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# Emergent Spacetime

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*Quantum Gravity*  
*Spacetime in String...*  
*Emergent Spacetime*

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# Emergent Spacetime

- 1. Quantum Gravity
- 2. Spacetime in String theory
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Quantum Gravity  
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# 1 Quantum Gravity

- Four kinds force in Nature:
  - Gravity; Newton, Einstein
  - Electromagnetic force; Maxwell
  - Strong interaction force;
  - Weak force;

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- **Two revolutionary discoveries in 20th century:**

- General relativity [Einstein 1915](#): A theory of gravitation.

Spacetime is dynamical: the interaction between spacetime and matter is nonlinear;

Black Hole, Cosmology, GPS, ...;

- Quantum principle: uncertainty principle, wave-function, ....

High energy physics: QED, QCD, SM, GUT, SUSY ....

Condensed matter physics, ....

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- **Unification:** Einstein's dream

- Gravity with EM: Kaluza-Klein;
- Electro-Weak plus Strong interaction: unified in Standard model;
  - ★ In the framework of Quantum Field Theory;(SR+QM)
  - ★ Gauge principle play the central role;
  - ★ Gauge group:  $SU(3) \times SU(2) \times U(1)$ ;
  - ★ Gauge bosons as the mediators of forces:  
Gluon,  $W^\pm$ , Z, Photon;
  - ★ The best theory we have; (Higgs in LHC?)
  - ★ The background geometry is Minkowski spacetime;

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- **Three questions:**

- How to quantize gravity?
- How to unify gravity with other forces?
- Why quantum gravity?

- **Answers:**

- Graviton is massless spin-2 particle; (Gravitational wave? LIGO, LISA, ....)
- Gravity is non-renormalizable; ( $\mathcal{N} = 8$  supergravity finite?)
- Gravity is special: nonlinear, background and dynamical; (Background independence essential?)
- Canonical quantum gravity, loop quantum gravity, spin foam, ...;
- String theory: unify the gravity with others in a natural way. The most promising candidate of quantum gravity;
- Quantum black hole, cosmological singularity and various questions in particle physics and cosmology; (A better understanding of QM?)

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## 2 Spacetime in String theory

- Spacetime near Planck scale  $l_p$

- ★  $l_p \sim 10^{-33} \text{cm}$ ;

- ★ Important question: physics near the cosmological singularity.  
Singularity resolved? Initial condition for inflation? DE?...

- ★ Quantum effect of gravity important;

- ★ Usual concept of spacetime by metric make sense?

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- **Quantum foam?** John Wheeler 1960's

- ★ Spacetime subject to the kinds of uncertainty required by QM;
- ★ Spacetime has foaminess: geometry has complex shapes and textures.
- ★ Quantum BH appear at  $l_p$  and then evaporate in  $10^{-43}$  seconds;
- ★ Wormhole would form and dissolve;
- ★ Baby universe?

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## • Noncommutative Geometry(NCG)

- Operator algebra in QM;
- Quantum spacetime as operator algebra;
- Noncommutative geometry; [A. Connes 1994](#)
- In string theory, NCG has natural realization:
  - \* Open String Field Theory; [E. Witten 1986](#)
  - \* D-brane with  $B_2$  field; [Seiberg & Witten 1999, ...](#)

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## • String theory:

- The elementary particles are not really point-like. They are "TINY" strings;
- There are two kinds of strings: open and closed;
- Unify the gravity with the other forces in a natural way;
- The string has constant tension  $T = \frac{1}{2\pi\alpha'}$ ;
- There exists an intrinsic length scale:

$$l_s^2 = \alpha' \quad (1)$$

- $\alpha'$  as Planck constant in the string worldsheet action;
- String coupling constant  $g_s$  govern the string interaction;

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- **T-duality**: The closed string on a circle with radius  $R$  is equivalent to the one on a circle with radius  $\alpha'/R$ ;
  - ★ Momentum  $\leftrightarrow$  Winding;
  - ★ Winding conservation is a stringy symmetry;
  - ★ Background geometry is ambiguous: what is the background metric?
  - ★ Due to the extensive nature of the string;
  - ★ String probe cannot detect the features in the geometry which are smaller than  $l_s$ ;
  - ★ Generalized to "Mirror symmetry" in Calabi-Yau manifolds;

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## • S-duality

- ★ Quantum nature: D-brane ...;
- ★ D-brane probe: Nonperturbative. Matrix model;
- ★ Strong/Weak duality: highly quantum/semiclassical backgrounds;
- ★ Breakdown of small distance/high energy connection: as we try to increase the energy of a probe, it becomes bigger;

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## • Locality in String theory:

- ★ QFT: local, keep causality, S-matrix analytic;
- ★ String theory: causal, S-matrix is analytic, but might not be local;
- ★ Dualities suggest non-locality;

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## • Spacetime in String theory:

- ★ Ambiguity in geometry;(Stringy geometry in mathematics)
- ★ Ambiguity in topology: topology transition;
- ★ Fuzziness: locality lost;
- ★ Matrix cosmology? Matrix degrees of freedom to describe the physics near the cosmological singularity;

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### 3 Emergent Spacetime

- Space and time are not fundamental, they are emergent concepts;
- The concept of locality cannot be fundamental;
- General covariance is a derived and useful concept at long distances;
- A fundamental theory should not have an underlying spacetime;

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## • Examples of emergent Space:

1. Myers effect: fuzzy space;[R. Myers 1999](#)
2. Matrix QM: 2D noncritical string theory;[M. Douglas 1991, ...](#)
3. Emergent space in BFSS matrix model;[BFSS 1997](#)
4. AdS/CFT correspondence.

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## • AdS/CFT correspondence:

- String theory in Anti-de-Sitter spacetime and a CFT at its boundary;
- A definition of string theory;
- The best studied one: IIB superstring in  $AdS_5 \times S^5$  is dual to the  $\mathcal{N} = 4$  Super-Yang-Mills in the large N limit; ( $AdS_5/CFT_4$  correspondence) [Maldacena 1997](#)
- Gravity/Gauge correspondence;
- String states/operators;(Beyond gravity/gauge correspondence)
- Strong/Weak duality;

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- The ideas behind  $AdS_5/CFT_4$ :

- Large  $N_c$  gauge theory is a string theory; 't Hooft 1974, A. Polyakov, ...
- Holographic principle; 't Hooft 1992, L. Susskind 1993
- Open/Closed string duality;

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## • Physical implications

– String theory side:

- \* Black hole physics: entropy, quasi-normal mode, unitary evolution;
- \* Background independence and emergent space: [LLM 2004](#) Half-BPS states in SYM correspond to various supergravity configurations, which are asym. to  $AdS_5 \times S^5$ ;

– Gauge theory side:

- \* AdS/QCD: strong coupling, meson spectrum, ...;
- \* RHIC (Relativistic Heavy Ions Collider) physics: QGP,...;

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## • Emergent time:

- If space emerges, why not time?
- No example;
- Locality in time? Violation of causality?
- What does it mean to have a theory without fundamental time? "Dynamics"?
- Wavefunction? Unitarity? ....
- Implications: the physics of space-like and null singularities (BH singularity and the cosmological singularity), the wave-function of the Universe, initial conditions for the Universe,...;

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