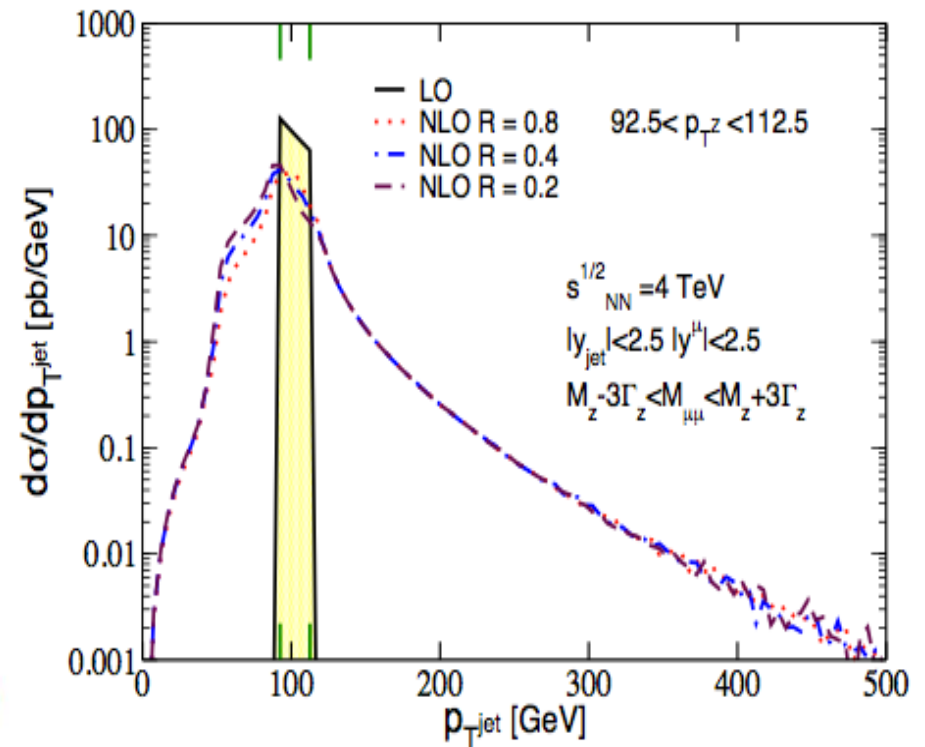
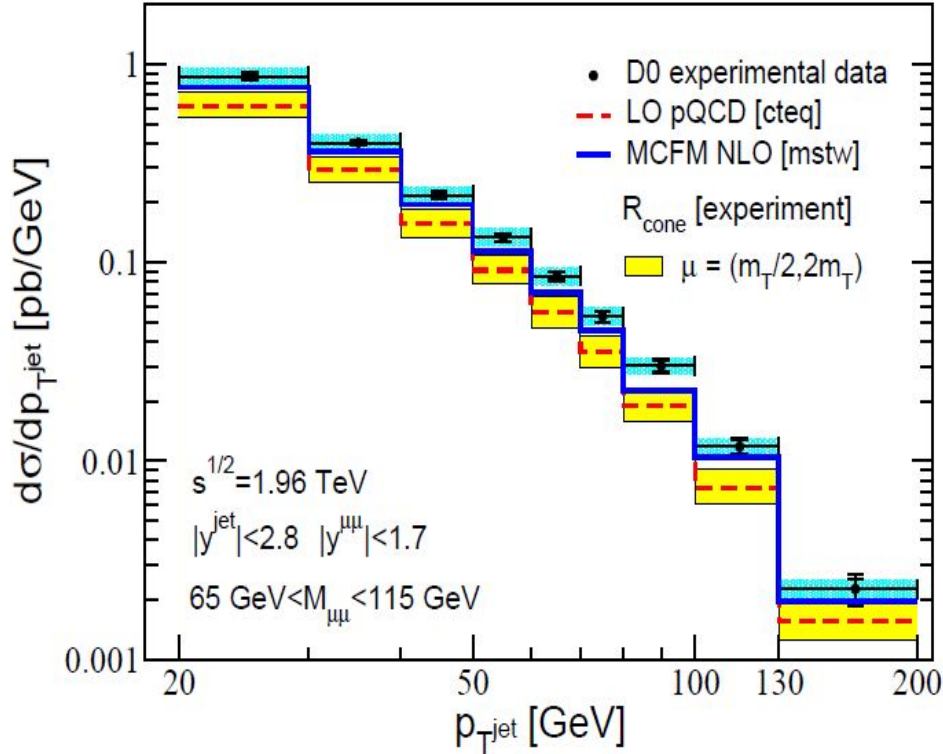


You are so light, I am too heavy.

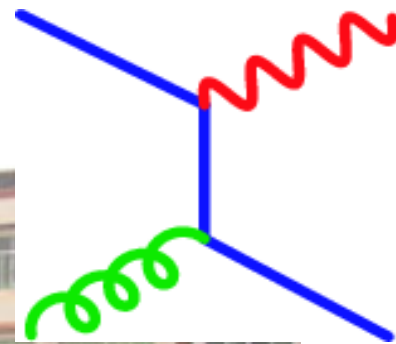
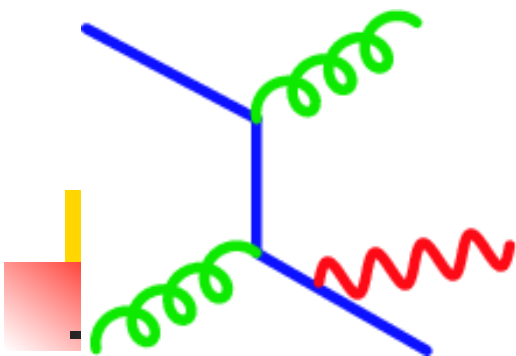


# $Z^0 + \text{jet}$ in $h+h$

- NLO pQCD gives a good description of the data at D0
- The momentum balance is broken due to NLO contribution



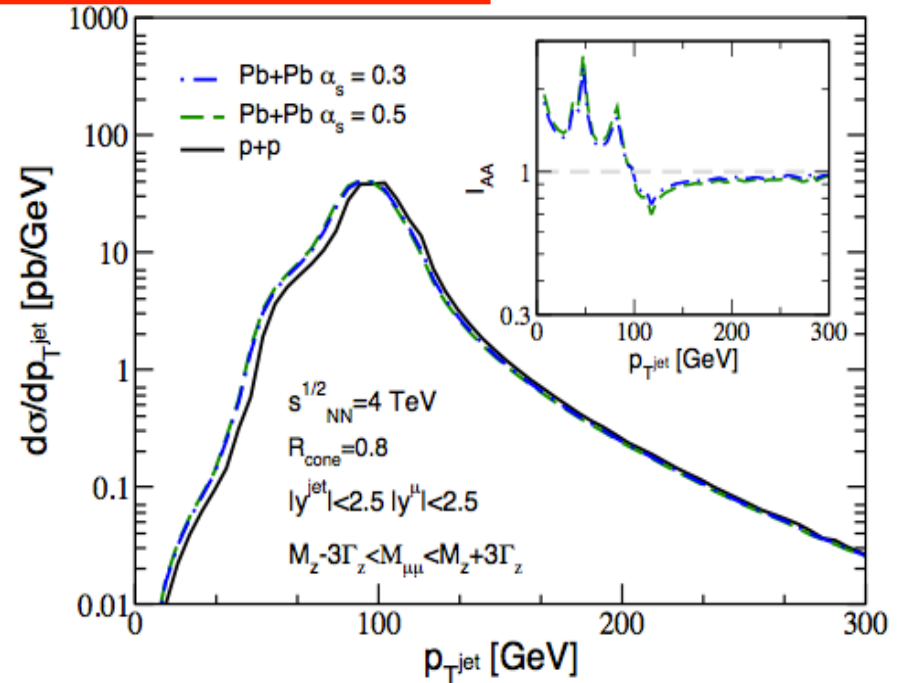
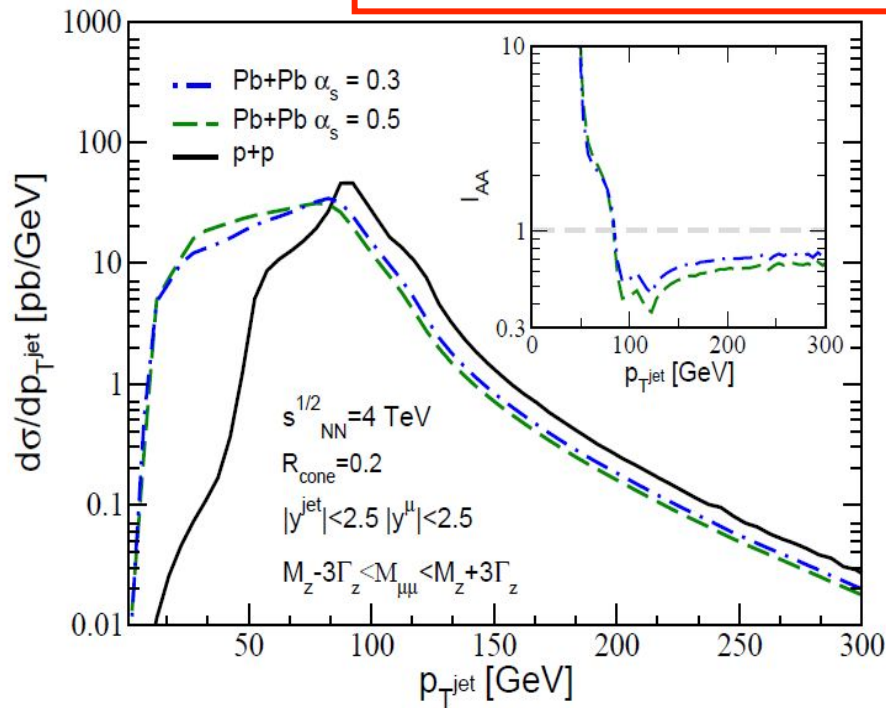
$$p_T \in (92.5 \text{ GeV}, 112.5 \text{ GeV})$$



# $Z^0 + \text{jet}$ in A+A: $I_{AA}$

- A sharp transition from tagged jet suppression above  $\sim p_T$  of Z to tagged jet enhancement below  $\sim p_T$  of Z

$$I_{AA}^{\text{jet}}(R, \omega_{\min}) = \frac{1}{\langle N_{\text{bin}} \rangle} \frac{d\sigma_{AA}}{dp_T(Z) dp_T(Q)} \bigg/ \frac{d\sigma_{pp}}{dp_T(Z) dp_T(\text{jet})}$$

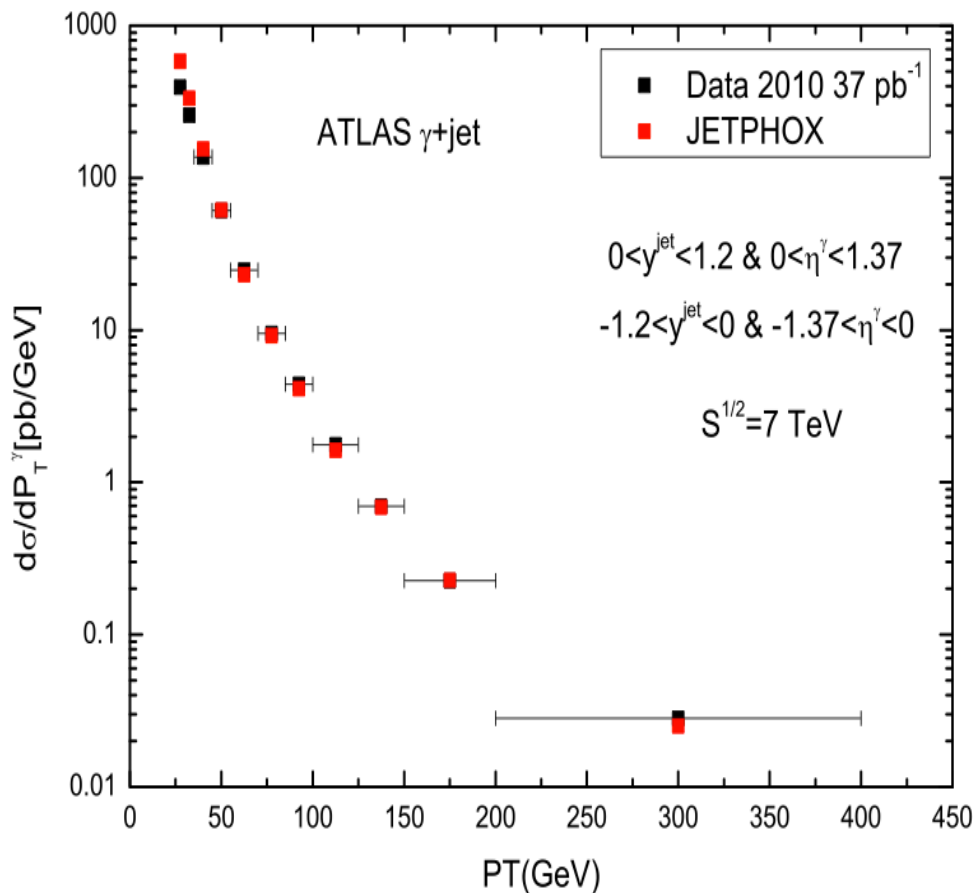


Neufeld, Vitev, BWZ, PRC 83, 034902 (2011).

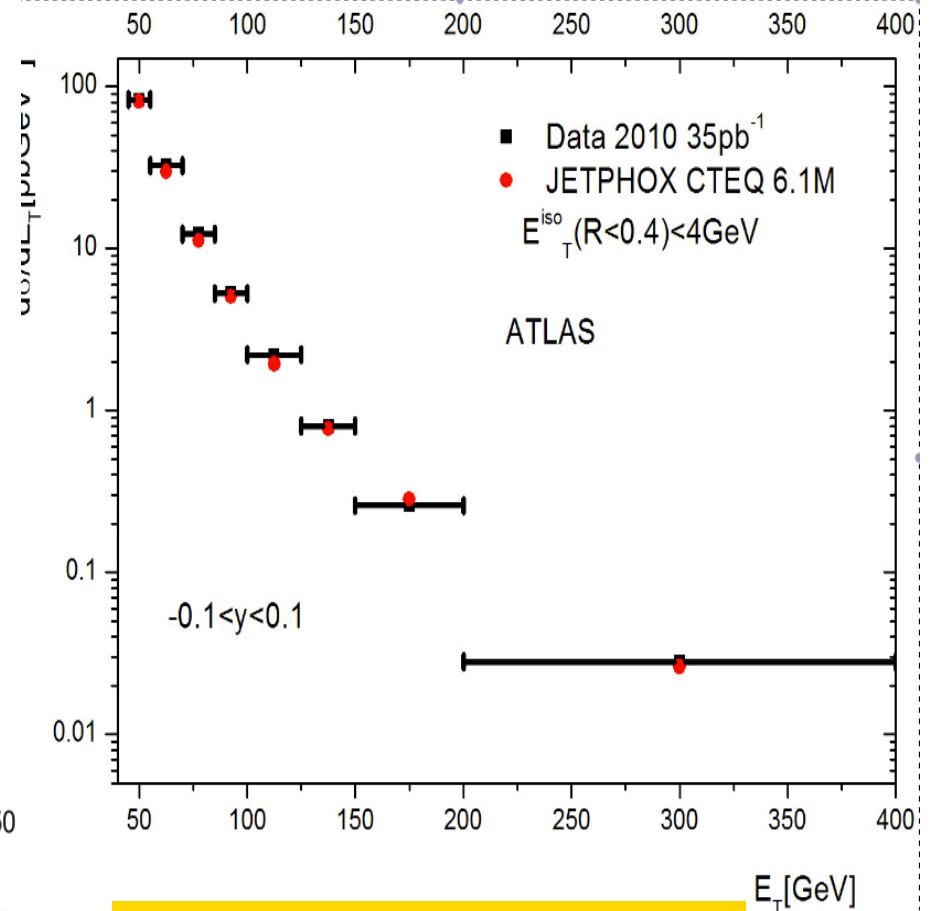
$p_T \in (92.5 \text{ GeV}, 112.5 \text{ GeV})$

# Photon + jet: p+p

- A good baseline for photon+jet in hadron-hadron production has been given by the NLO pQCD.



ATLAS, 1203.3161

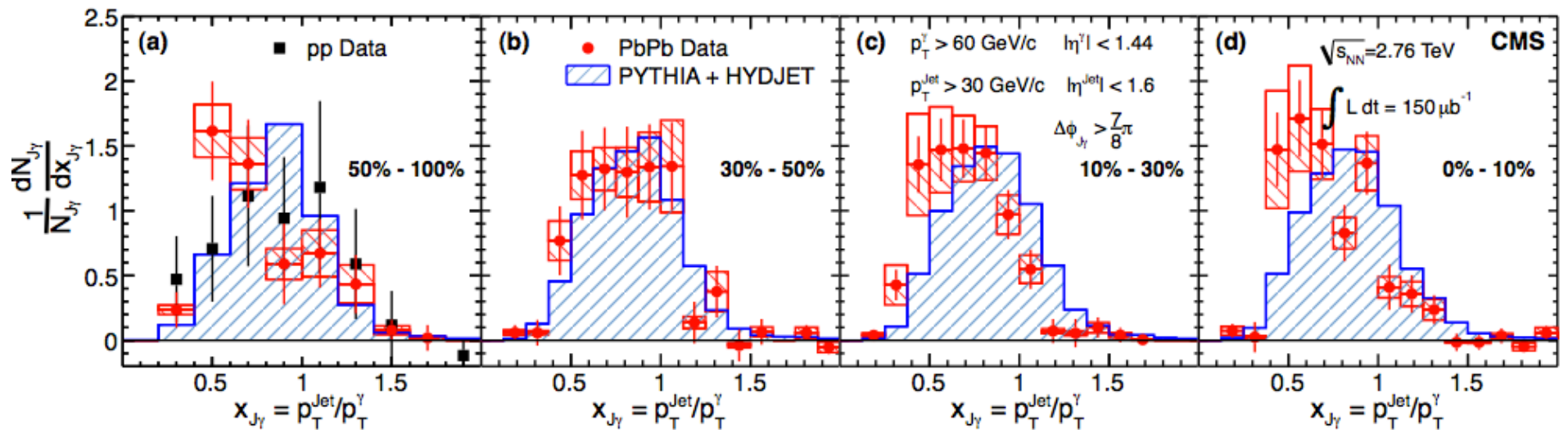


ATLAS, 1012.4389



# Photon + jet: Pb+Pb

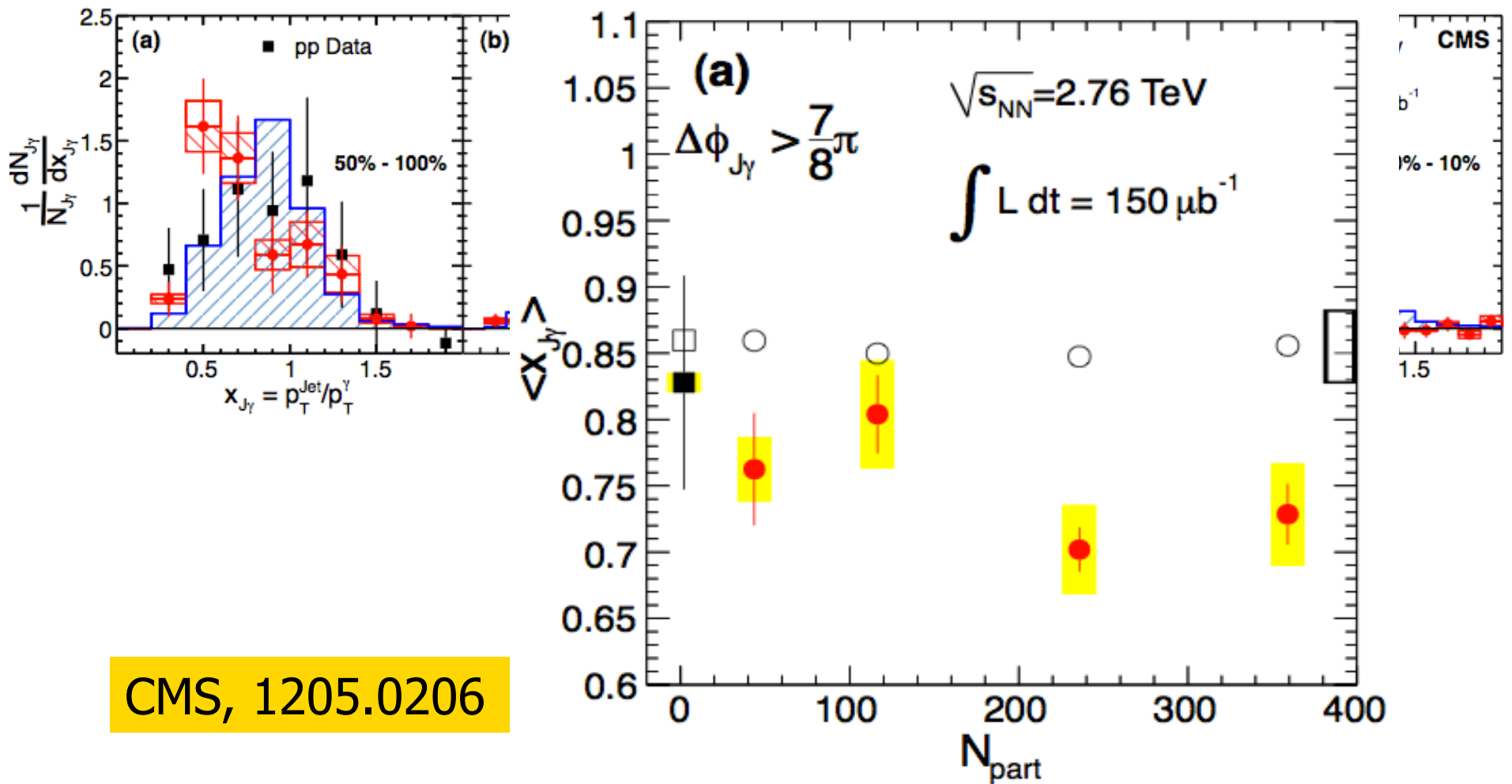
- Latest results of photon tagged jet in HIC have been given by CMS



CMS, 1205.0206

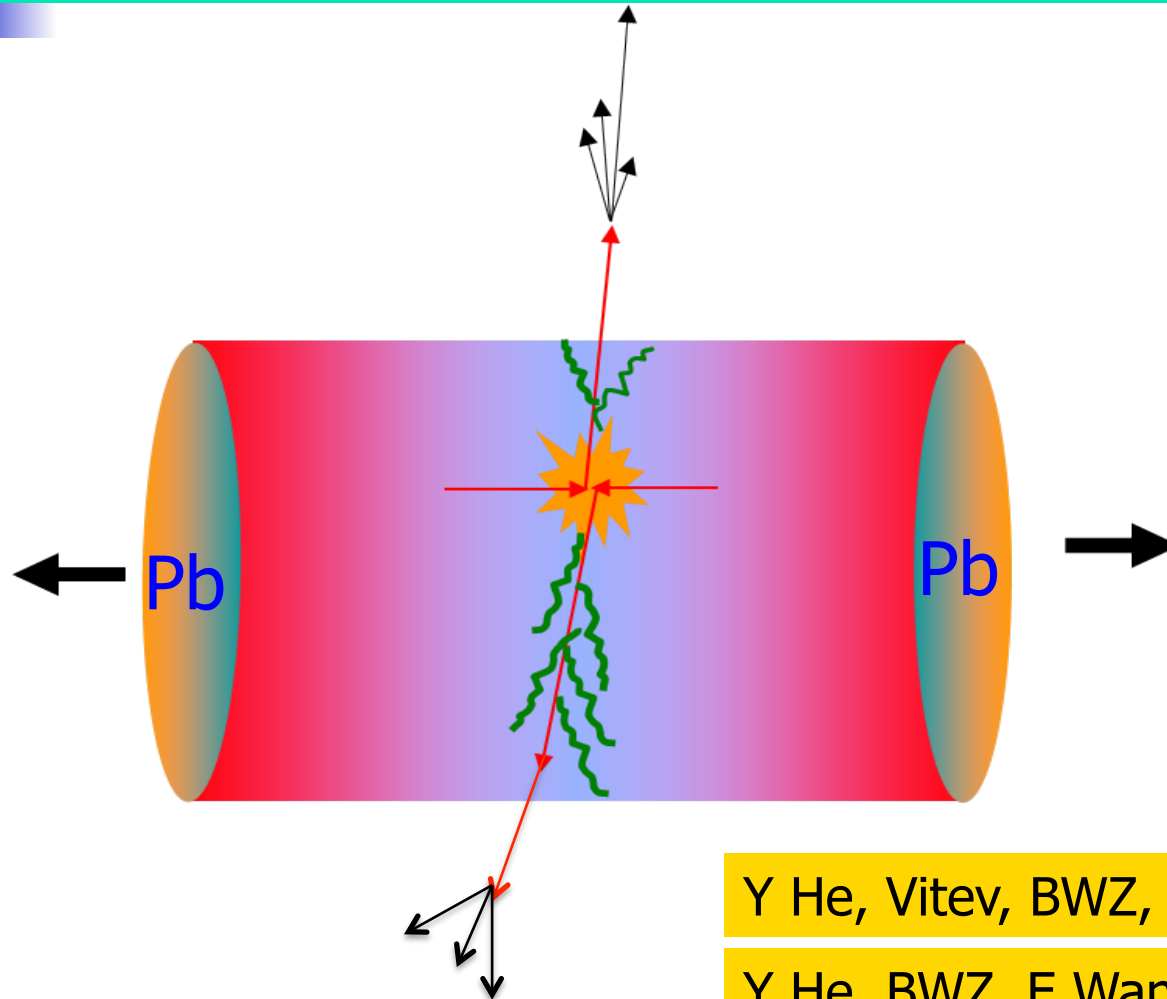
# Photon + jet: Pb+Pb

- Latest results of photon tagged jet in HIC have been given by CMS



CMS, 1205.0206

# Dijet production in HIC at NLO

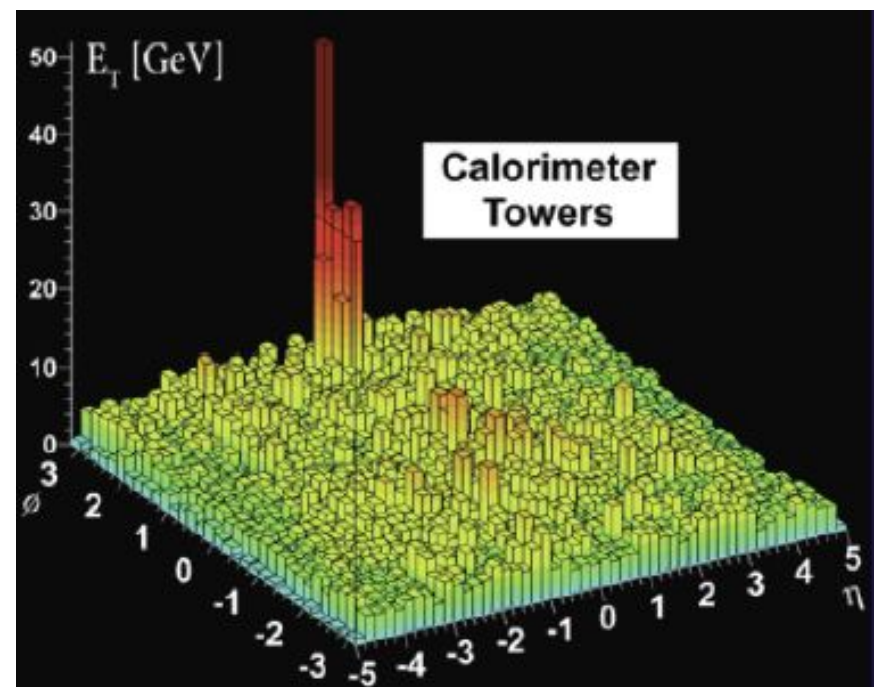
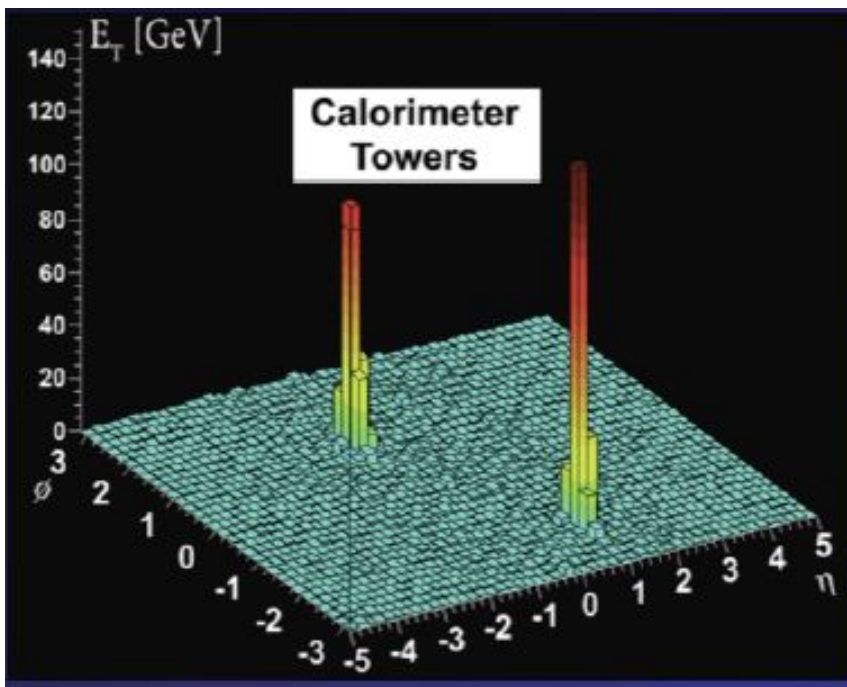


Y He, Vitev, BWZ, arXiv:1105.2566

Y He, BWZ, E Wang, EPJC (2012)

# Measuring Dijets in Pb+Pb

- Jet quenching at LHC has been observed for the first time in dijet productions at Pb+Pb by ATLAS and CMS.

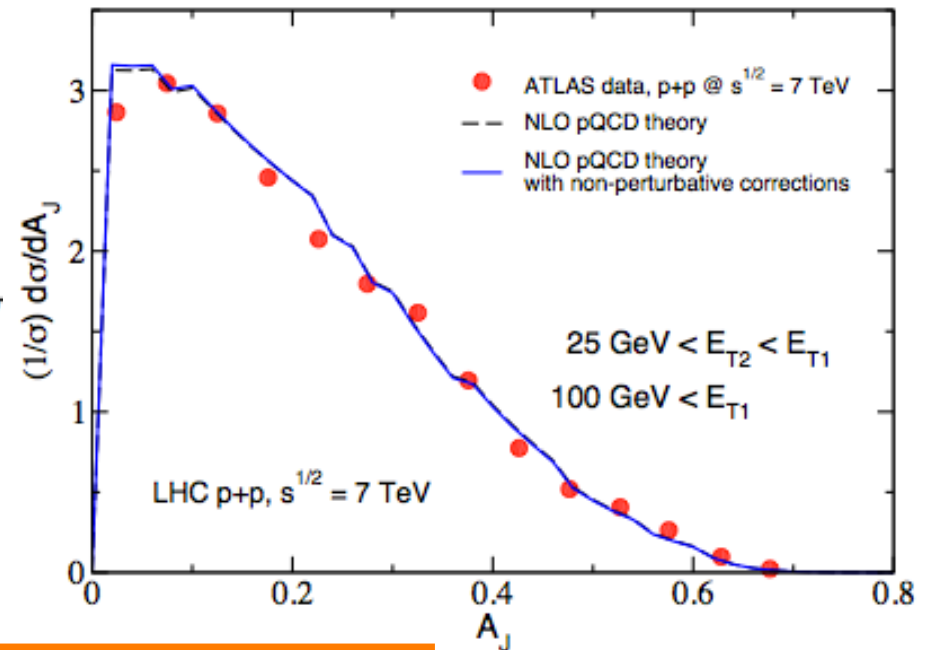
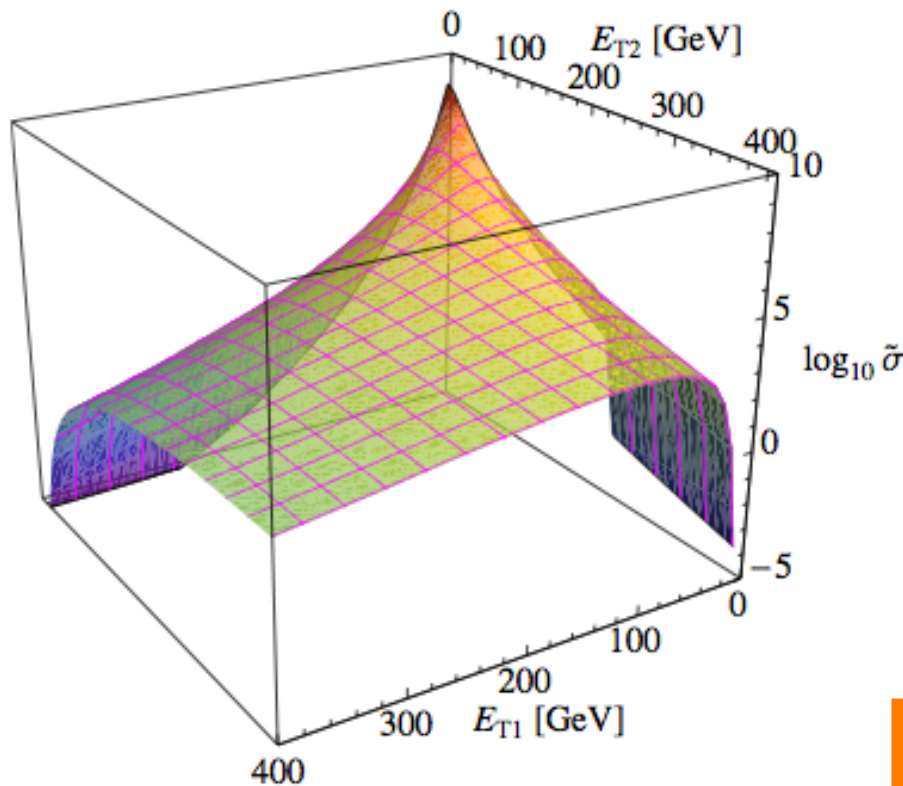


ATLAS, arXiv:1011.6182, PRL (2011);

CMS, arXiv: 1102.1957, PRC(2011)

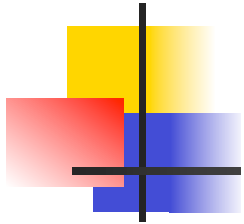
# Dijets in p+p at NLO

- Dijet yield gives a broad distribution at NLO.
- Dijet asymmetry is described very well by NLO pQCD.

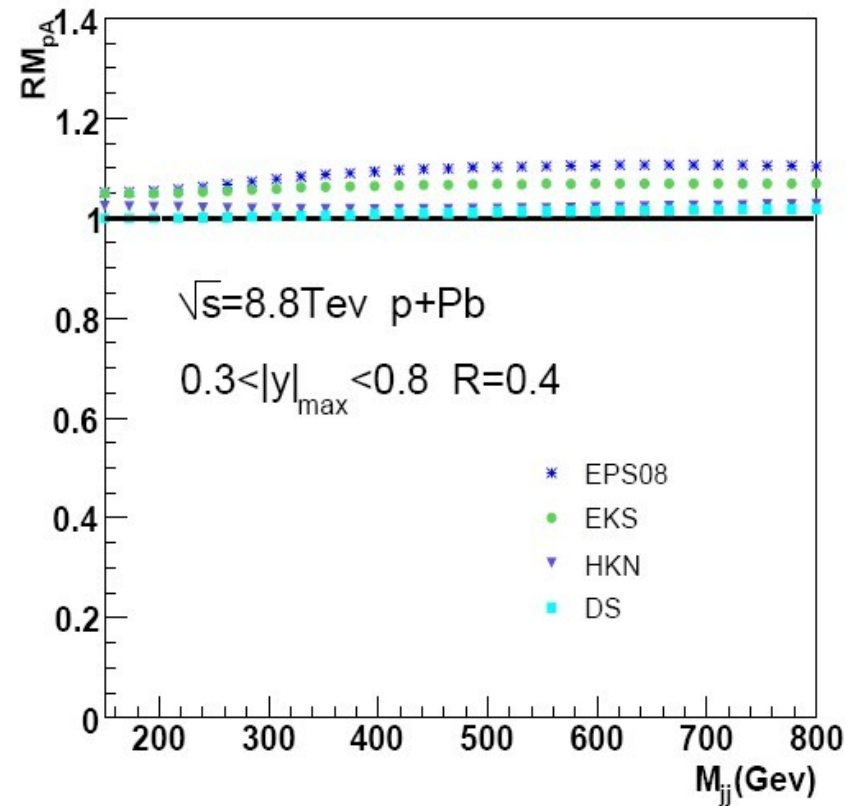
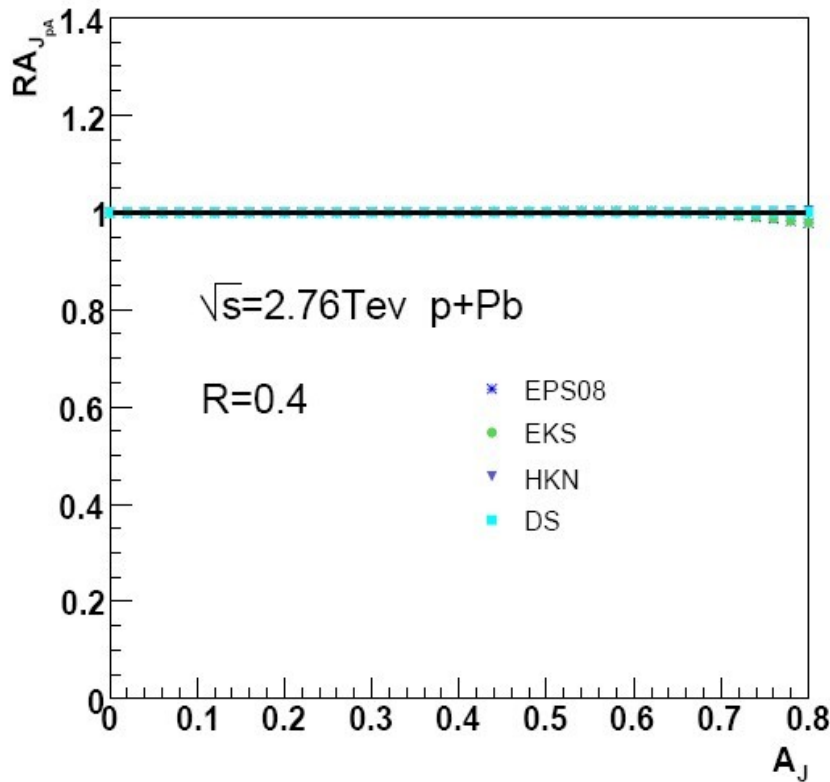


$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}$$

# Dijet in HIC: CNM

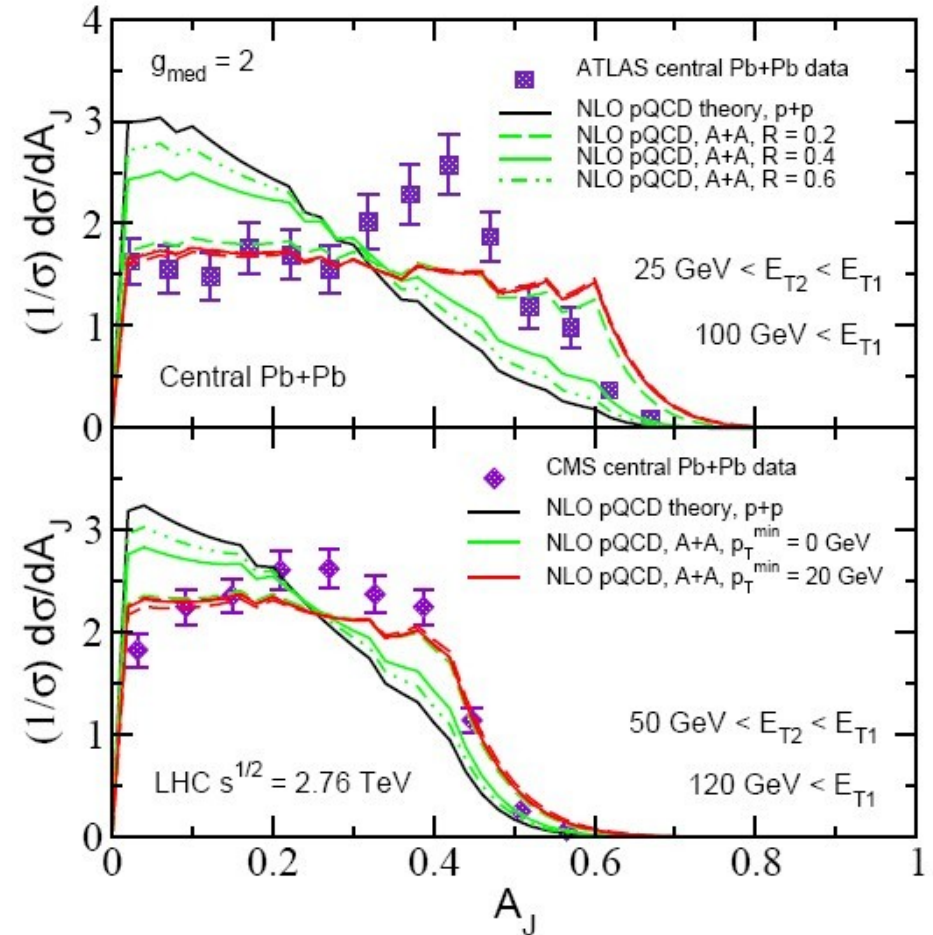
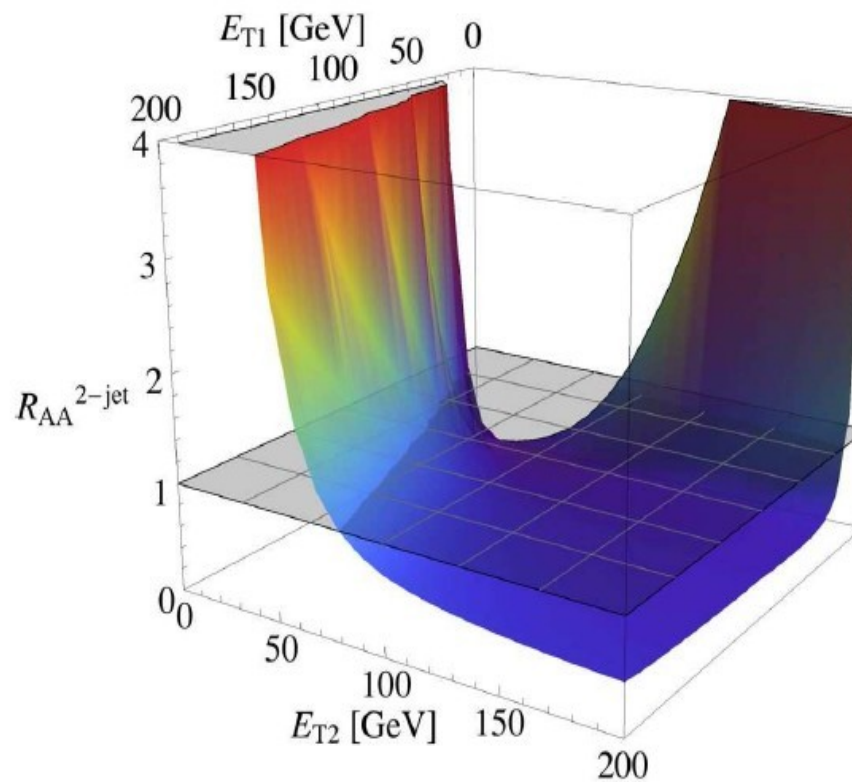


$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}} \quad M_{jj}^2 = 2p_T^2 [1 + \cosh(y_1 - y_2)]$$



Y He, BWZ, E Wang, EPJC (2012)

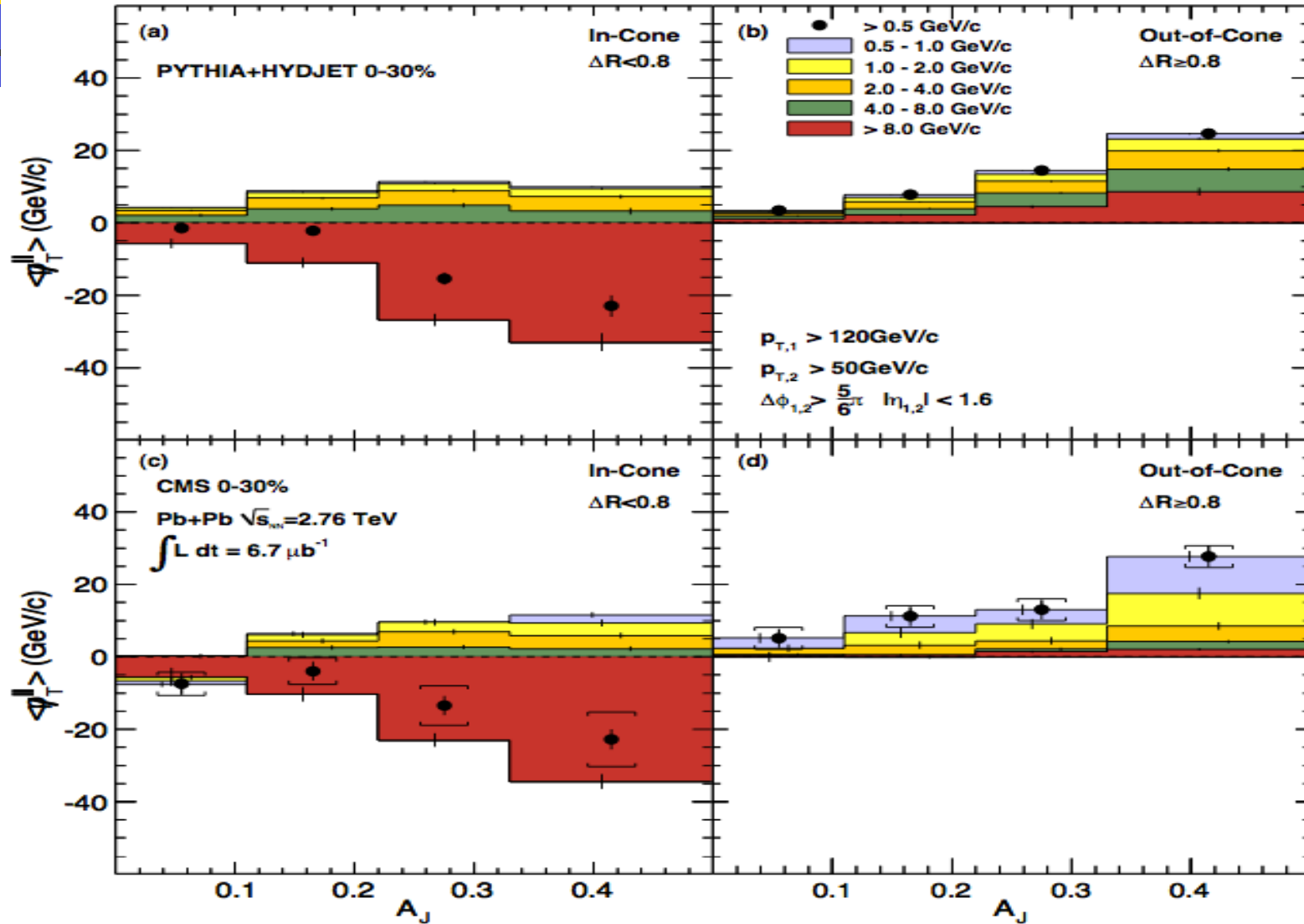
# Dijet in HIC at NLO



Y He, Vitev, BWZ, arXiv:1105.2566

# Dijet in HIC by CMS

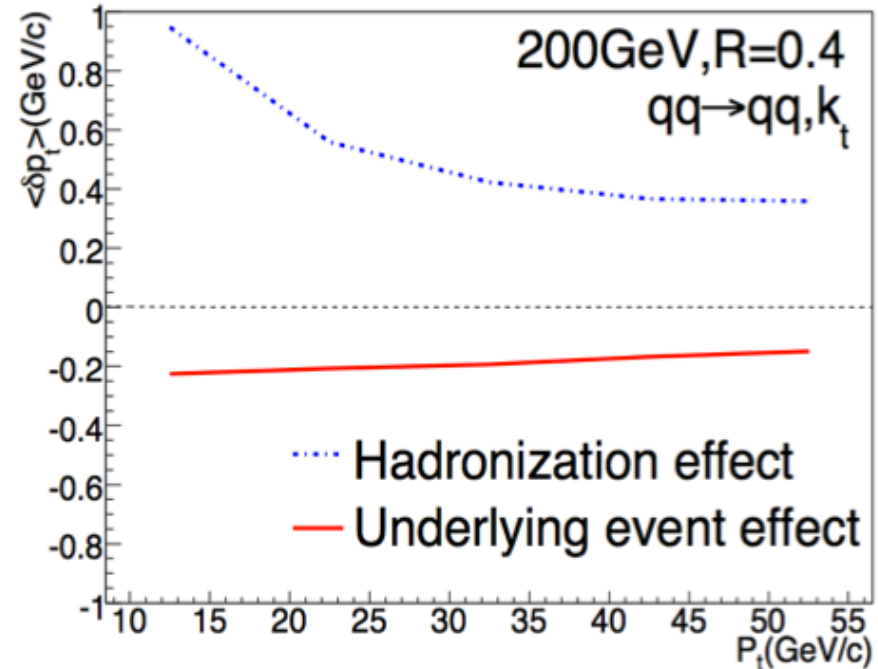
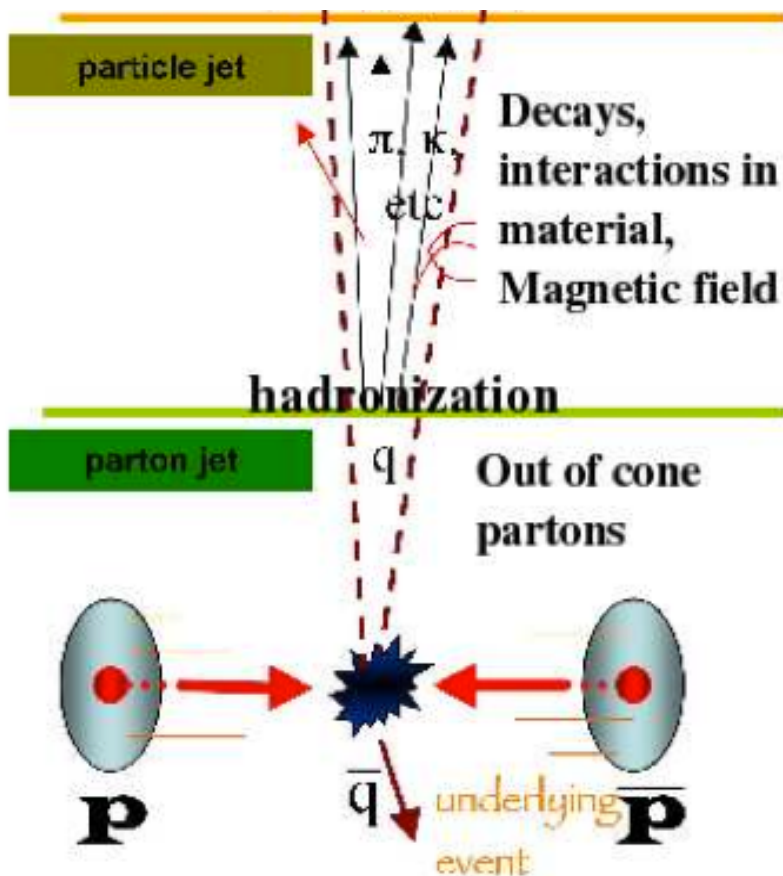
$$p_T^{\parallel} = \sum_i -p_T^i \cos(\phi_i - \phi_{\text{Leading Jet}})$$





# Non-perturbative effects

- Non-perturbative effects: hadronization & underlying event.
- Two effects will go in opposite direction: partial cancellation between "splash-out" effect and "splash-in" effect.

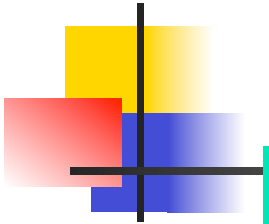


H Li, BWZ, E Wang (2012)

# Summary

- An entirely new frontier of HIC — jet observables: jet shapes, inclusive jets, tagged jets, dijets, ...





非常感谢!  
Thank you!

# Jet finding algorithms

- Cone algorithm
- Midpoint cone algorithm
- $k_T$  algorithm

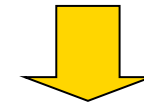
$$k_{T,i}^2 = p_{T,i}^2$$

$$k_{T,(i,j)}^2 = \min(p_{T,i}^2, p_{T,j}^2) \frac{R_{i,j}^2}{D^2}$$

if  $k_{T,(i,j)}^2 < k_{T,i}^2$ , merge

- Anti- $k_T$  algorithm
- Seedless algorithm

Parton merge parameter



**NLO**

$$R_{rc} = \min \left( R_{sep} R, \frac{E_{T_i} + E_{T_j}}{\max(E_{T_i}, E_{T_j})} R \right)$$

- Midpoint cone  $R_{sep} = 2$
- Cone  $1 < R_{sep} < 2$
- $K_T$   $D = R, R_{sep} = 1$