



中国科学技术大学

交叉学科理论研究中心

Interdisciplinary Center for Theoretical Study

[English Version]

Secondary but more fascinating phenomenology in the next-generation large-scale neutrino experiments

Ye-Ling Zhou (HIAS) 2023-12-7



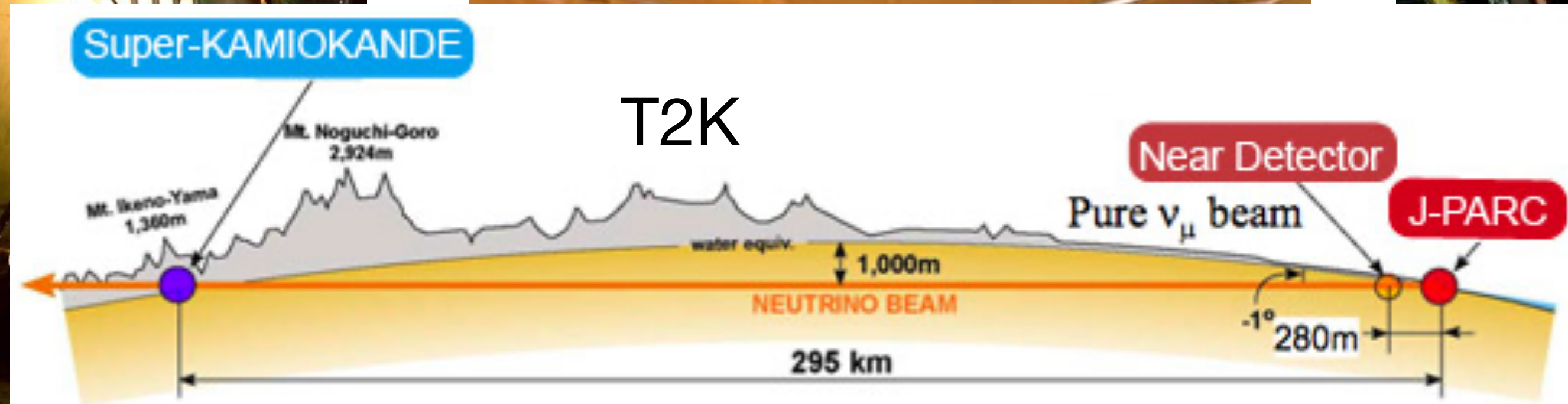
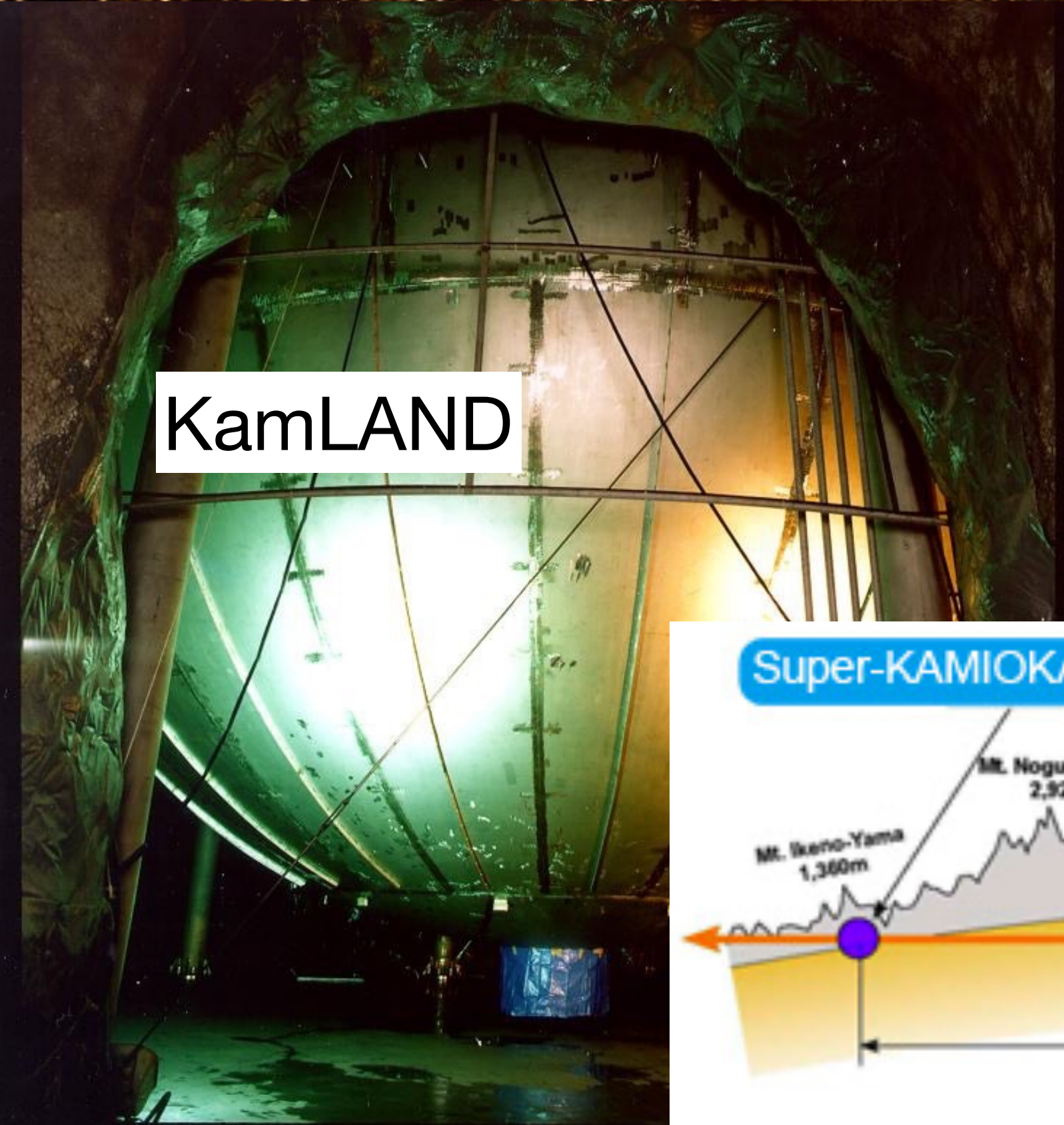
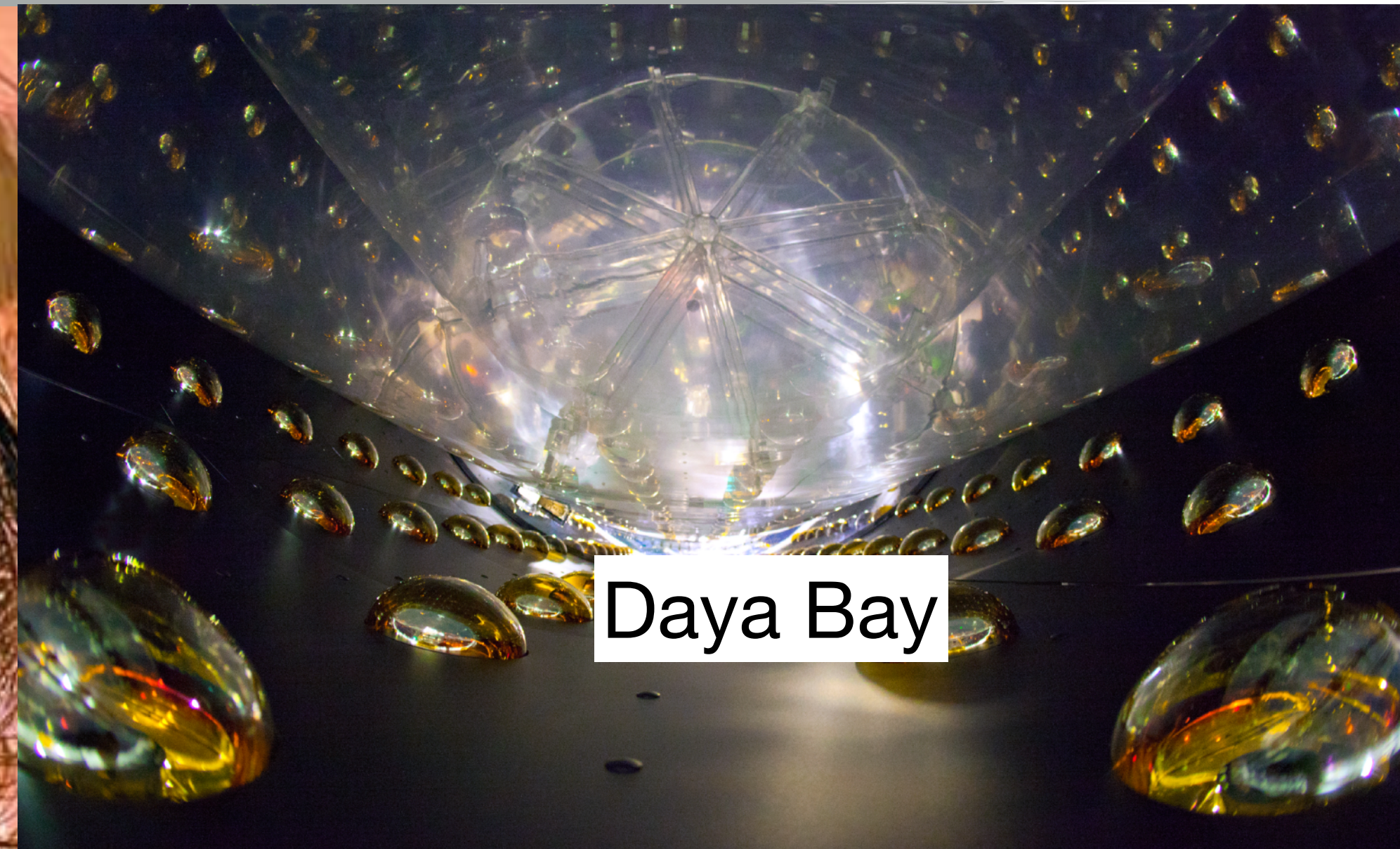
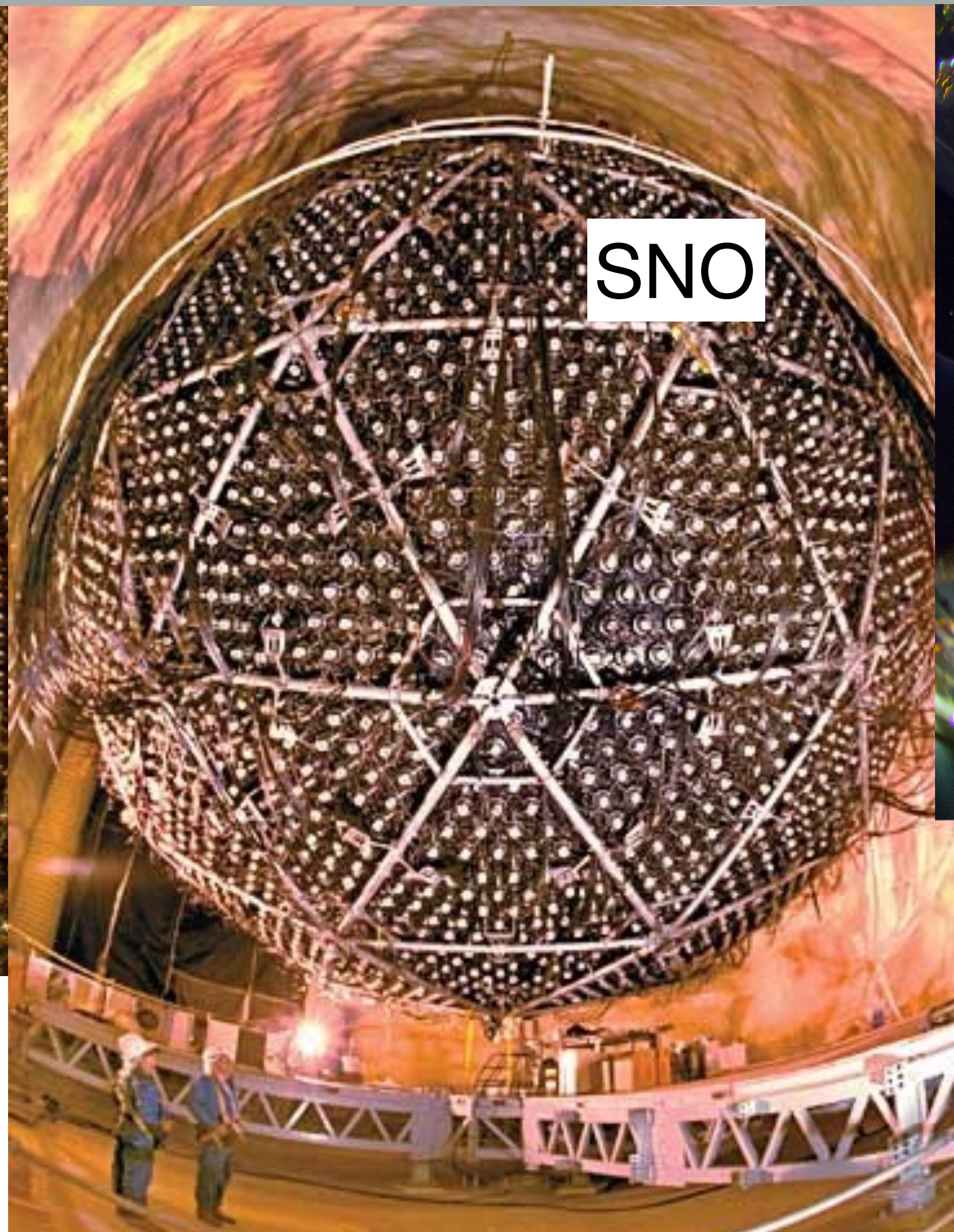
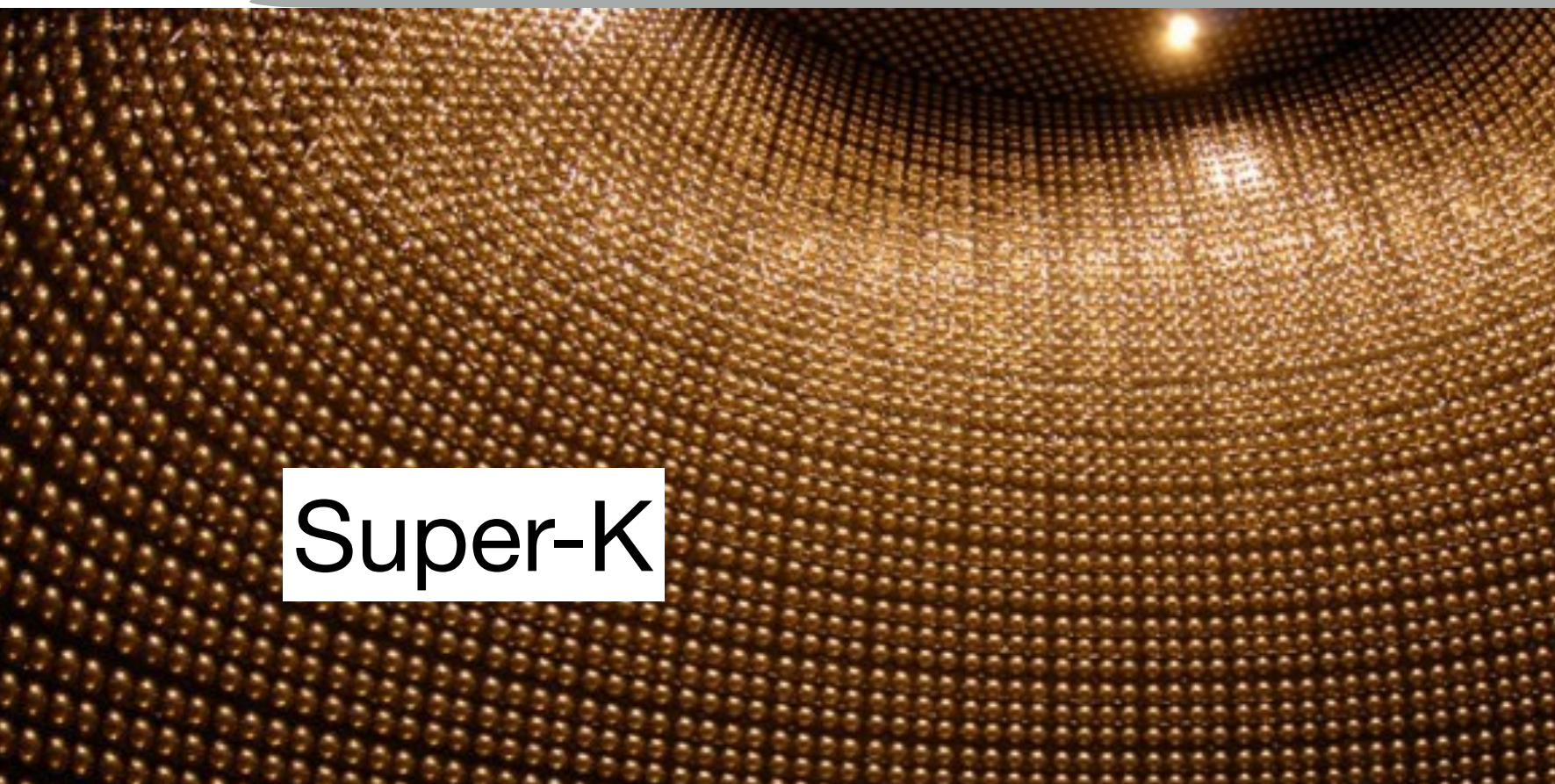
國科大杭州高等研究院

Hangzhou Institute for Advanced Study, UCAS

基础物理与数学科学学院

School of Fundamental Physics and Mathematical Sciences

Some important neutrino experiments in the past



Some important neutrino experiments in the past

Super-K

SNO

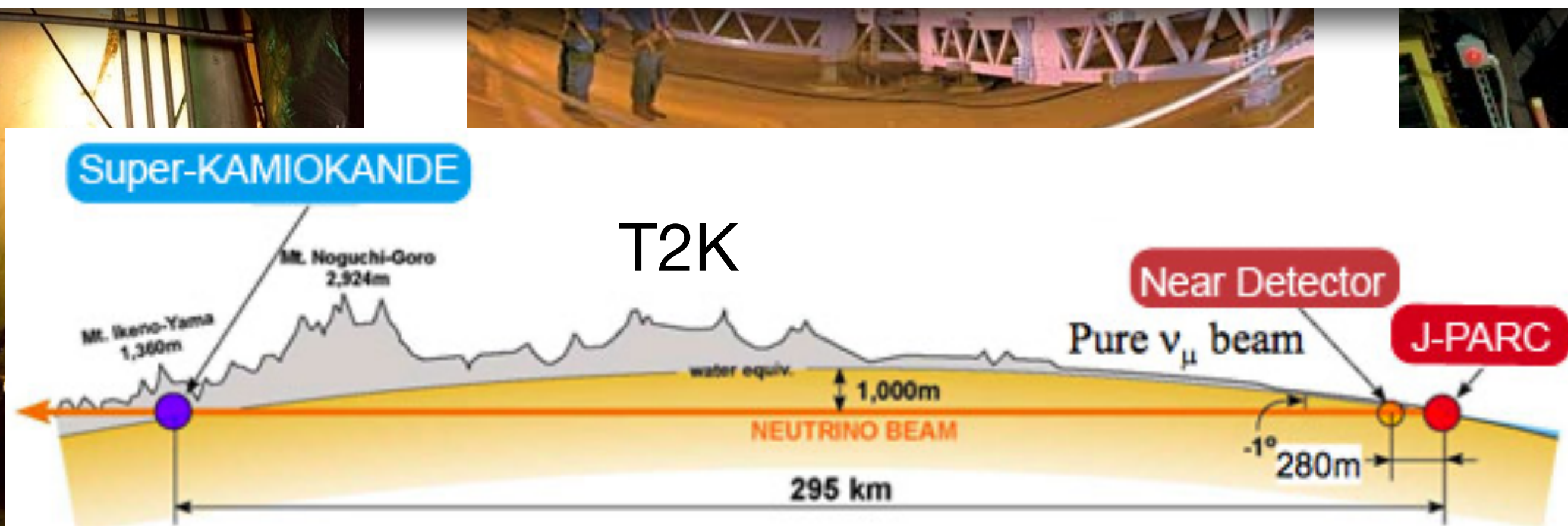
Daya Bay

KamLAND

MINOS

Table 2: Some key milestones associated with the experimental discoveries of neutrino or antineutrino oscillations.

	Neutrino sources and (or) oscillations	Main discoverers	Nobel Prize
1968	solar neutrinos ($\nu_e \rightarrow \nu_e$) [59]	R. Davis	2002
1987	supernova antineutrinos ($\bar{\nu}_e$) [62, 63]	M. Koshiba	2002
1998	atmospheric neutrinos ($\nu_\mu \rightarrow \nu_\mu$) [64]	Xing, Phys.Rept, 2019	
2001	solar neutrinos ($\nu_e \rightarrow \nu_e, \nu_\mu, \nu_\tau$) [65, 66, 67]		
2002	accelerator neutrinos ($\nu_\mu \rightarrow \nu_\mu$) [68]	K. Nishikawa	
2002	reactor antineutrinos ($\bar{\nu}_e \rightarrow \bar{\nu}_e$) [69]	A. Suzuki	
2011	accelerator neutrinos ($\nu_\mu \rightarrow \nu_e$) [70, 71]	K. Nishikawa	
2012	reactor antineutrinos ($\bar{\nu}_e \rightarrow \bar{\nu}_e$) [72]	K. B. Luk, Y. Wang	



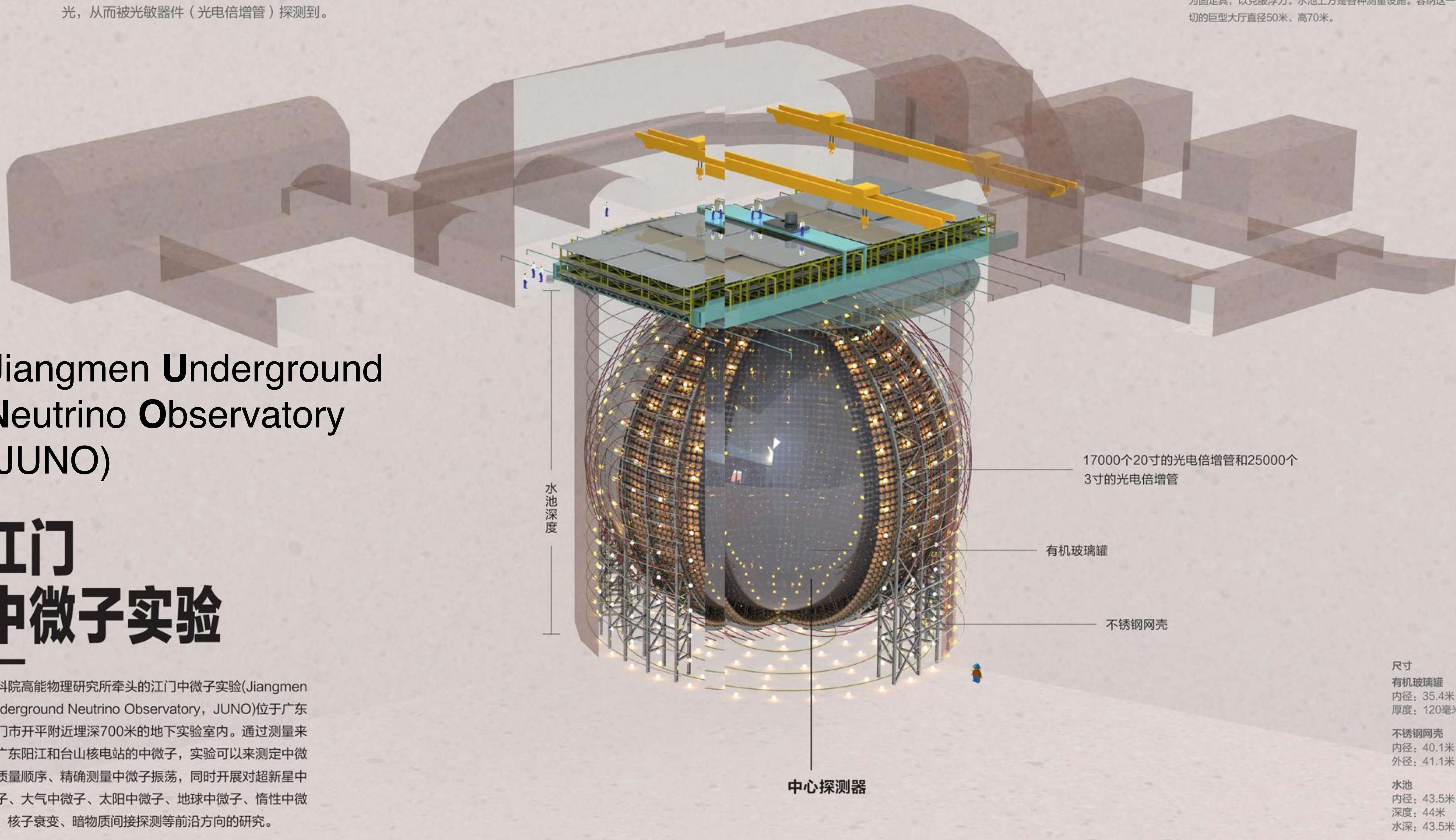
光，从而被光敏器件（光电倍增管）探测到。

为固定其，以免上浮。水池上方是各种测量设施。容纳这一切的巨大大厅直径50米、高70米。

Jiangmen Underground Neutrino Observatory (JUNO)

江门中微子实验

中科院高能物理研究所牵头的江门中微子实验(Jiangmen Underground Neutrino Observatory, JUNO)位于广东江门市开平附近埋深700米的地下实验室内。通过测量来自广东阳江和台山核电站的中微子，实验可以来测定中微子质量顺序、精确测量中微子振荡，同时开展对超新星中微子、大气中微子、太阳中微子、地球中微子、惰性中微子、核子衰变、暗物质间接探测等前沿方向的研究。



17000个20寸的光电倍增管和25000个3寸的光电倍增管

有机玻璃罐

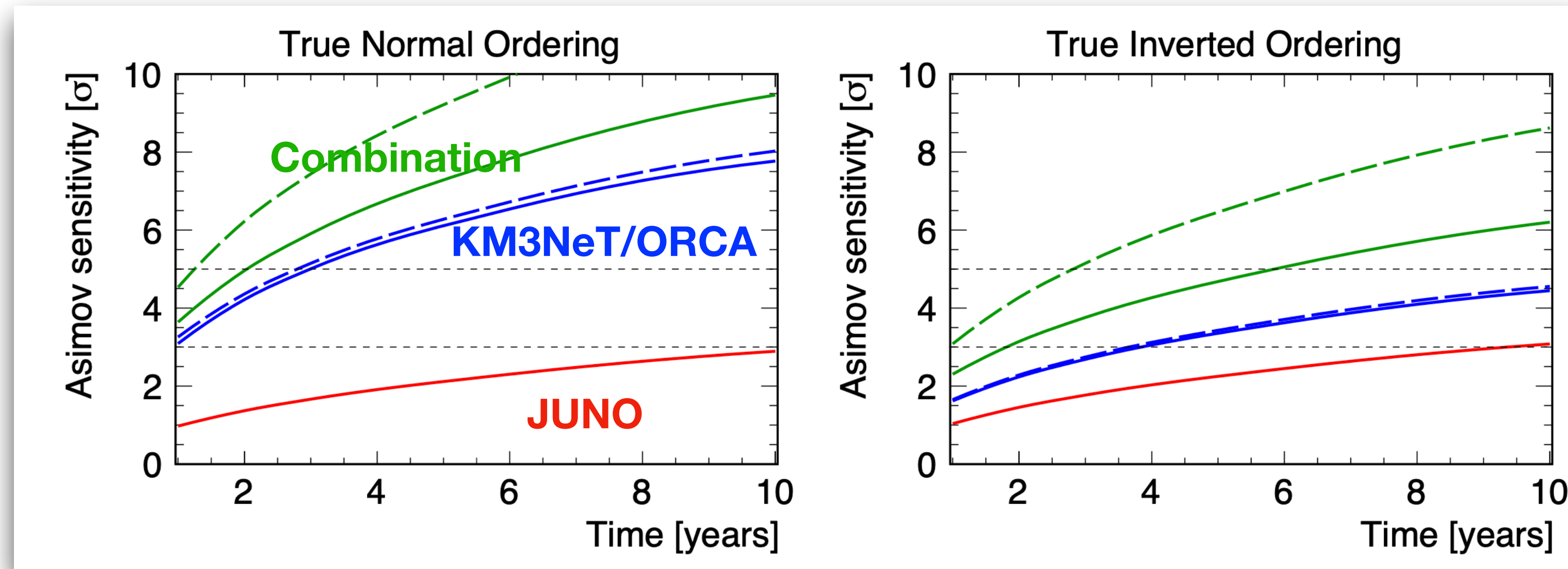
不锈钢网壳

中心探测器

水池深度

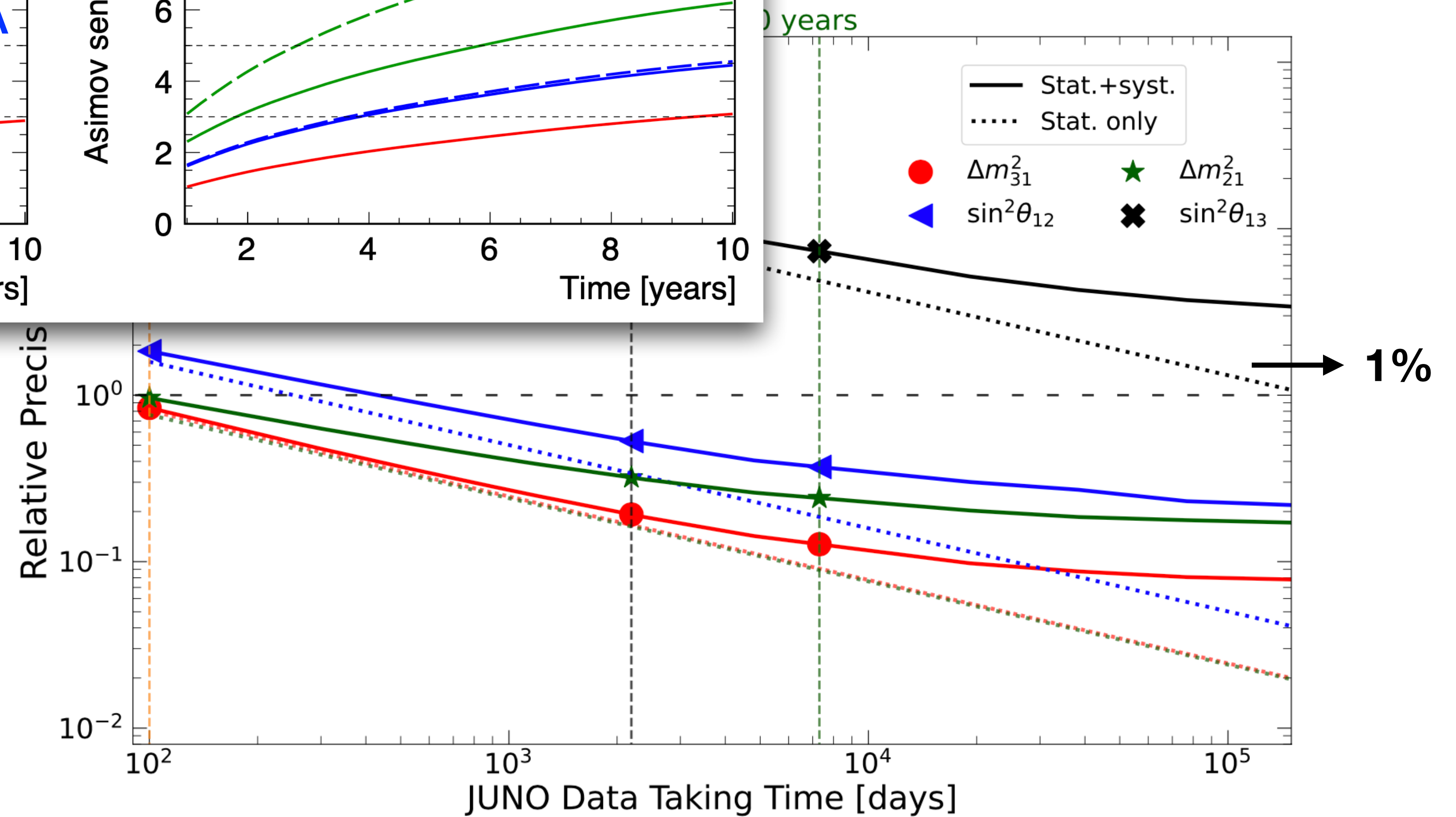
尺寸
有机玻璃罐
内径：35.4米
厚度：120毫米
不锈钢网壳
内径：40.1米
外径：41.1米
水池
内径：43.5米
深度：44米
水深：43.5米

JUNO



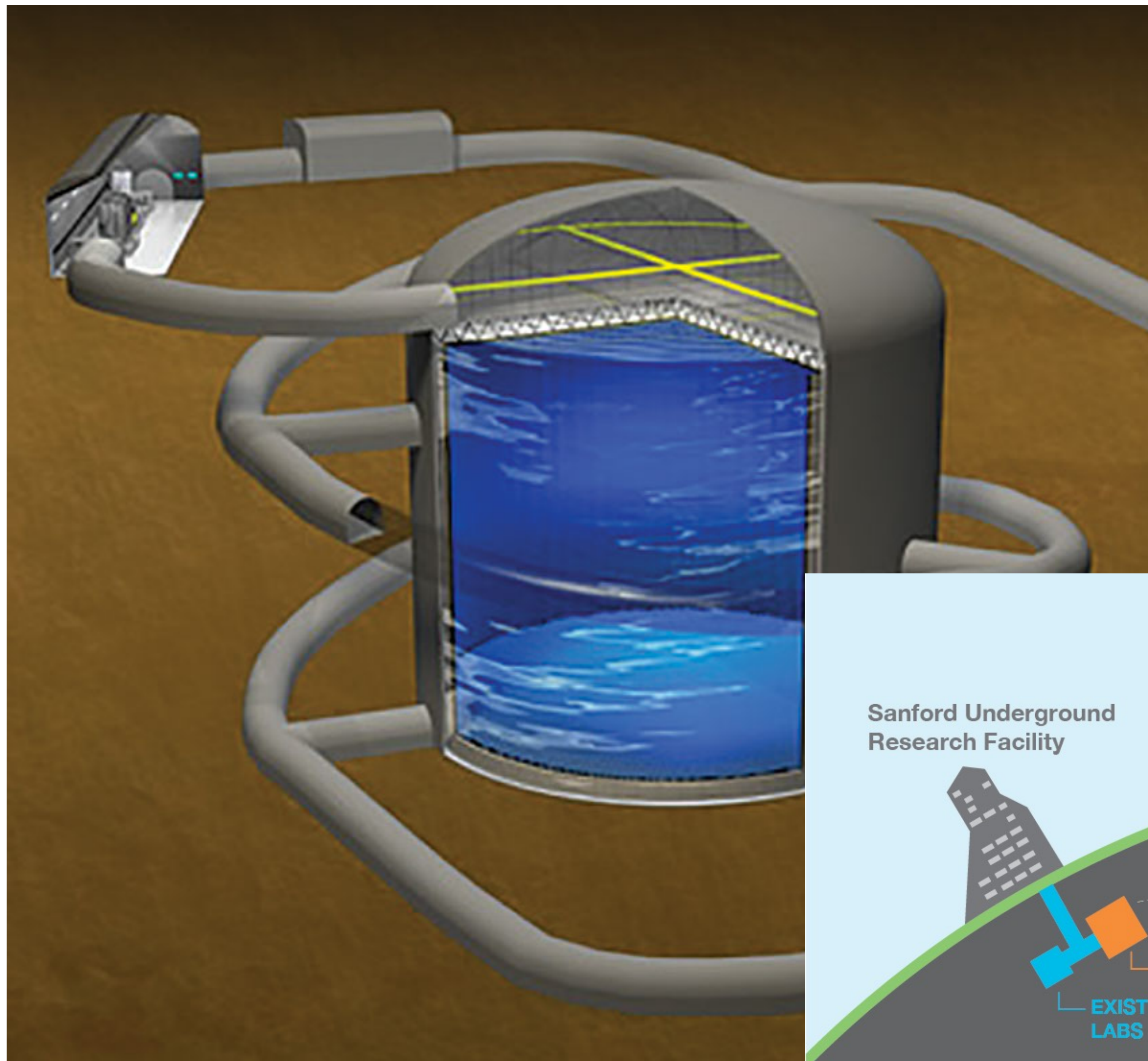
Mass Hierarchy determination,
state-of-art sensitivity performance

2108.06293



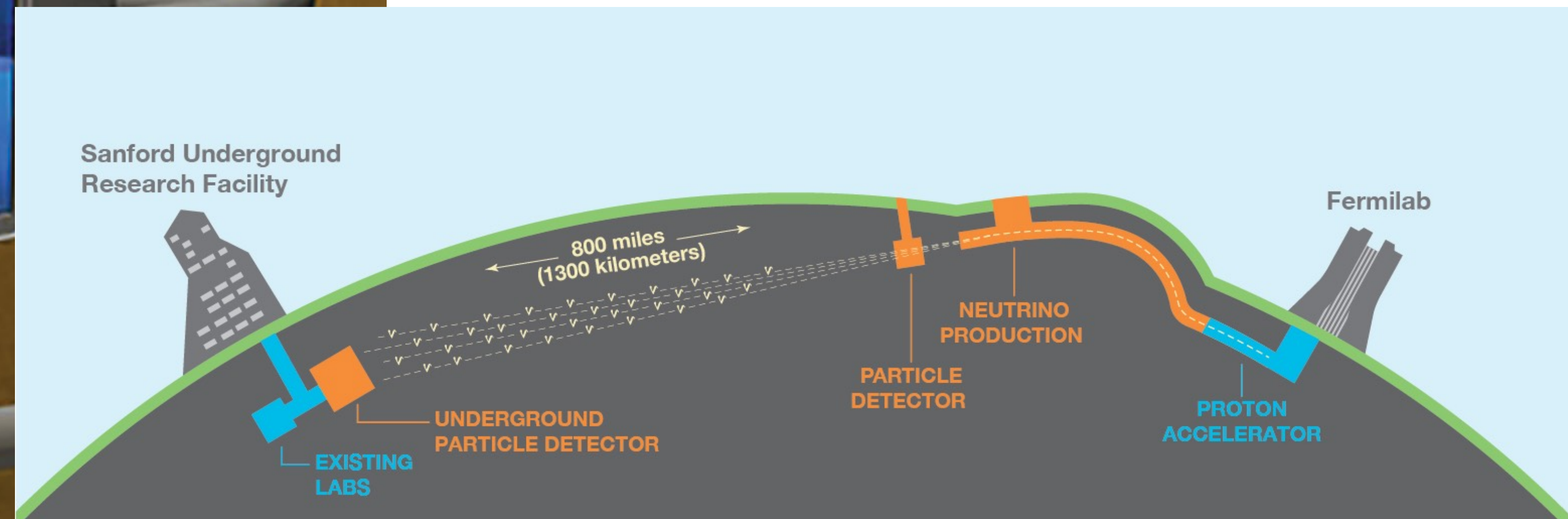
JUNO collaboration 2204.13249

Hyper-K & DUNE



Hyper-K, 188kton FV, expected to run in 2027

DUNE, run in 2030?



Hyper-K & DUNE

Hyper-K
1805.04163

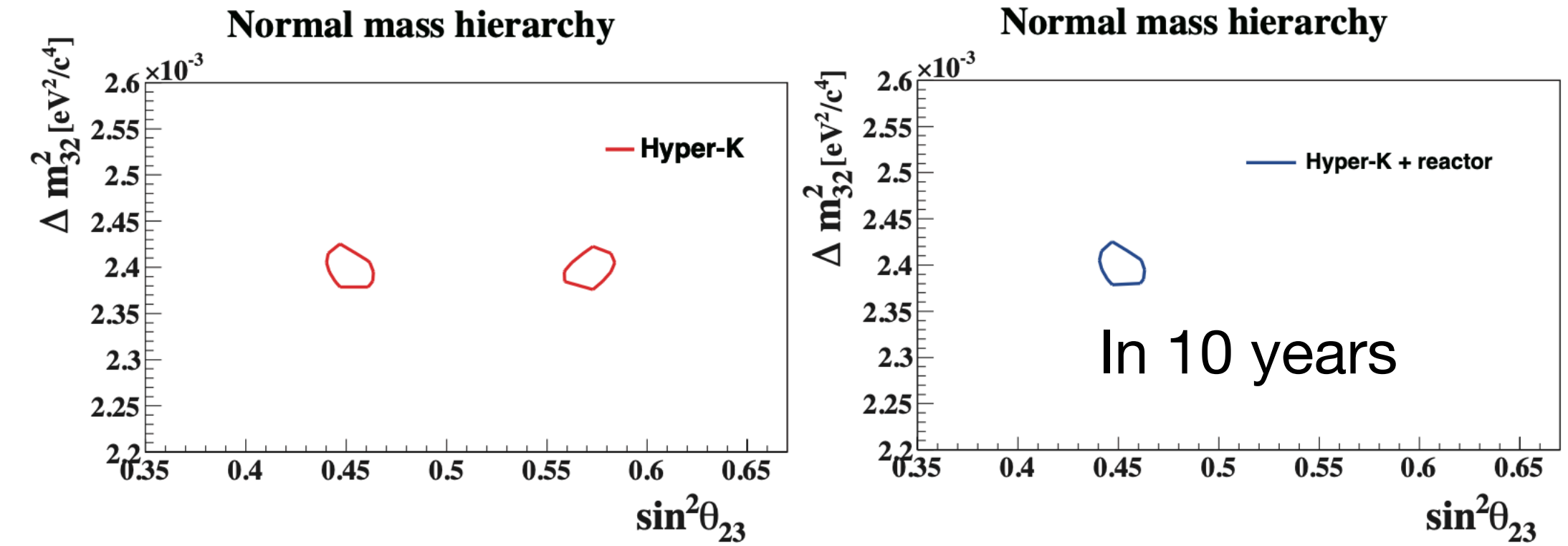
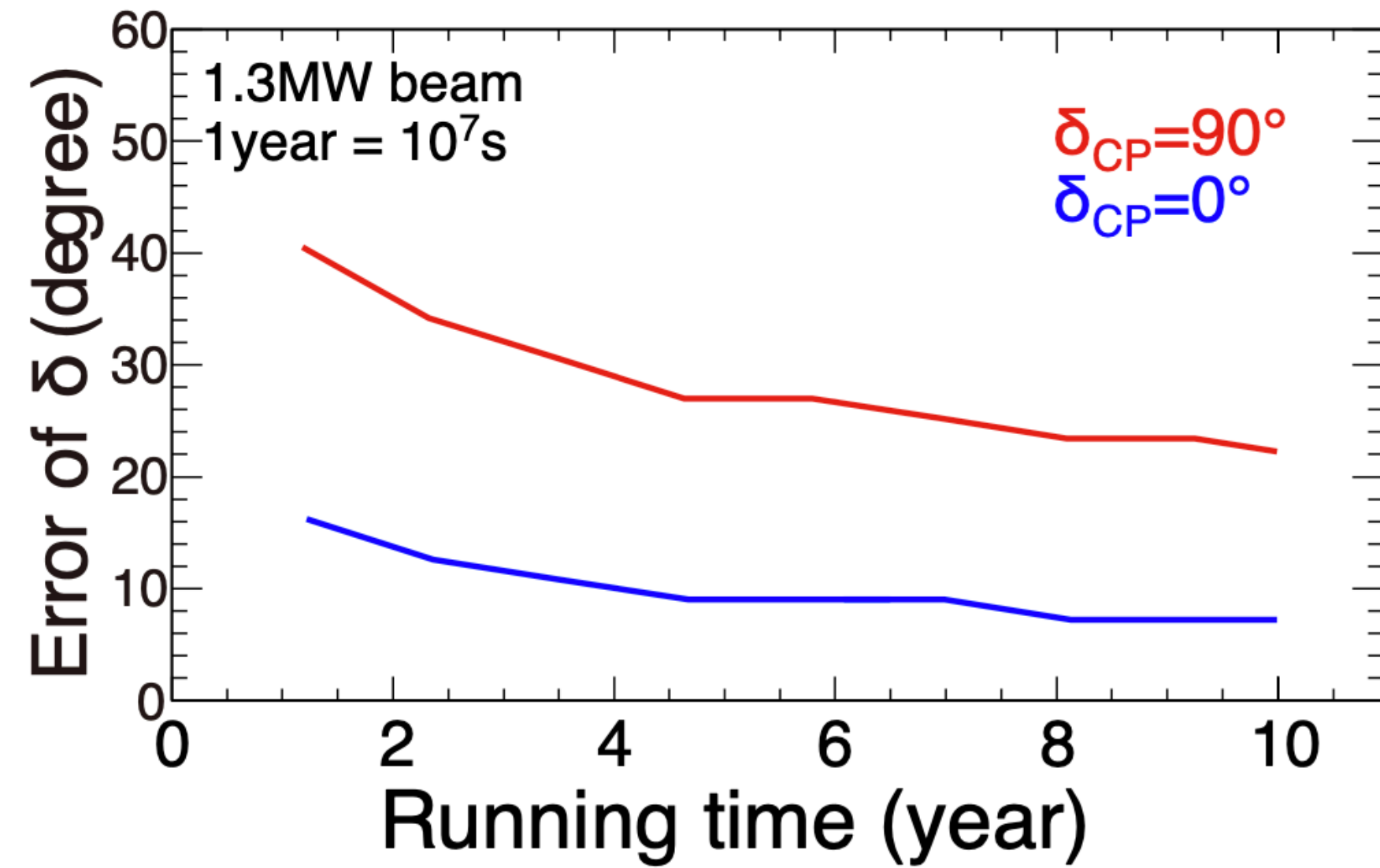
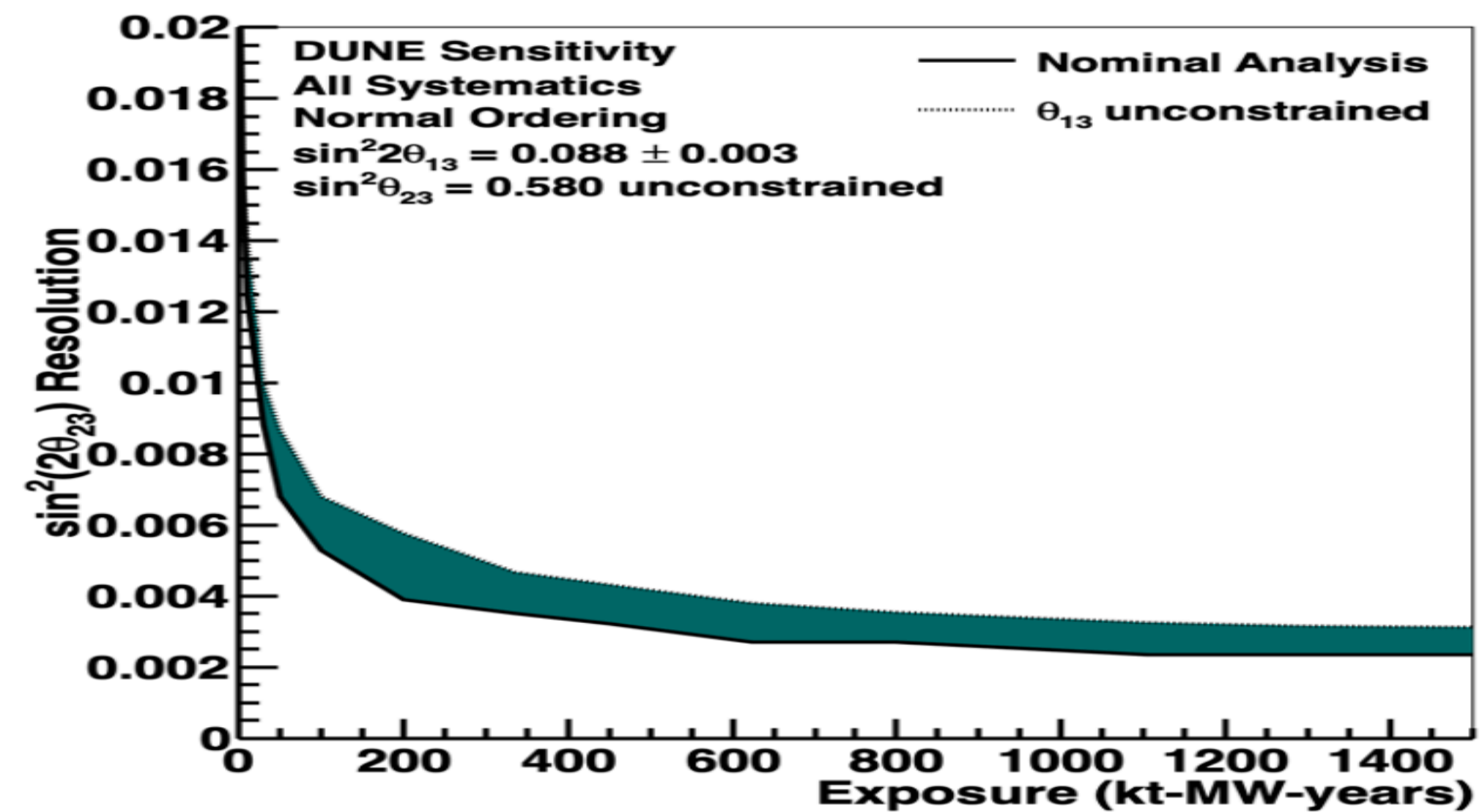
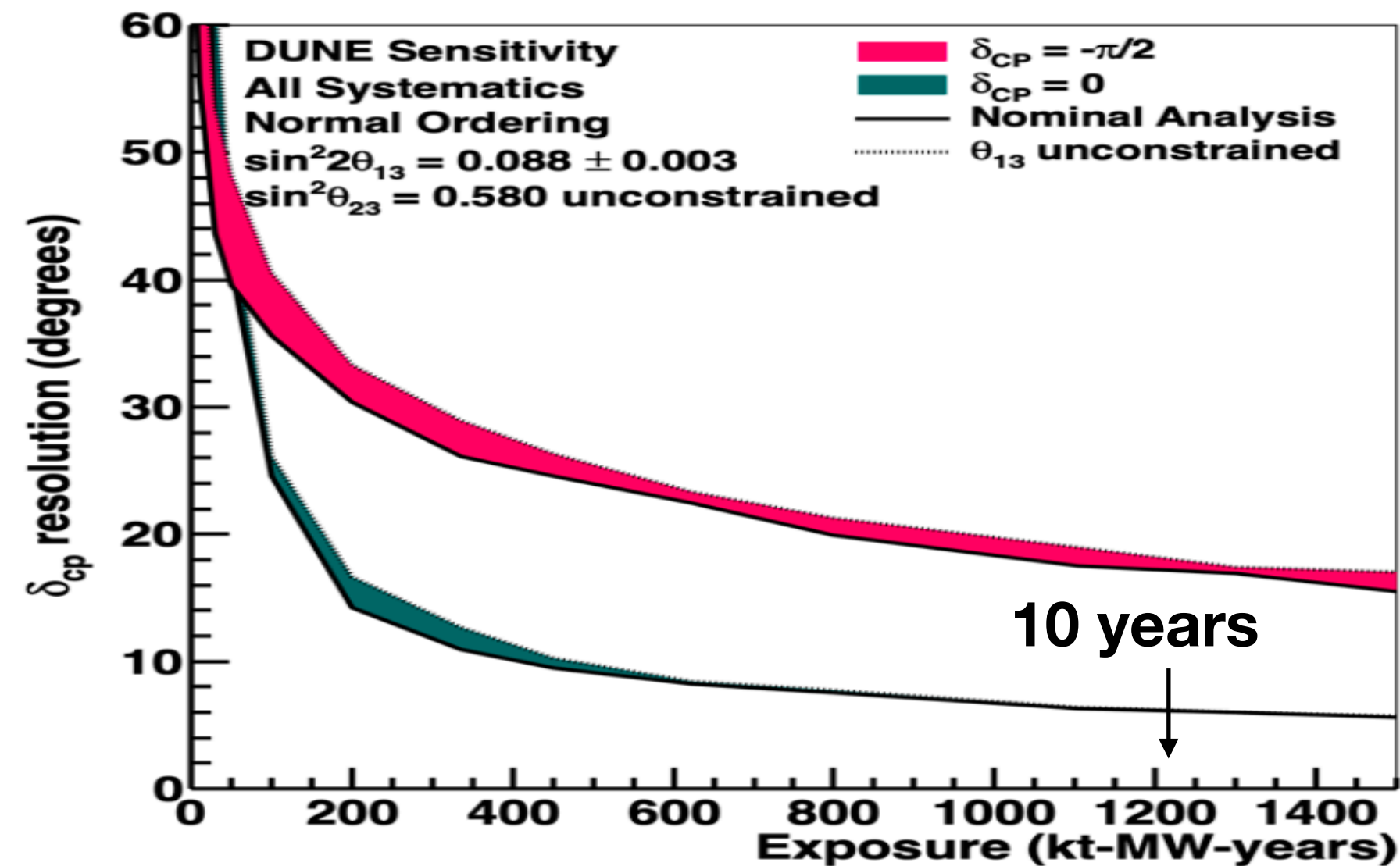


FIG. 144. 90% CL allowed regions in the $\sin^2 \theta_{23}$ - Δm_{32}^2 plane. The true values are $\sin^2 \theta_{23} = 0.45$ and $\Delta m_{32}^2 = 2.4 \times 10^{-3} \text{ eV}^2$. Effect of systematic uncertainties is included. Left: Hyper-K only. Right: With a reactor constraint.

DUNE
2002.03005

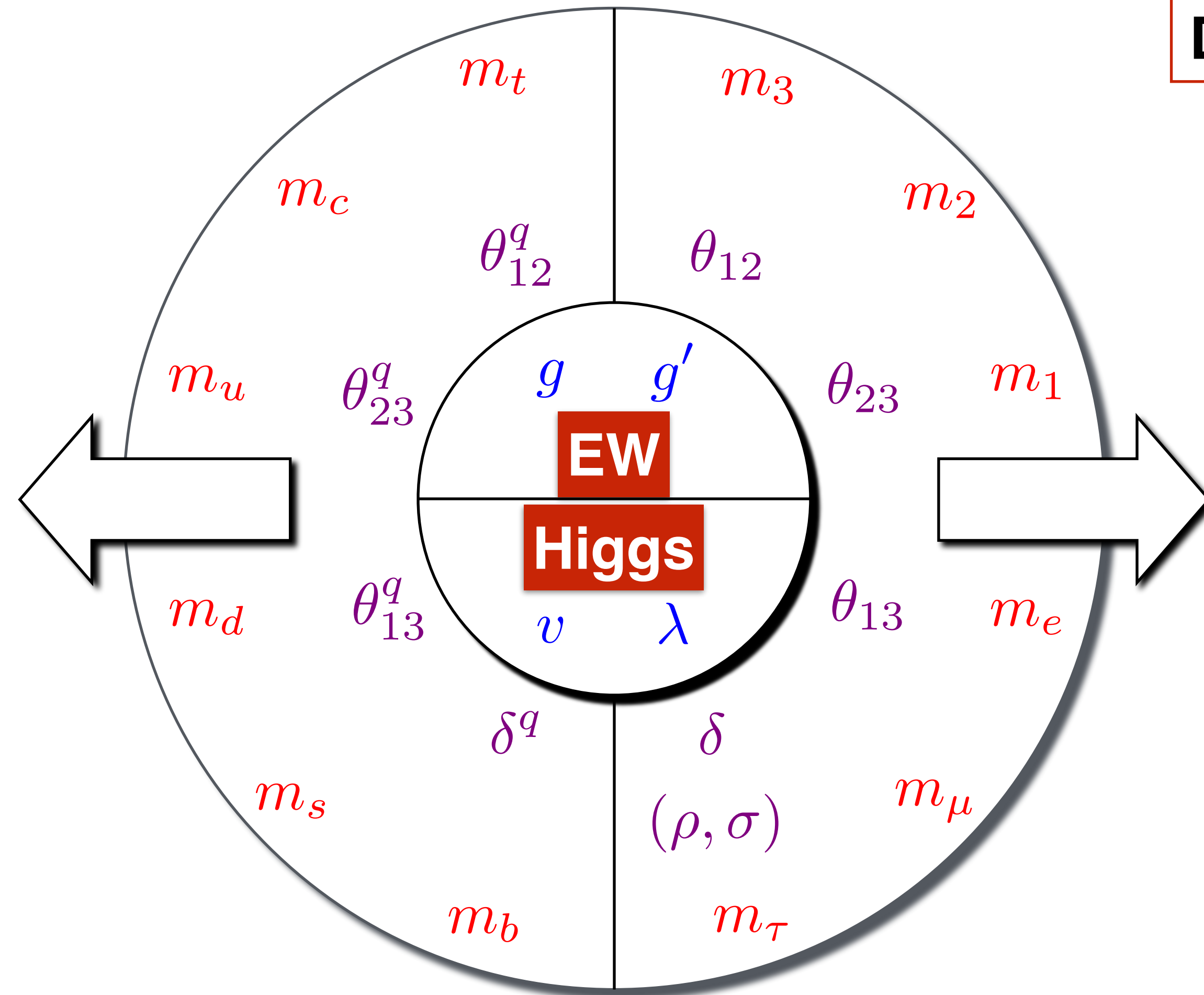


**Neutrino
Dirac or Majorana?**

$$\Delta m_{21}^2 = m_2^2 - m_1^2$$

$$\Delta m_{31}^2 = m_3^2 - m_1^2$$

**Quark masses
and mixing**



**Lepton masses
and mixing**

QCD

g_s

$\bar{\theta}$

Strong CP

**We are entering an era of precision
measurement of neutrino physics!**

We are entering an era of precision measurement of neutrino physics!

It will give us a deeper understanding of neutrino masses and mixing!

Origin of neutrino masses, lepton mixing and CP violation

We are entering an era of precision measurement of neutrino physics!

It will give us a deeper understanding of neutrino masses and mixing!



No, I do not want to talk about them

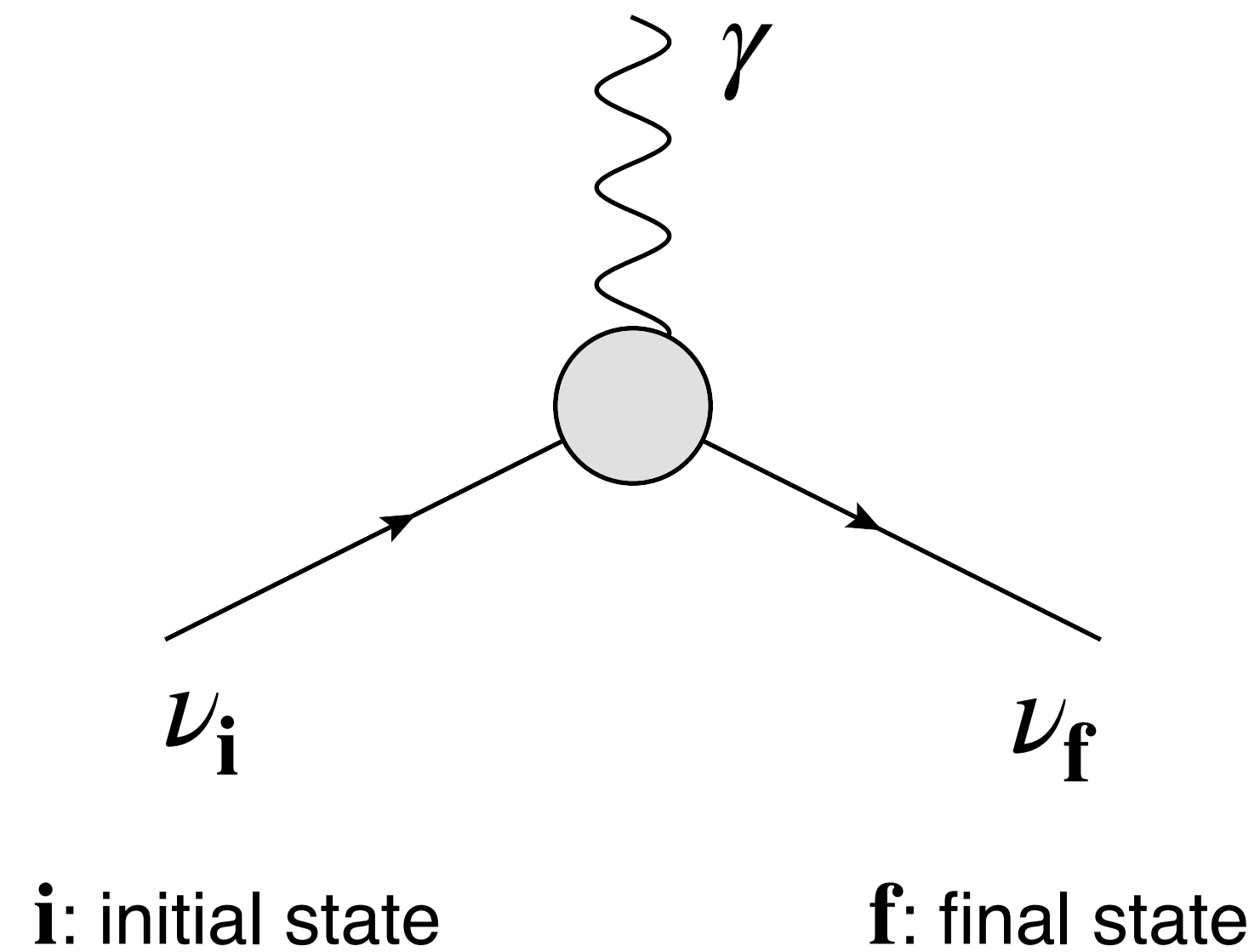
of neutrino masses, lepton mixing and CP violation

Not primary, but more fascinating phenos

Neutrino electromagnetic property and
CP-violating radiative decay

Proton decay and its probe to grand
unified theories (GUT)

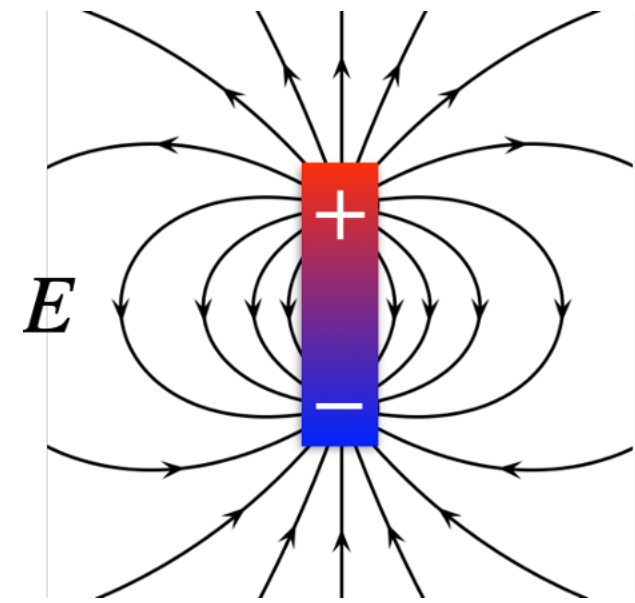
Neutrino electromagnetic property and CP-violating radiative decay



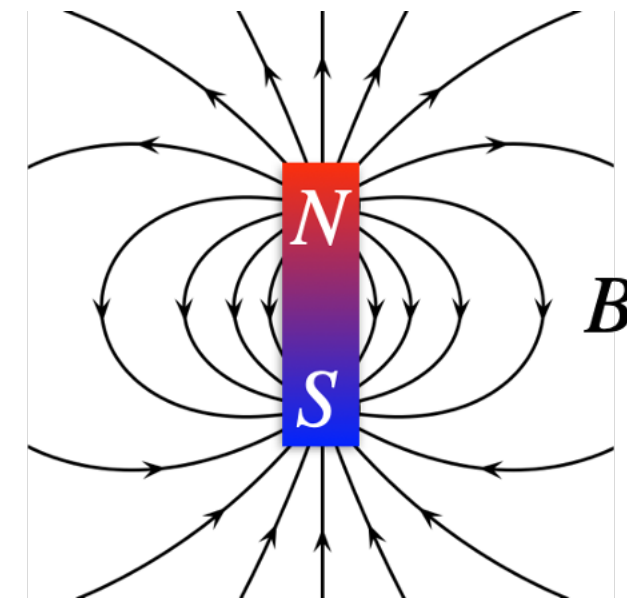
Neutrino electromagnetic dipole moment

- Neutral fermions may have electromagnetic dipole moment (EMDM)

electric
dipole
moment
 d



magnetic
dipole
moment
 μ



- EMDM form factor

$$\mathcal{H}_{\text{EMDM}} = j_\mu A^\mu \quad \langle \nu_{\mathbf{f}} | j_\mu | \nu_{\mathbf{i}} \rangle = \bar{u}_{\mathbf{f}} \Gamma_{\mathbf{fi}}^\mu(q^2) u_{\mathbf{i}}$$

$$\Gamma_{\mathbf{fi}}^\mu(q^2) = -\mu_{\mathbf{fi}}(q^2) i\sigma^{\mu\nu} q_\nu + d_{\mathbf{fi}}(q^2) i\sigma^{\mu\nu} q_\nu \gamma_5$$

- Diagonal ($\mathbf{i} = \mathbf{f}$) EDMM is zero for Majorana particles

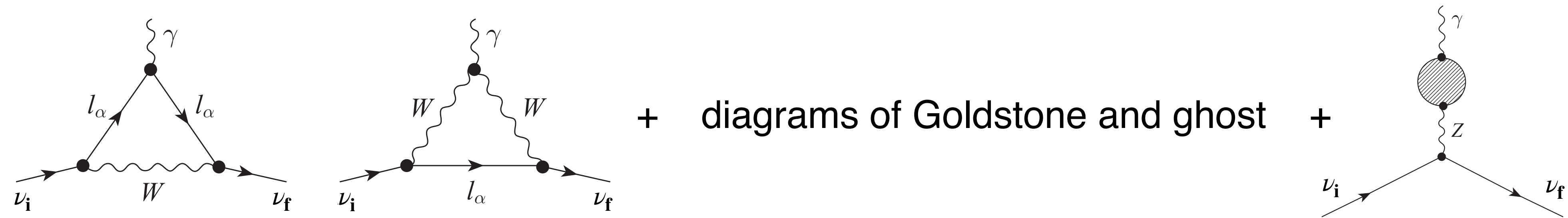
- Transition ($\mathbf{i} \neq \mathbf{f}$) EDMM $\Rightarrow \nu_{\mathbf{i}} \rightarrow \nu_{\mathbf{f}} + \gamma$ if $m_{\mathbf{i}} > m_{\mathbf{j}}$

- Early studies: Shrock, 1974; Petcov; Goldman & Stephenson, 1977; Schechter & Valle, 1981; Pal & Wolfenstein, Schechter & Valle; Shrock; Nieves; Kayser, 1982 ...

General electromagnetic property of light neutrinos

- Neutrino EMDM is generated via weak interaction of the SM

Full one-loop calc in electroweak symm with R_ξ gauge: Dvornikov & Studenikin, hep-ph/0305206; 0411085



Theoretical predictions: $d, \mu \sim \frac{eg^2}{16\pi^2} \frac{m_\nu}{M_W^2} \sim 10^{-20} \mu_B$ (diagonal), $\sim \frac{eg^2}{16\pi^2} \frac{m_\nu}{M_W^2} \frac{m_\tau^2}{M_W^2} \sim 10^{-24} \mu_B$ (transition)

Including non-unitarity effect: $d \sim \mu \lesssim 10^{-22} \mu_B$ (transition)

and $\gamma - Z$ self diagram is necessary to cancel infinity and electric charge.

For a full calc, see Xing & **YLZ**, 1201.2543

- Experimental progress

$$\mu \leq 2.9 \times 10^{-11} \mu_B$$

90%CL @ GEMMA (diagonal MDM)

$$\mu \in (1.4, 2.9) \times 10^{-11} \mu_B$$

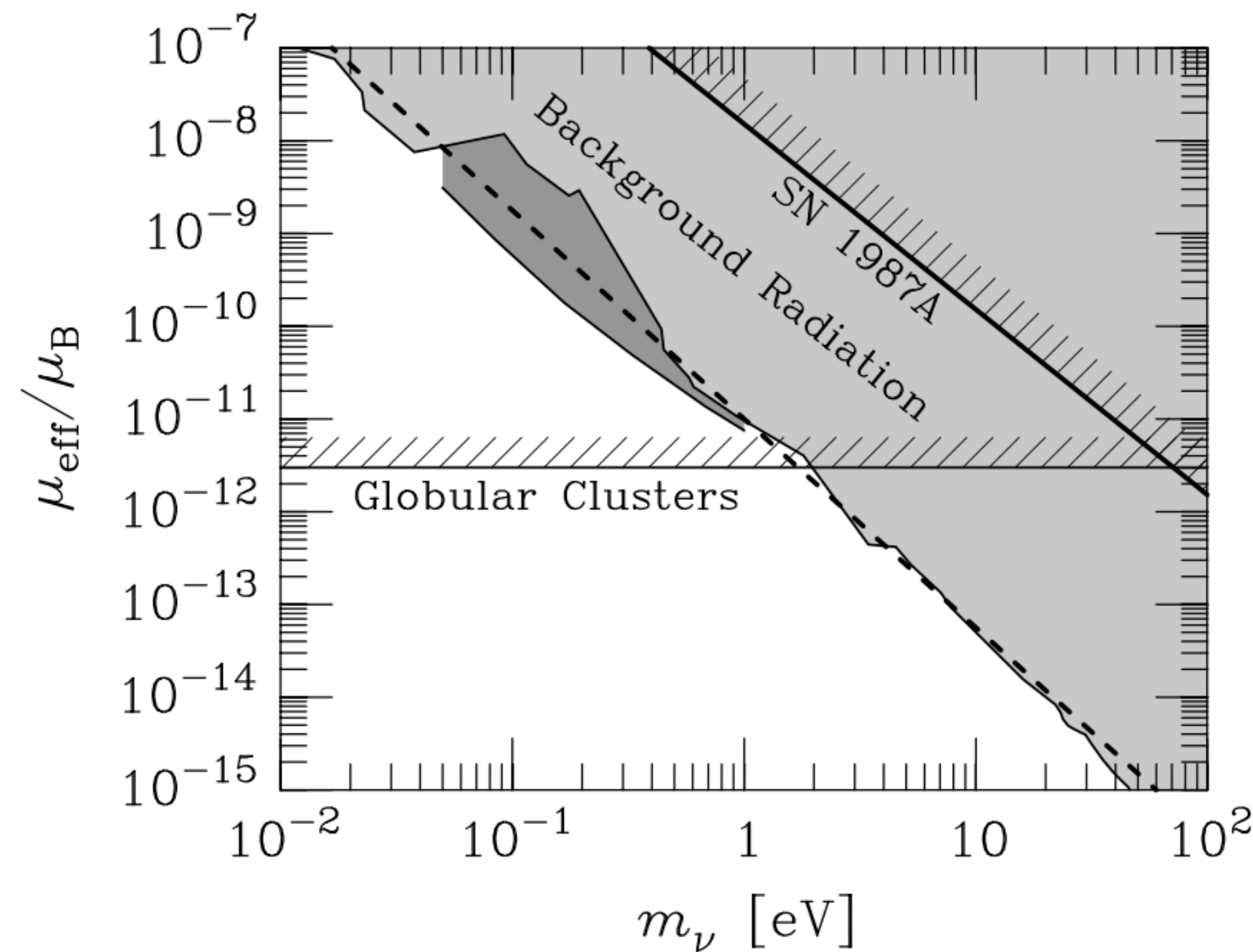
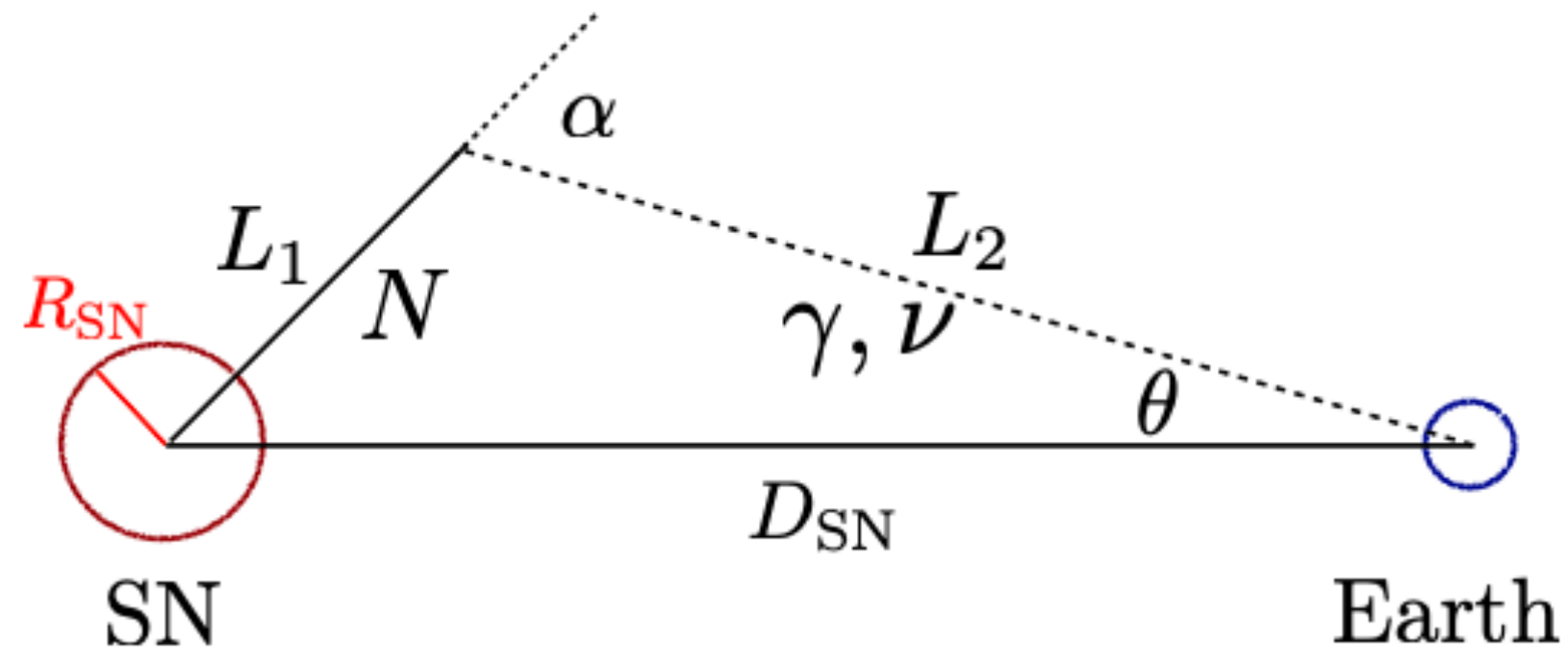
90% CL @ XENON1T, 2006.09721

Borexino, Super-K, TEXONO, DARWIN ...

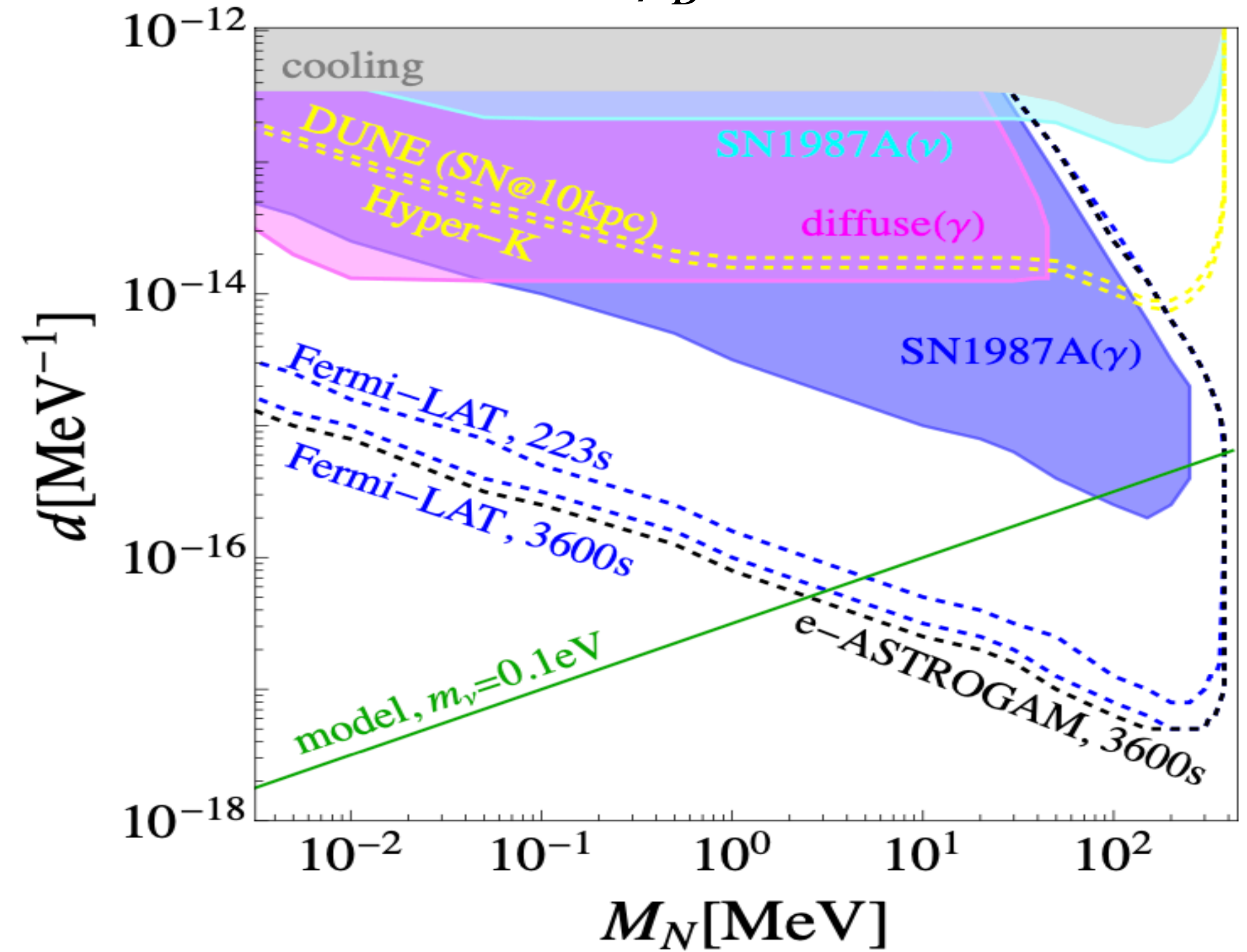
Electromagnetic property of heavier neutrinos

- Heavier neutrinos, $d, \mu \sim 10^{-20} \mu_B \frac{m_N}{m_\nu} \times$ (active-sterile mixing)

$$\text{MeV}^{-1} \simeq 3.3 \mu_B$$

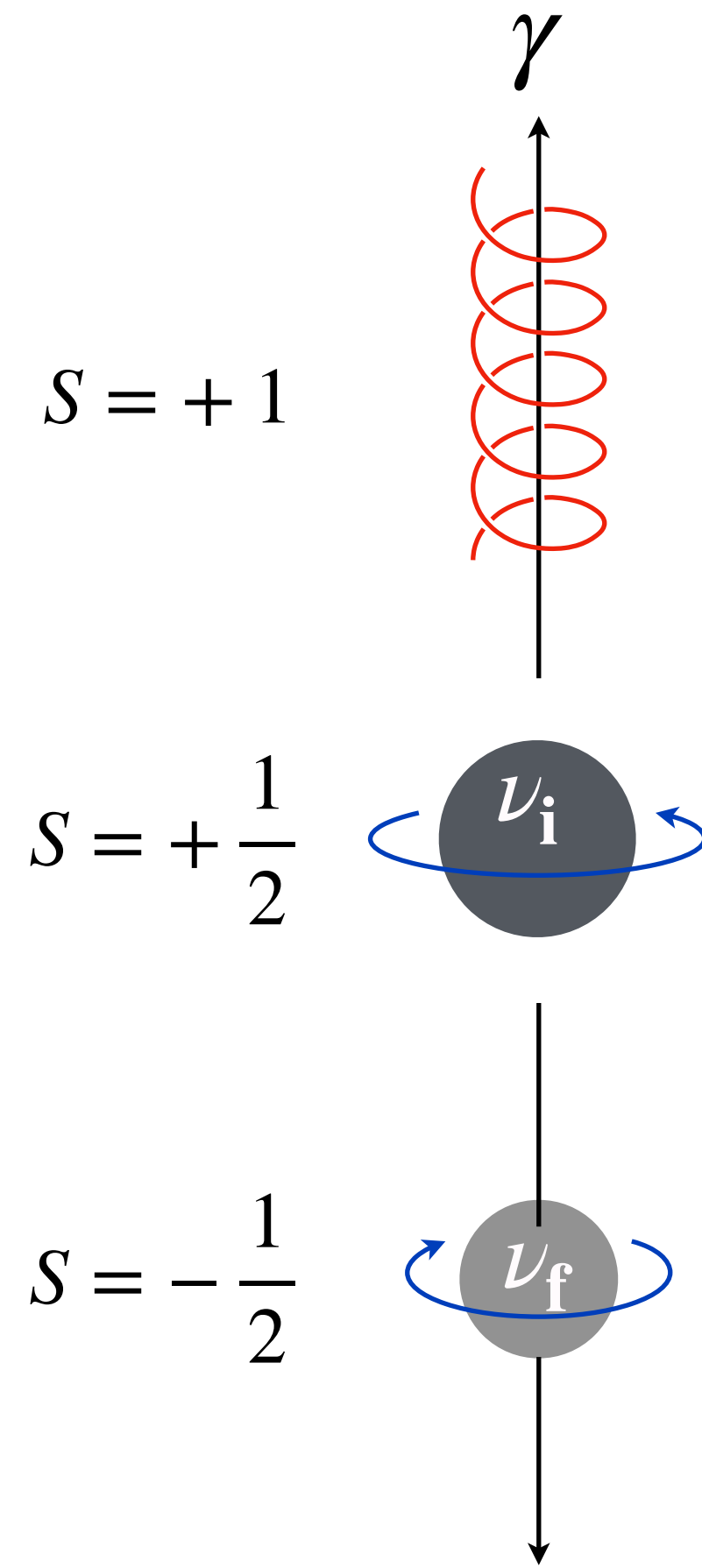


Giunti & Studenikin, 1403.6344



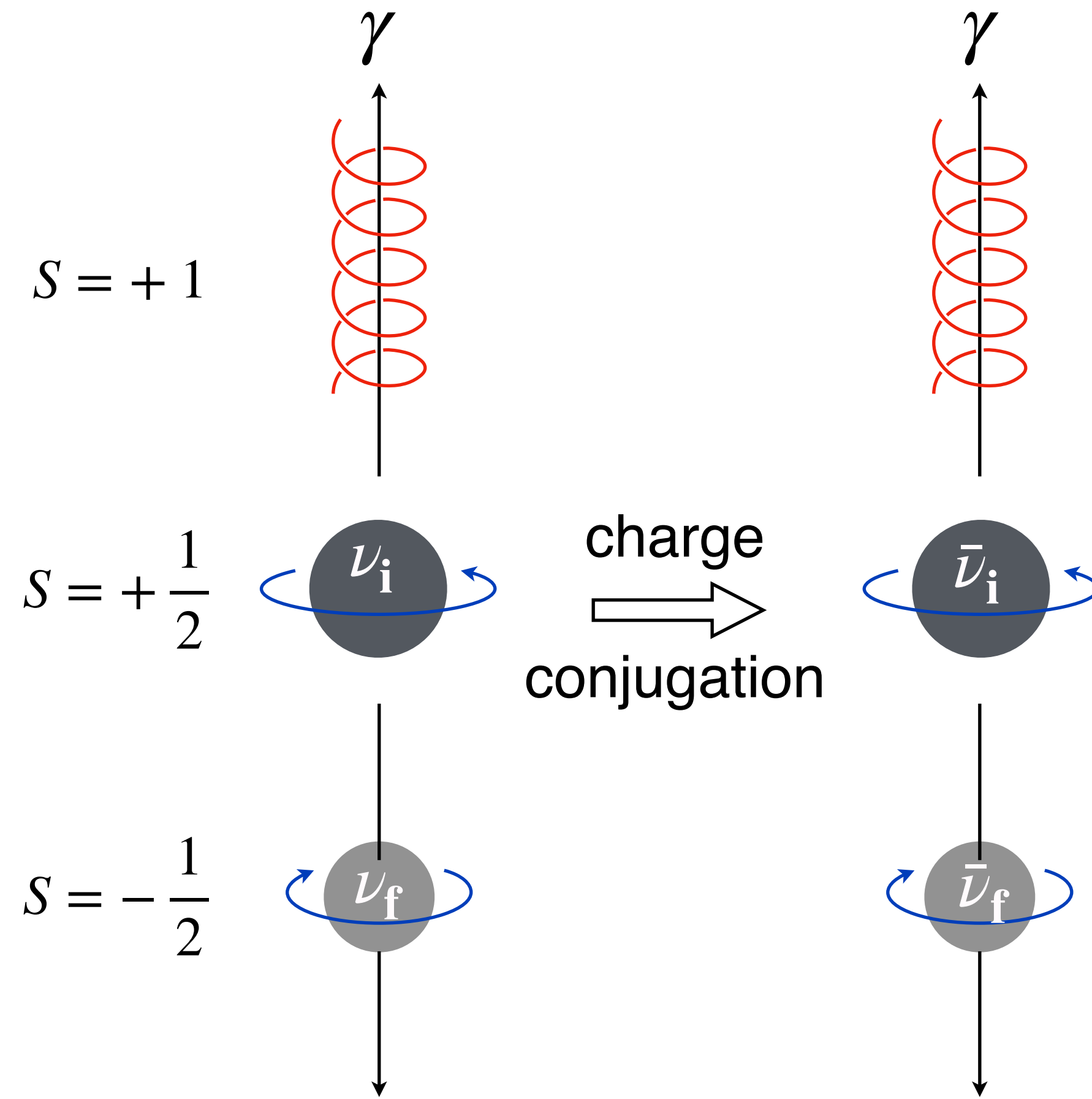
Brdar, de Gouvêa, Ying-Ying Li, Machado, 2302.10965

In the rest frame with photon released in +z direction

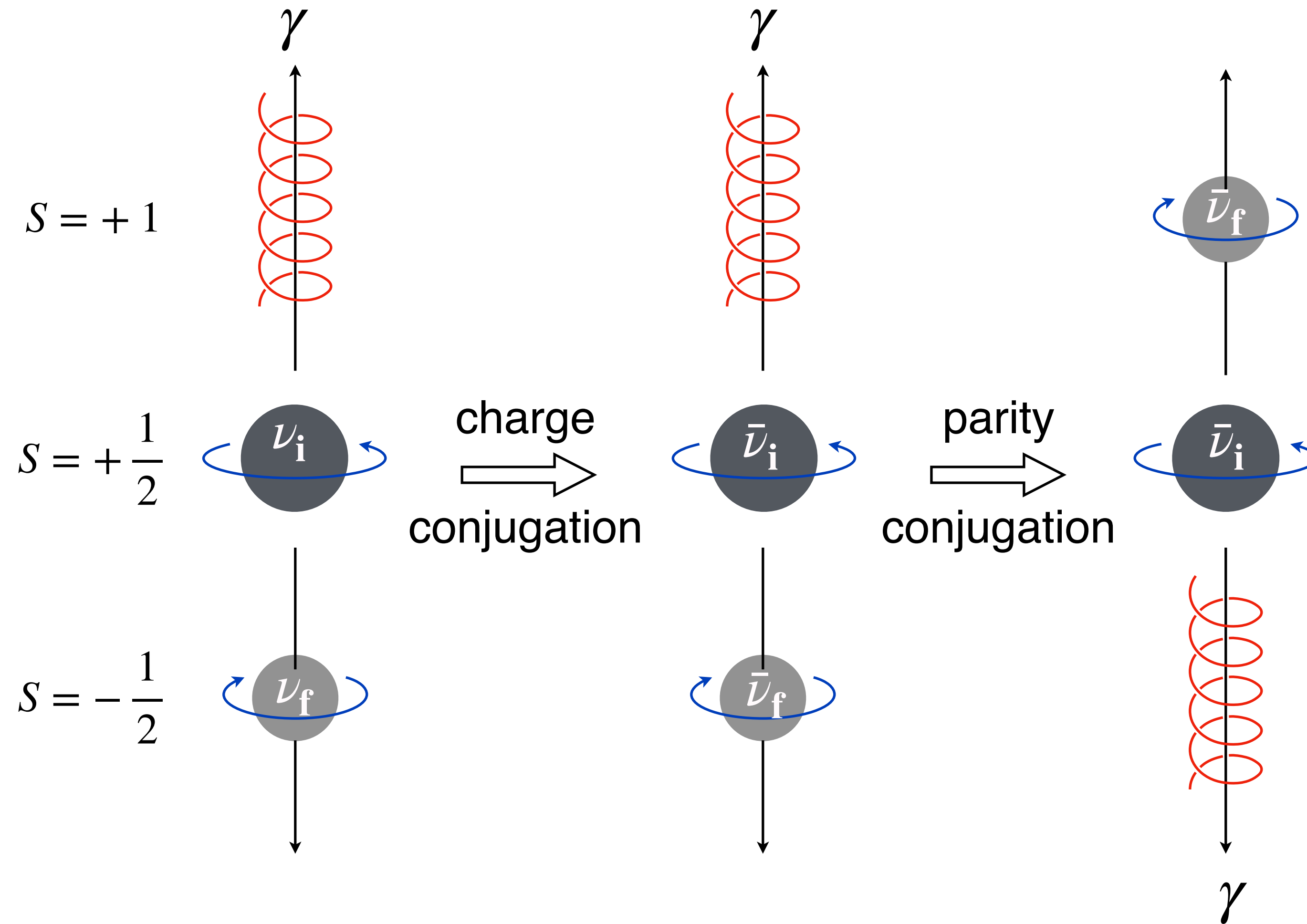


CP transformation in the Dirac neutrino case

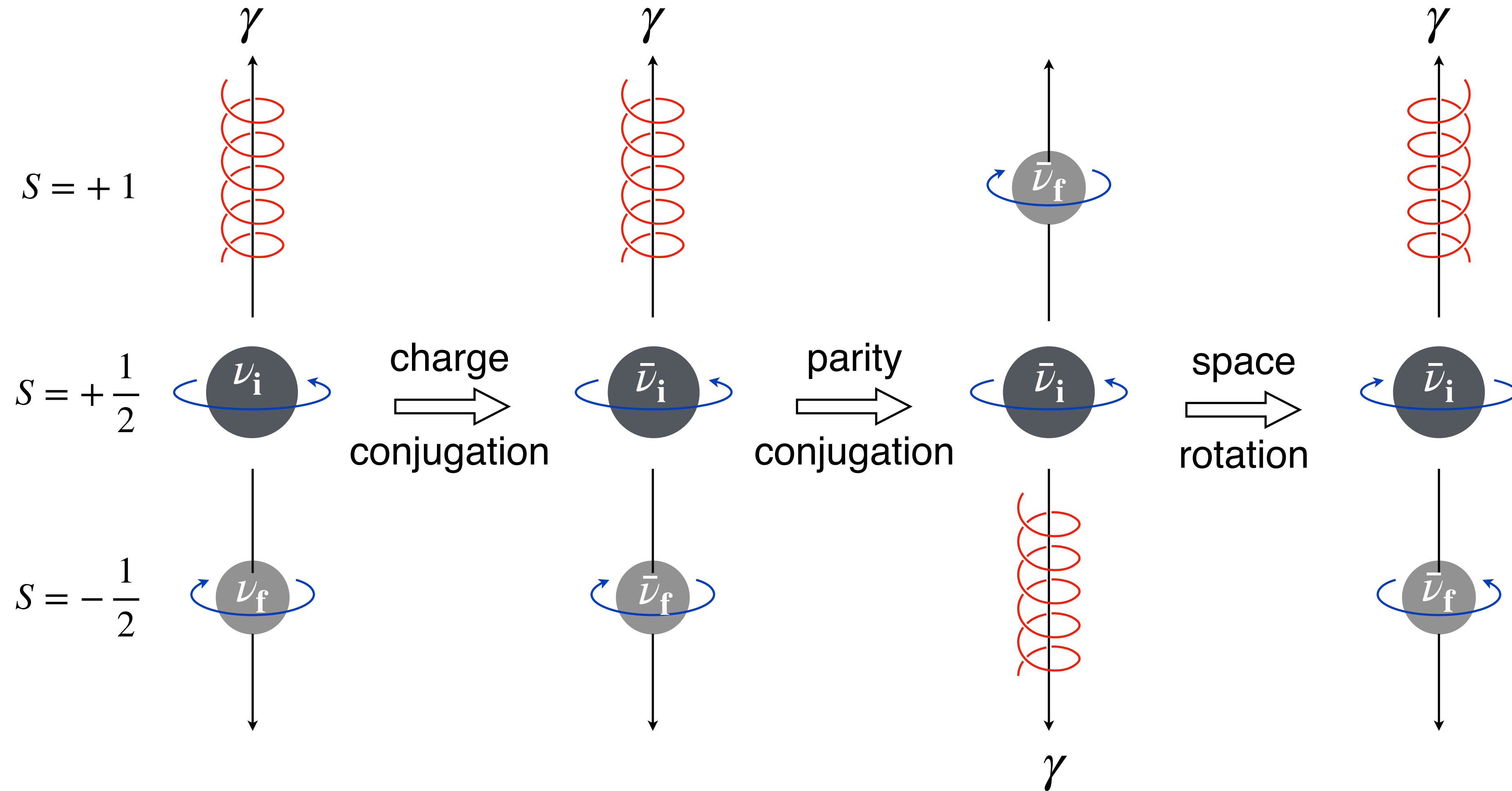
In the rest frame with photon released in +z direction



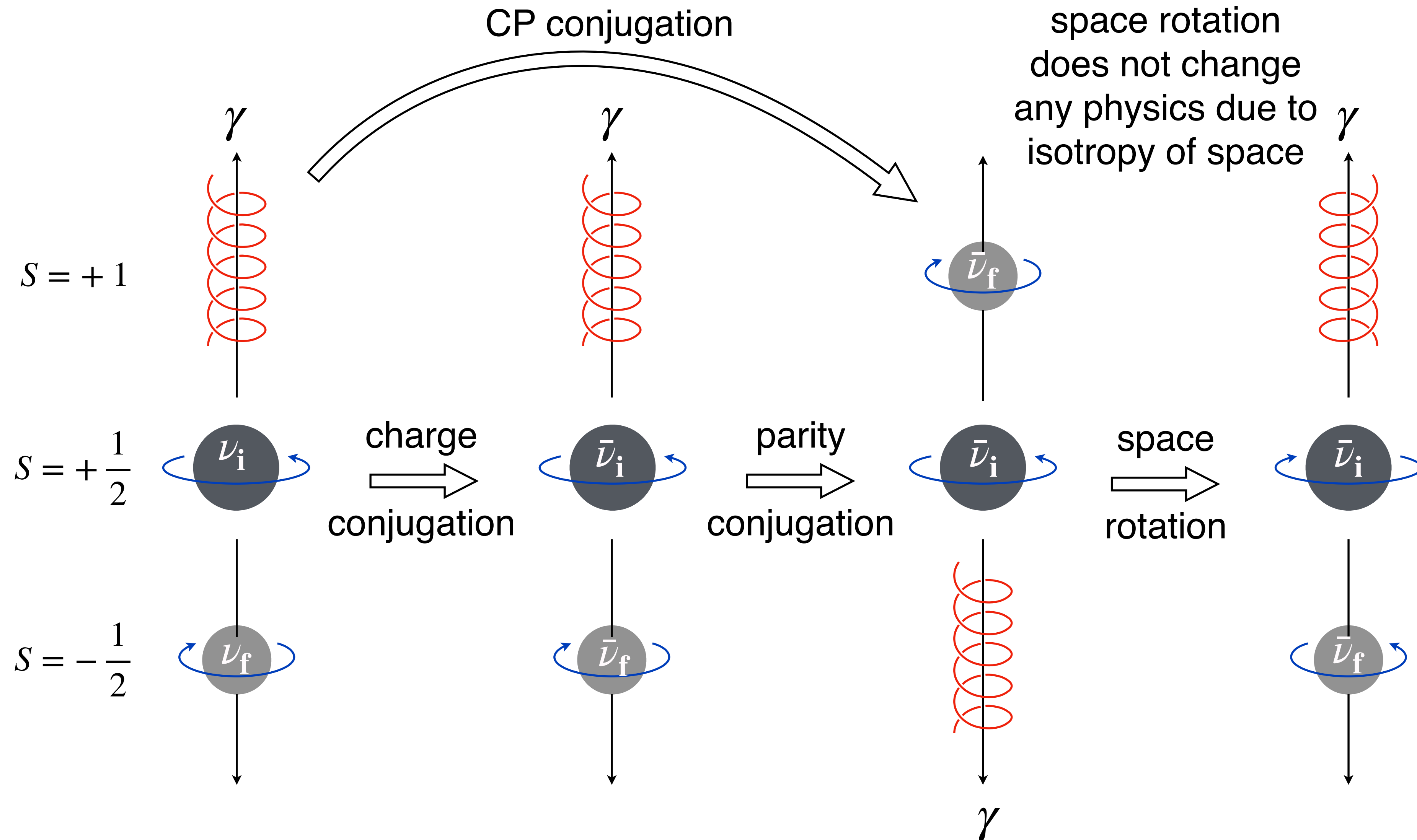
CP transformation in the Dirac neutrino case



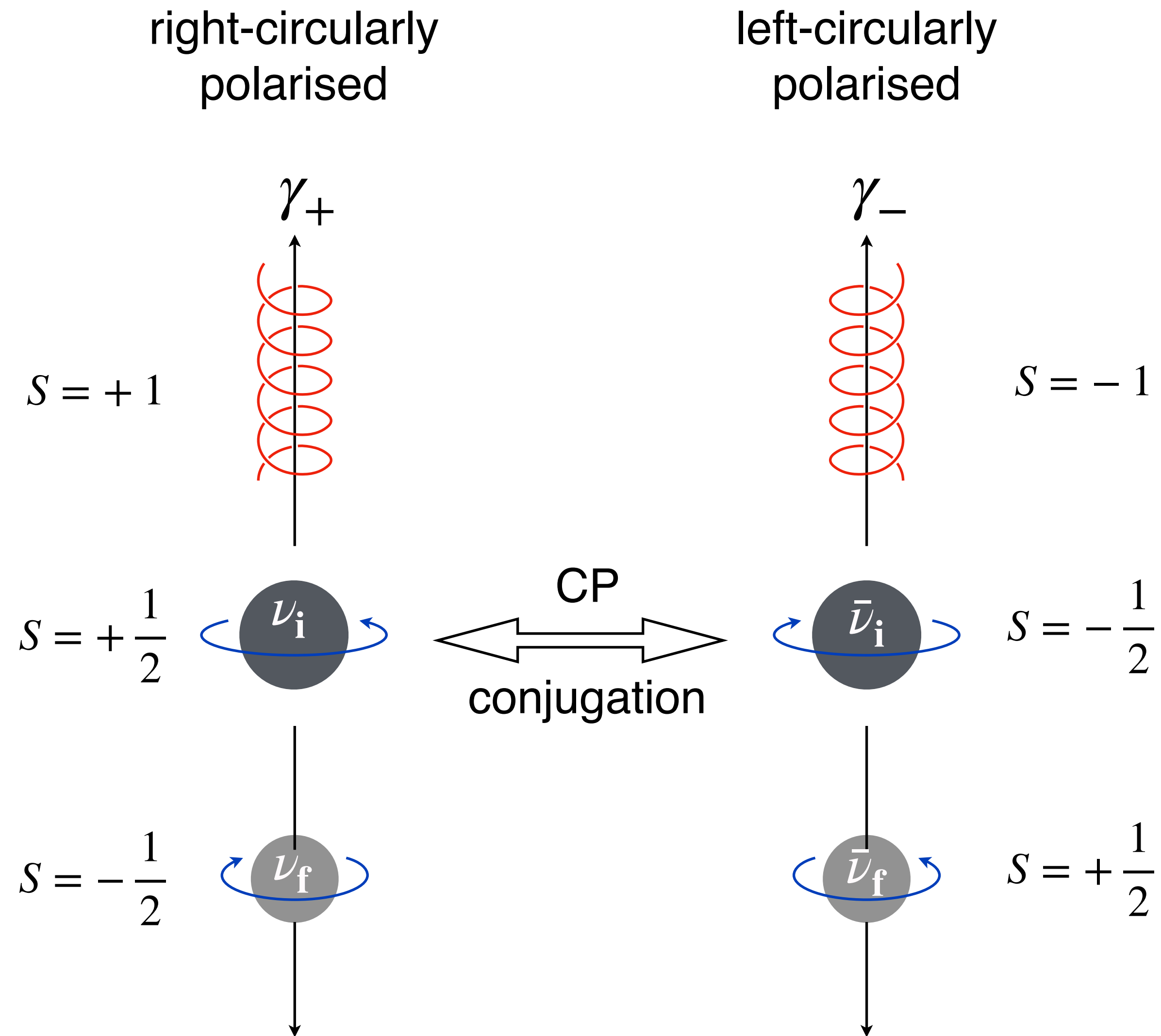
CP transformation in the Dirac neutrino case



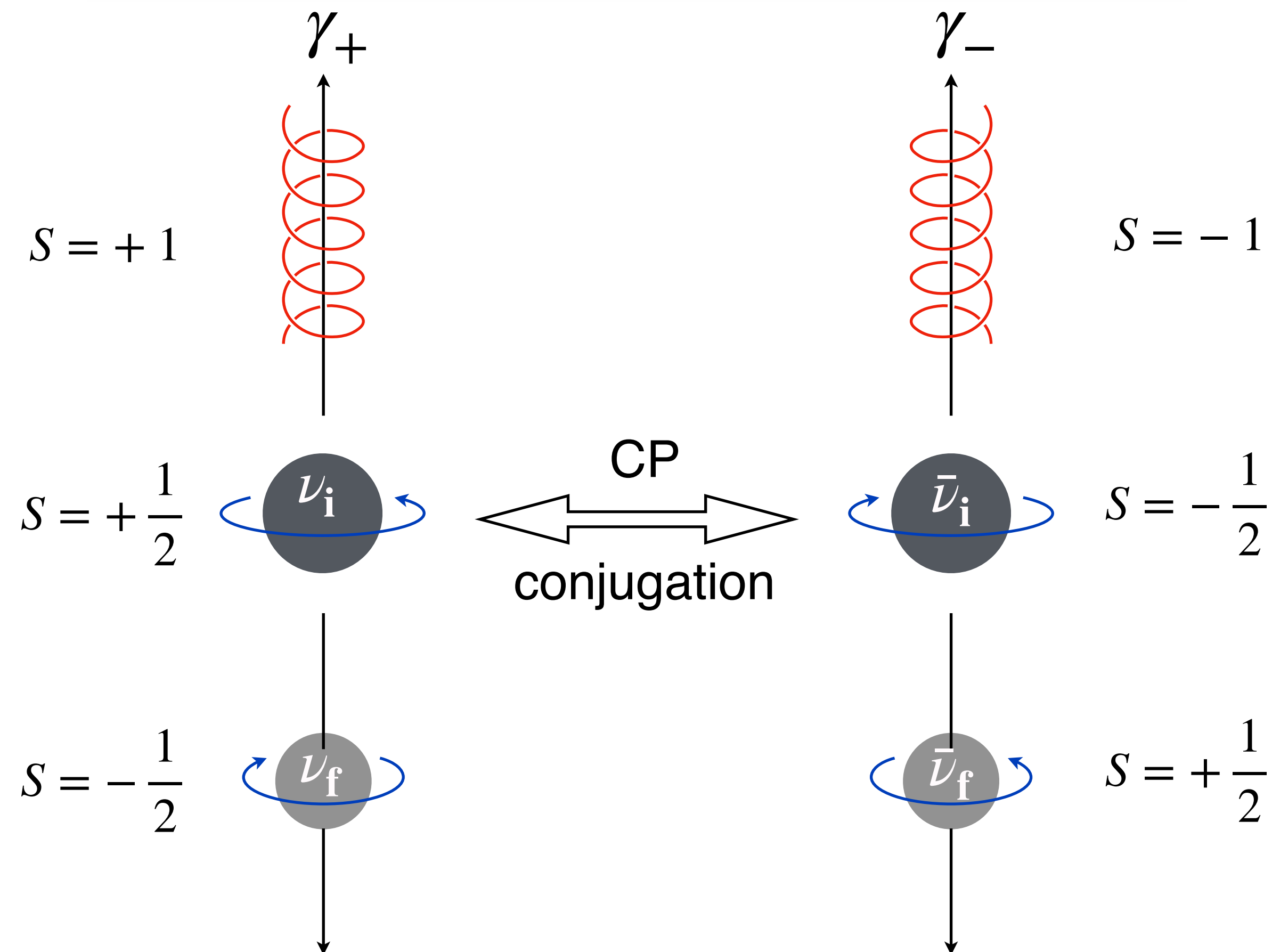
CP transformation in the Dirac neutrino case



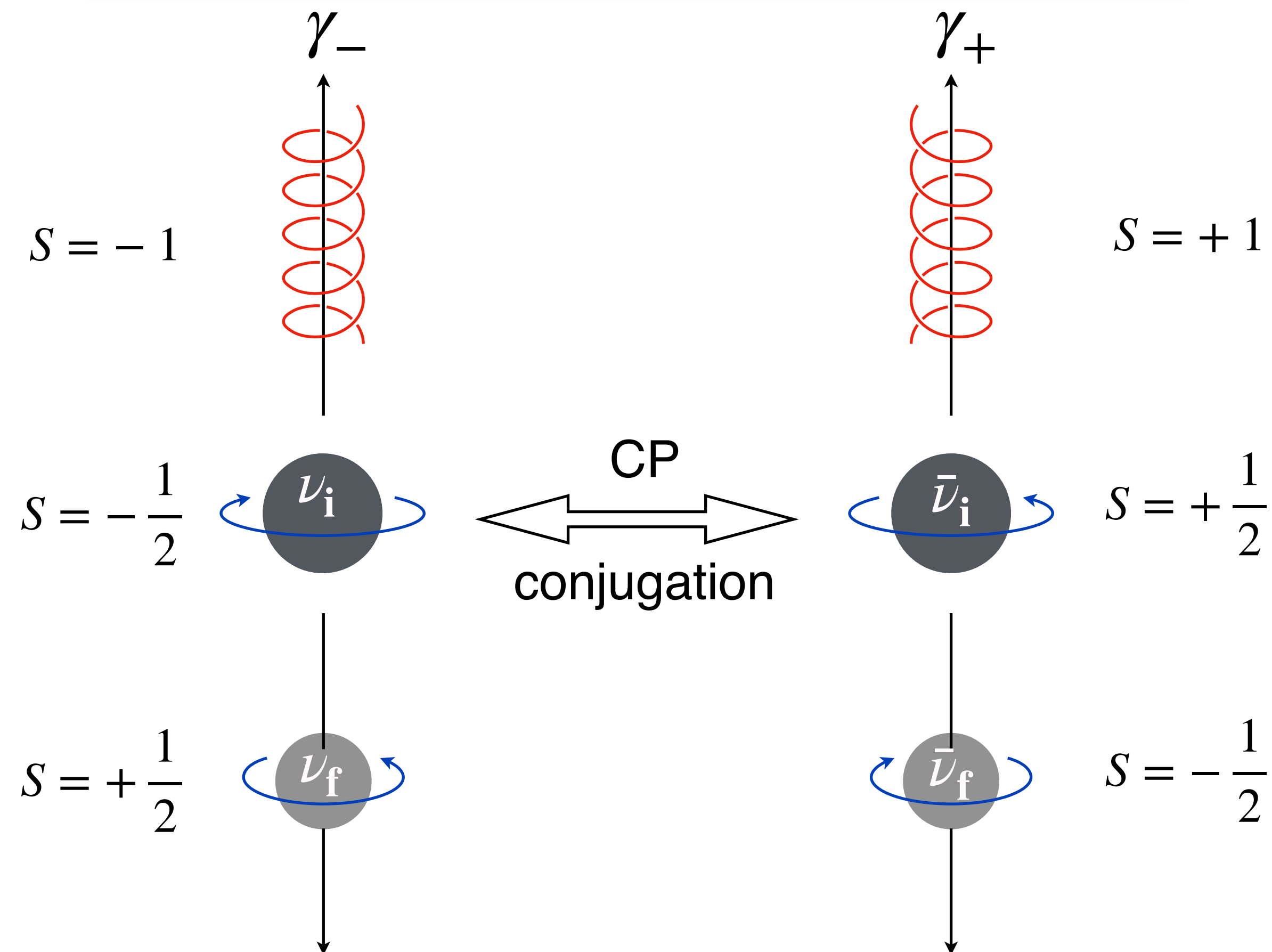
CP transformation for Dirac neutrinos



$$\Delta_{CP,+} = \frac{\Gamma(\nu_i \rightarrow \nu_f + \gamma_+) - \Gamma(\bar{\nu}_i \rightarrow \bar{\nu}_f + \gamma_-)}{\Gamma(\nu_i \rightarrow \nu_f + \gamma) + \Gamma(\bar{\nu}_i \rightarrow \bar{\nu}_f + \gamma)}$$

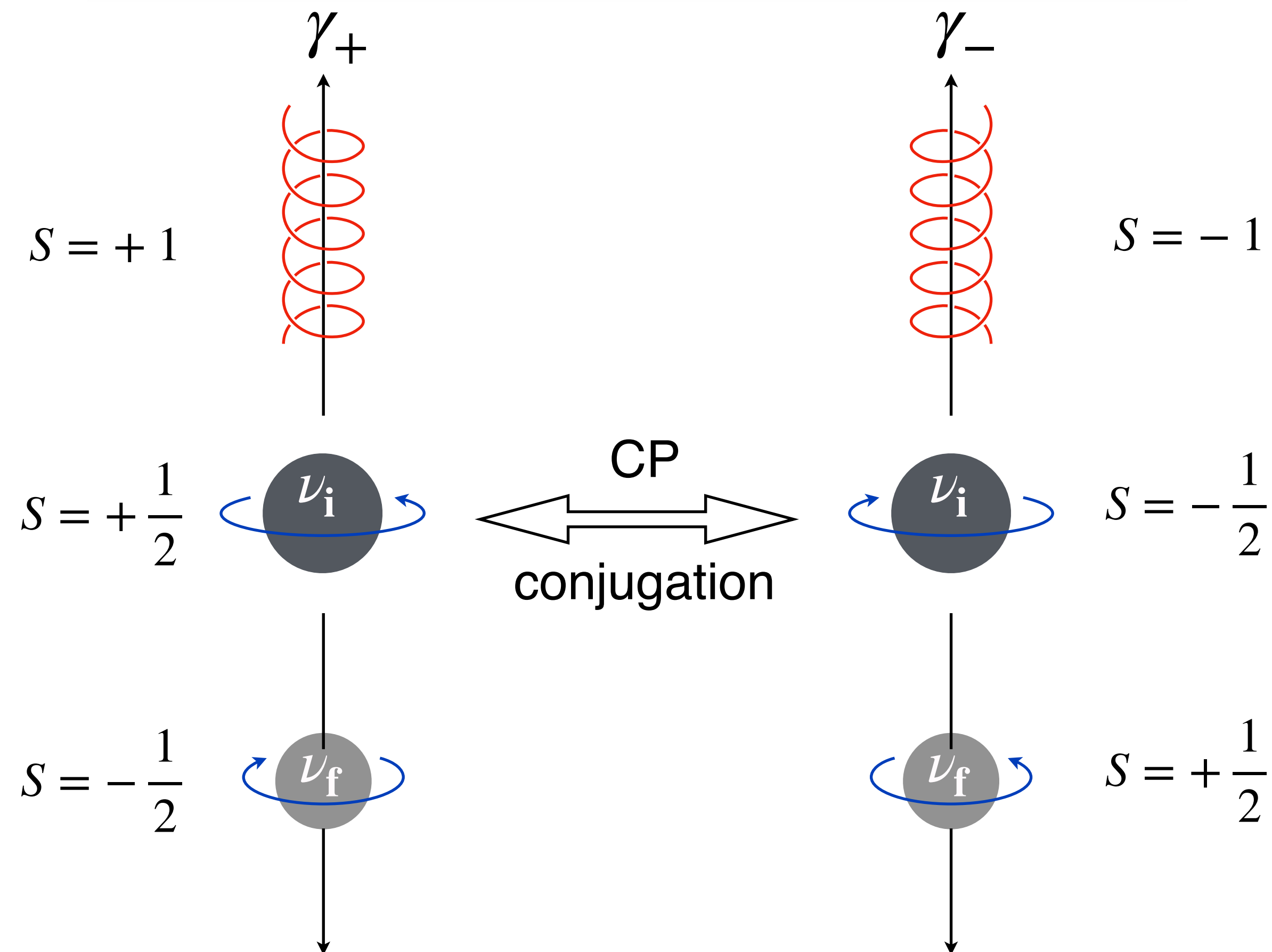


$$\Delta_{CP,-} = \frac{\Gamma(\nu_i \rightarrow \nu_f + \gamma_-) - \Gamma(\bar{\nu}_i \rightarrow \bar{\nu}_f + \gamma_+)}{\Gamma(\nu_i \rightarrow \nu_f + \gamma) + \Gamma(\bar{\nu}_i \rightarrow \bar{\nu}_f + \gamma)}$$



CP transformation for Majorana neutrinos

$$\Delta_{CP}^M = \frac{\Gamma(\nu_i \rightarrow \nu_f + \gamma_+) - \Gamma(\nu_i \rightarrow \nu_f + \gamma_-)}{\Gamma(\nu_i \rightarrow \nu_f + \gamma) + \Gamma(\nu_i \rightarrow \nu_f + \gamma)}$$



CP asymmetry in terms of form factors

- Re-express the form factor in the chiral representation

Form factor
for ν

$$\Gamma_{\mathbf{fi}}^\mu(q^2) = + i\sigma^{\mu\nu} q_\nu [f_{\mathbf{fi}}^L P_L + f_{\mathbf{fi}}^R P_R]$$

$$f_{\mathbf{fi}}^{L,R} = - \mu_{\mathbf{fi}} \pm id_{\mathbf{fi}}$$

$$P_{L,R} = (\mathbf{1} \pm \gamma_5)/2$$

Form factor
for $\bar{\nu}$

$$\bar{\Gamma}_{\mathbf{if}}^\mu(q^2) = + i\sigma^{\mu\nu} q_\nu [\bar{f}_{\mathbf{if}}^L P_L + \bar{f}_{\mathbf{if}}^R P_R]$$

$$\langle \nu_{\mathbf{f}} | j_\mu | \nu_{\mathbf{i}} \rangle = \bar{u}_{\mathbf{f}} \Gamma_{\mathbf{fi}}^\mu(q^2) u_{\mathbf{i}}$$

$$\langle \bar{\nu}_{\mathbf{f}} | j_\mu | \bar{\nu}_{\mathbf{i}} \rangle = \bar{v}_{\mathbf{i}} \bar{\Gamma}_{\mathbf{if}}^\mu(q^2) v_{\mathbf{f}}$$

CPT invariance

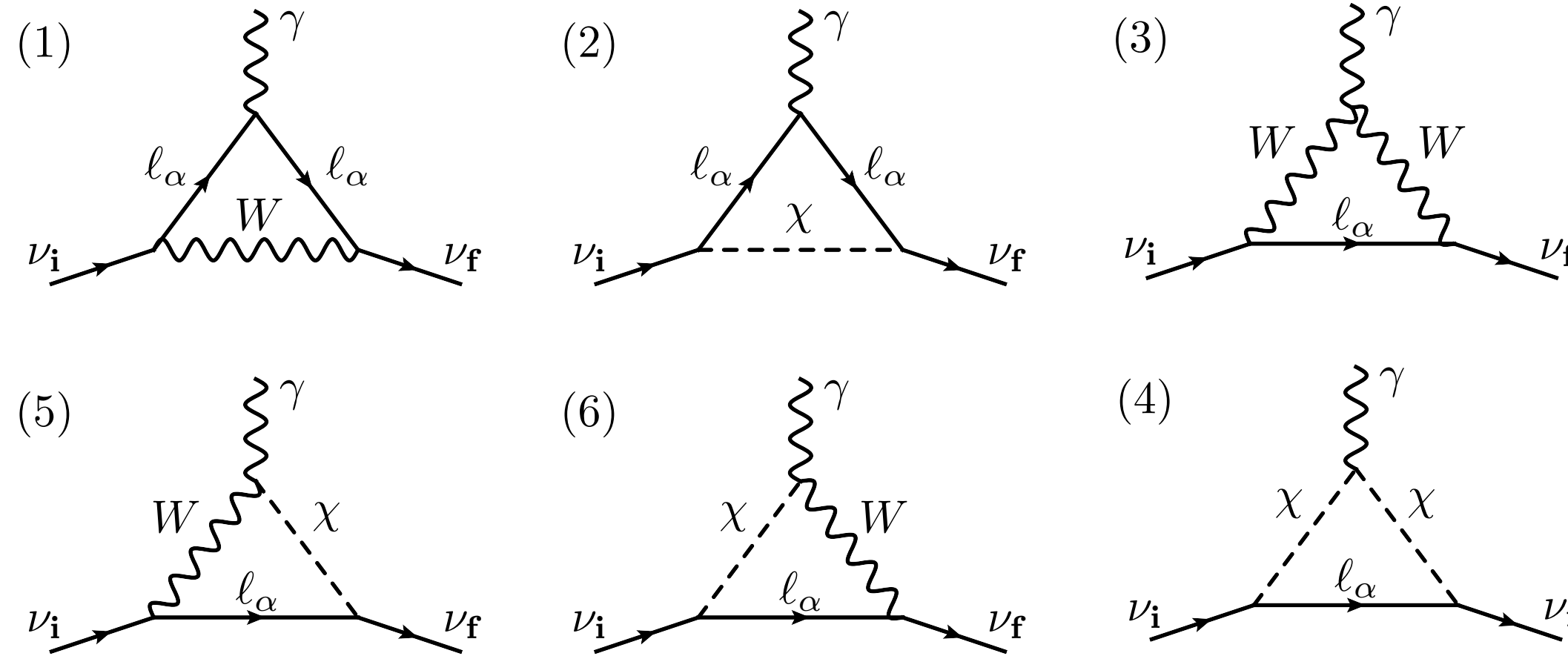
$$\mathcal{M}(\bar{\nu}_{\mathbf{i}} \rightarrow \bar{\nu}_{\mathbf{f}} + \gamma) = \mathcal{M}(\nu_{\mathbf{f}} + \gamma \rightarrow \nu_{\mathbf{i}}) \Rightarrow \bar{f}_{\mathbf{if}}^{L,R} = - f_{\mathbf{fi}}^{L,R}$$

$$\bar{\Gamma}_{\mathbf{if}}^\mu(q^2) = - i\sigma^{\mu\nu} q_\nu [f_{\mathbf{if}}^L P_L + f_{\mathbf{if}}^R P_R]$$

CP asymmetry
for Dirac ν

$$\Delta_{CP,+} = \frac{|f_{\mathbf{fi}}^L|^2 - |f_{\mathbf{if}}^R|^2}{|f_{\mathbf{fi}}^L|^2 + |f_{\mathbf{fi}}^R|^2 + |f_{\mathbf{if}}^R|^2 + |f_{\mathbf{if}}^L|^2},$$

$$\Delta_{CP,-} = \frac{|f_{\mathbf{fi}}^R|^2 - |f_{\mathbf{if}}^L|^2}{|f_{\mathbf{fi}}^L|^2 + |f_{\mathbf{fi}}^R|^2 + |f_{\mathbf{if}}^R|^2 + |f_{\mathbf{if}}^L|^2},$$



Summation \sum_{α}
for charged leptons
 $\alpha = e, \mu, \tau$ in the loop

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(1)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{\gamma_{\nu} P_L (\not{p}_f - \not{p} + m_{\alpha}) \gamma^{\mu} (\not{p}_i - \not{p} + m_{\alpha}) \gamma^{\nu} P_L}{[(p_f - p)^2 - m_{\alpha}^2][(p_i - p)^2 - m_{\alpha}^2][p^2 - m_W^2]},$$

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(2)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{(m_f P_L - m_{\alpha} P_R) (\not{p}_f - \not{p} + m_{\alpha}) \gamma^{\mu} (\not{p}_i - \not{p} + m_{\alpha}) (m_{\alpha} P_L - m_i P_R)}{m_W^2 [(p_f - p)^2 - m_{\alpha}^2][(p_i - p)^2 - m_{\alpha}^2][p^2 - m_W^2]},$$

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(3)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{\gamma_{\rho} P_L (\not{p} + m_{\alpha}) \gamma_{\nu} P_L V^{\mu\nu\rho}}{[(p_f - p)^2 - m_W^2][(p_i - p)^2 - m_W^2][p^2 - m_{\alpha}^2]},$$

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(4)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{(2p - p_i - p_f)^{\mu} (m_f P_L - m_{\alpha} P_R) (\not{p} + m_{\alpha}) (m_{\alpha} P_L - m_i P_R)}{m_W^2 [(p_f - p)^2 - m_W^2][(p_i - p)^2 - m_W^2][p^2 - m_{\alpha}^2]},$$

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(5)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{\gamma^{\mu} P_L (\not{p} + m_{\alpha}) (m_{\alpha} P_L - m_i P_R)}{[(p_f - p)^2 - m_W^2][(p_i - p)^2 - m_W^2][p^2 - m_{\alpha}^2]},$$

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(6)} = i \frac{eg^2}{2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \int \frac{d^4 p}{(2\pi)^4} \frac{(m_{\alpha} P_R - m_f P_L) (\not{p} + m_{\alpha}) \gamma^{\mu} P_L}{[(p_f - p)^2 - m_W^2][(p_i - p)^2 - m_W^2][p^2 - m_{\alpha}^2]},$$

$$V^{\mu\nu\rho} = g^{\mu\nu} (2p_i - p - p_f)^{\rho} + g^{\rho\mu} (2p_f - p - p_i)^{\nu} + g^{\nu\rho} (2p - p_i - p_f)^{\mu}.$$

- Neutrino form factor in radiative decay

$$\Gamma_{\mathbf{fi},\alpha}^{\mu,(k)} = \frac{eG_F}{4\sqrt{2}\pi^2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \left[i\sigma^{\mu\nu} q_\nu (\mathcal{F}_{\mathbf{fi},\alpha} m_i P_R + \mathcal{F}_{\mathbf{if},\alpha} m_f P_L) \right].$$

coefficients in the coupling

kinetic term

- Loop function in the kinetic term

$$\begin{aligned} \mathcal{F}_{\mathbf{fi},\alpha} = & \int_0^1 dx \left\{ \frac{(m_i^2 - m_\alpha^2 - 2m_W^2)(m_\alpha^2 + m_f^2 x^2) + m_{\mathbf{fi},\alpha}^4 x}{(m_i^2 - m_f^2)^2 x} \log \left(\frac{m_\alpha^2 + (m_W^2 - m_\alpha^2 - m_i^2)x + m_i^2 x^2}{m_\alpha^2 + (m_W^2 - m_\alpha^2 - m_f^2)x + m_f^2 x^2} \right) \right. \\ & + \left. \frac{(m_i^2 - m_\alpha^2 - 2m_W^2)(m_\alpha^2 + m_f^2(1-x)^2) + m_{\mathbf{fi},\alpha}^4(1-x)}{(m_i^2 - m_f^2)^2 x} \log \left(\frac{m_W^2 + (m_\alpha^2 - m_W^2 - m_i^2)x + m_i^2 x^2}{m_W^2 + (m_\alpha^2 - m_W^2 - m_f^2)x + m_f^2 x^2} \right) \right\} \\ & + \frac{m_f^2 - m_\alpha^2 - 2m_W^2}{m_i^2 - m_f^2}, \quad m_{\mathbf{fi},\alpha}^4 = -(m_i^2 - m_\alpha^2 - m_W^2)(m_f^2 + m_\alpha^2 - 2m_W^2) + 2m_\alpha^2 m_W^2 \end{aligned}$$

- Neutrino form factor in radiative decay

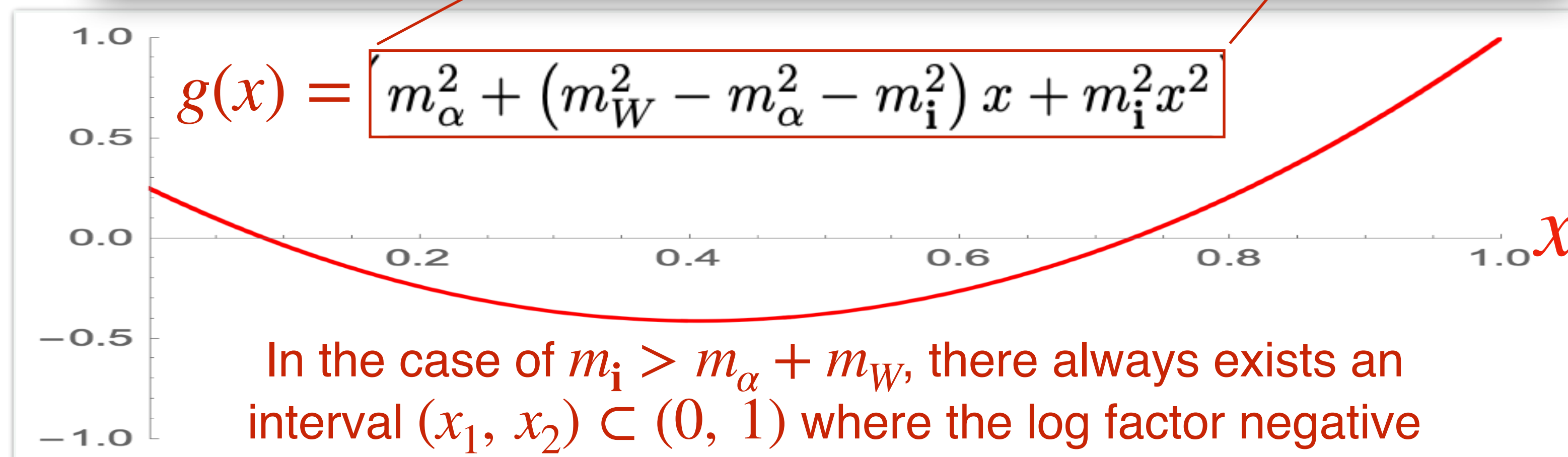
$$\Gamma_{\text{fi},\alpha}^{\mu,(k)} = \frac{eG_F}{4\sqrt{2}\pi^2} \mathcal{U}_{\alpha i} \mathcal{U}_{\alpha f}^* \left[i\sigma^{\mu\nu} q_\nu (\mathcal{F}_{\text{fi},\alpha} m_i P_R + \mathcal{F}_{\text{if},\alpha} m_f P_L) \right].$$

coefficients in the coupling

kinetic term

- Loop function in the kinetic term

$$\mathcal{F}_{\text{fi},\alpha} = \int_0^1 dx \left\{ \frac{(m_i^2 - m_\alpha^2 - 2m_W^2)(m_\alpha^2 + m_f^2 x^2) + m_{\text{fi},\alpha}^4 x}{(m_i^2 - m_f^2)^2 x} \log \left(\frac{m_\alpha^2 + (m_W^2 - m_\alpha^2 - m_i^2)x + m_i^2 x^2}{m_\alpha^2 + (m_W^2 - m_\alpha^2 - m_f^2)x + m_f^2 x^2} \right) \right. \\ \left. + \frac{(m_i^2 - m_\alpha^2 - 2m_W^2)(m_\alpha^2 + m_f^2(1-x)^2) + m_{\text{fi},\alpha}^4(1-x)}{(m_i^2 - m_f^2)^2 x} \log \left(\frac{m_W^2 + (m_\alpha^2 - m_W^2 - m_i^2)x + m_i^2 x^2}{m_W^2 + (m_\alpha^2 - m_W^2 - m_f^2)x + m_f^2 x^2} \right) \right\} \\ + \frac{m_f^2 - m_\alpha^2 - 2m_W^2}{m_i^2 - m_f^2}, \quad m_{\text{fi},\alpha}^4 = -(m_i^2 - m_\alpha^2 - m_W^2)(m_f^2 + m_\alpha^2 - 2m_W^2) + 2m_\alpha^2 m_W^2$$



Explicit result of the imaginary part of loop integration

- Using the following formula, we finally obtain

$$\int_0^1 dx f(x) \log g(x) = \int_0^1 dx f(x) \log |g(x)| + i\pi \int_{x_1}^{x_2} dx f(x).$$

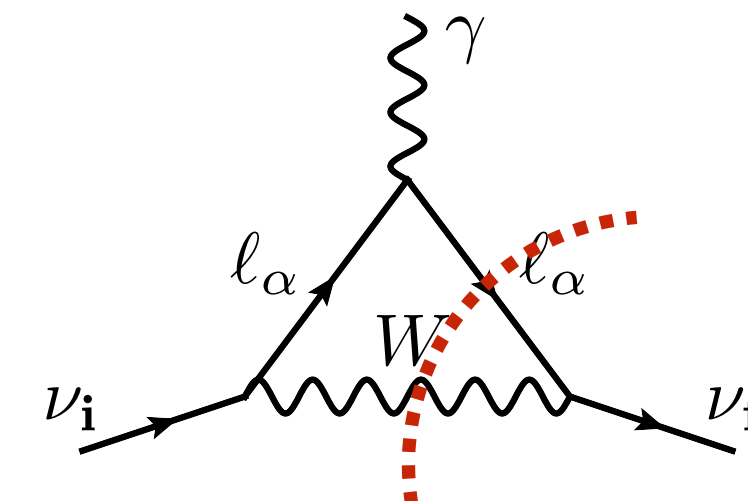
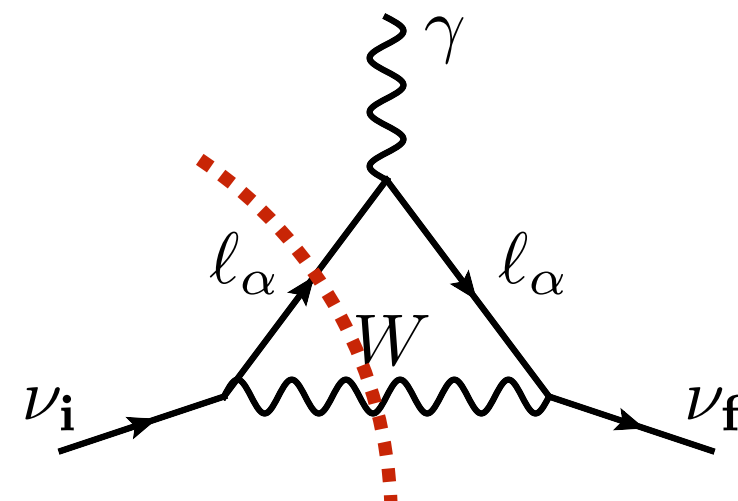
$$\begin{aligned} \text{Im}(\mathcal{F}_{\text{fi},\alpha}) = & \pi \vartheta(m_i - m_W - m_\alpha) \left\{ \frac{m_i^2 - m_\alpha^2 - 2m_W^2}{(m_i^2 - m_f^2)^2} \left[-\mu_i^2 \frac{m_f^2}{m_i^2} + m_\alpha^2 \log \left(\frac{m_i^2 + m_\alpha^2 - m_W^2 + \mu_i^2}{m_i^2 + m_\alpha^2 - m_W^2 - \mu_i^2} \right) \right] \right. \\ & \left. + \frac{(2m_i^2 - m_f^2 - m_\alpha^2 - 2m_W^2) m_W^2}{(m_i^2 - m_f^2)^2} \log \left(\frac{m_i^2 - m_\alpha^2 + m_W^2 + \mu_i^2}{m_i^2 - m_\alpha^2 + m_W^2 - \mu_i^2} \right) \right\} \\ & + \pi \vartheta(m_f - m_W - m_\alpha) \left\{ -\frac{m_i^2 - m_\alpha^2 - 2m_W^2}{(m_i^2 - m_f^2)^2} \left[-\mu_f^2 + m_\alpha^2 \log \left(\frac{m_f^2 + m_\alpha^2 - m_W^2 + \mu_f^2}{m_f^2 + m_\alpha^2 - m_W^2 - \mu_f^2} \right) \right] \right. \\ & \left. + \frac{(2m_i^2 - m_f^2 - m_\alpha^2 - 2m_W^2) m_W^2}{(m_i^2 - m_f^2)^2} \log \left(\frac{m_f^2 - m_\alpha^2 + m_W^2 + \mu_f^2}{m_f^2 - m_\alpha^2 + m_W^2 - \mu_f^2} \right) \right\}, \end{aligned}$$

$$\mu_i^2 = \sqrt{m_i^4 + m_\alpha^4 + m_W^4 - 2m_i^2 m_\alpha^2 - 2m_i^2 m_W^2 - 2m_\alpha^2 m_W^2},$$

$$\mu_f^2 = \sqrt{m_f^4 + m_\alpha^4 + m_W^4 - 2m_f^2 m_\alpha^2 - 2m_f^2 m_W^2 - 2m_\alpha^2 m_W^2}.$$

In the case $m_f > m_\alpha + m_W$, log of the m_f -dependent term generates another imaginary term, which partially cancel the one from the m_i -dependent term.

The result is consistent with optical theorem:



- Factorisation of coefficient contributions

	Imaginary (Jarlskog-like parameters)	Real
Dirac & Majorana	$\mathcal{J}_{\alpha\beta}^{\text{if}} = \text{Im}(\mathcal{U}_{\alpha i}\mathcal{U}_{\alpha f}^*\mathcal{U}_{\beta i}^*\mathcal{U}_{\beta f})$,	$\mathcal{R}_{\alpha\beta}^{\text{if}} = \text{Re}(\mathcal{U}_{\alpha i}\mathcal{U}_{\alpha f}^*\mathcal{U}_{\beta i}^*\mathcal{U}_{\beta f})$.
Majorana	$\mathcal{V}_{\alpha\beta}^{\text{if}} = \text{Im}(\mathcal{U}_{\alpha i}\mathcal{U}_{\alpha f}^*\mathcal{U}_{\beta i}\mathcal{U}_{\beta f}^*)$,	$\mathcal{C}_{\alpha\beta}^{\text{if}} = \text{Re}(\mathcal{U}_{\alpha i}\mathcal{U}_{\alpha f}^*\mathcal{U}_{\beta i}\mathcal{U}_{\beta f}^*)$.

- CP asymmetry for Dirac neutrinos

$$\Delta_{CP,+}^{\text{D}} = \frac{-\sum_{\alpha,\beta} \mathcal{J}_{\alpha\beta}^{\text{if}} \text{Im}(\mathcal{F}_{\text{if},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{f}}^2}{\sum_{\alpha,\beta} \mathcal{R}_{\alpha\beta}^{\text{if}} \left[\text{Re}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{fi},\beta}^*)m_{\text{i}}^2 + \text{Re}(\mathcal{F}_{\text{if},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{f}}^2 \right]},$$

$$\Delta_{CP,-}^{\text{D}} = \frac{-\sum_{\alpha,\beta} \mathcal{J}_{\alpha\beta}^{\text{if}} \text{Im}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{fi},\beta}^*)m_{\text{i}}^2}{\sum_{\alpha,\beta} \mathcal{R}_{\alpha\beta}^{\text{if}} \left[\text{Re}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{fi},\beta}^*)m_{\text{i}}^2 + \text{Re}(\mathcal{F}_{\text{if},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{f}}^2 \right]},$$

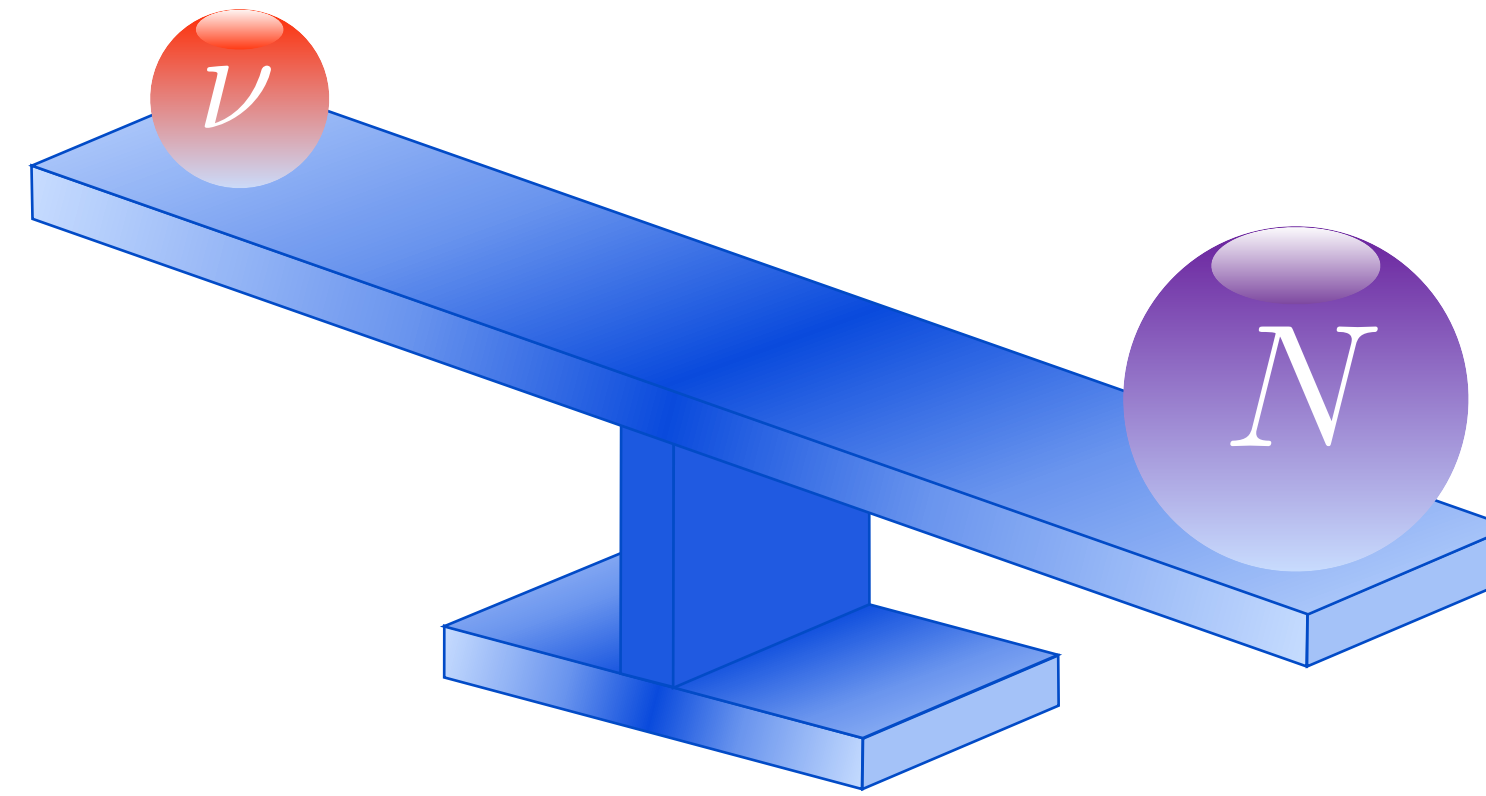
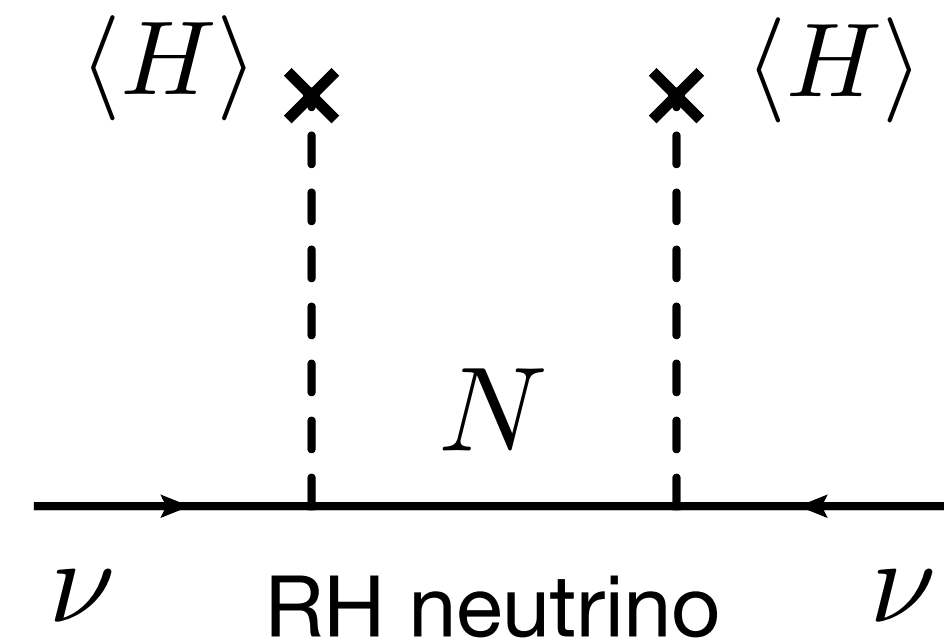
Interference between
charged leptons with
different masses
(always satisfied)

- CP asymmetry for Majorana neutrinos

$$\Delta_{CP}^{\text{M}} = \frac{\sum_{\alpha,\beta} \mathcal{J}_{\alpha\beta}^{\text{if}} \left[\text{Im}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{fi},\beta}^*)m_{\text{i}}^2 - \text{Im}(\mathcal{F}_{\text{if},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{f}}^2 \right] - 2\mathcal{V}_{\alpha\beta}^{\text{if}} \text{Im}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{i}}m_{\text{f}}}{\sum_{\alpha,\beta} \mathcal{R}_{\alpha\beta}^{\text{if}} \left[\text{Re}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{fi},\beta}^*)m_{\text{i}}^2 + \text{Re}(\mathcal{F}_{\text{if},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{f}}^2 \right] - 2\mathcal{C}_{\alpha\beta}^{\text{if}} \text{Re}(\mathcal{F}_{\text{fi},\alpha}\mathcal{F}_{\text{if},\beta}^*)m_{\text{i}}m_{\text{f}}},$$

CP asymmetries in different channels in seesaw

- Seesaw mechanism



$$\mathcal{M}_{\nu+N} = \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \Rightarrow \begin{cases} M_\nu = -M_D M_R^{-1} M_D^T \\ \mathcal{U} = \begin{pmatrix} U & R \\ \times & \times \end{pmatrix} \end{cases} \quad R: \text{active-sterile mixing}$$

- minimal seesaw: two RH neutrinos N_1 and $N_2 \Rightarrow m_1 = 0$

We fix the mass ordering $M_2 > M_1$ such that N_2 can decay to N_1

Casas-Ibarra parametrisation

$$R_{\alpha I} = \sum_{i=1,2} U_{\alpha i} \Omega_{iI} \sqrt{\frac{m_{i+1}}{M_I}} \quad \Omega = \begin{pmatrix} \cos \omega & \sin \omega \\ -\zeta \sin \omega & \zeta \cos \omega \end{pmatrix} \quad \begin{array}{l} \omega \text{ is a complex mixing angle} \\ \zeta = \pm 1 \end{array}$$

- $\nu_i \rightarrow \nu_j + \gamma \quad \Rightarrow \quad \text{no CP violation}$

- $N_I \rightarrow \nu + \gamma$ with $M_I > M_W$

$$\Delta_{CP}(N_I \rightarrow \nu\gamma) = \frac{\sum_i \sum_{\alpha,\beta} \mathcal{J}_{\alpha\beta}^{(I+3)i} \text{Im}(\mathcal{F}_{i(I+3),\alpha} \mathcal{F}_{i(I+3),\beta}^*)}{\sum_i \sum_{\alpha,\beta} \mathcal{R}_{\alpha\beta}^{(I+3)i} \text{Re}(\mathcal{F}_{i(I+3),\alpha} \mathcal{F}_{i(I+3),\beta}^*)} \lesssim 10^{-17}$$

\Rightarrow very small CP violation

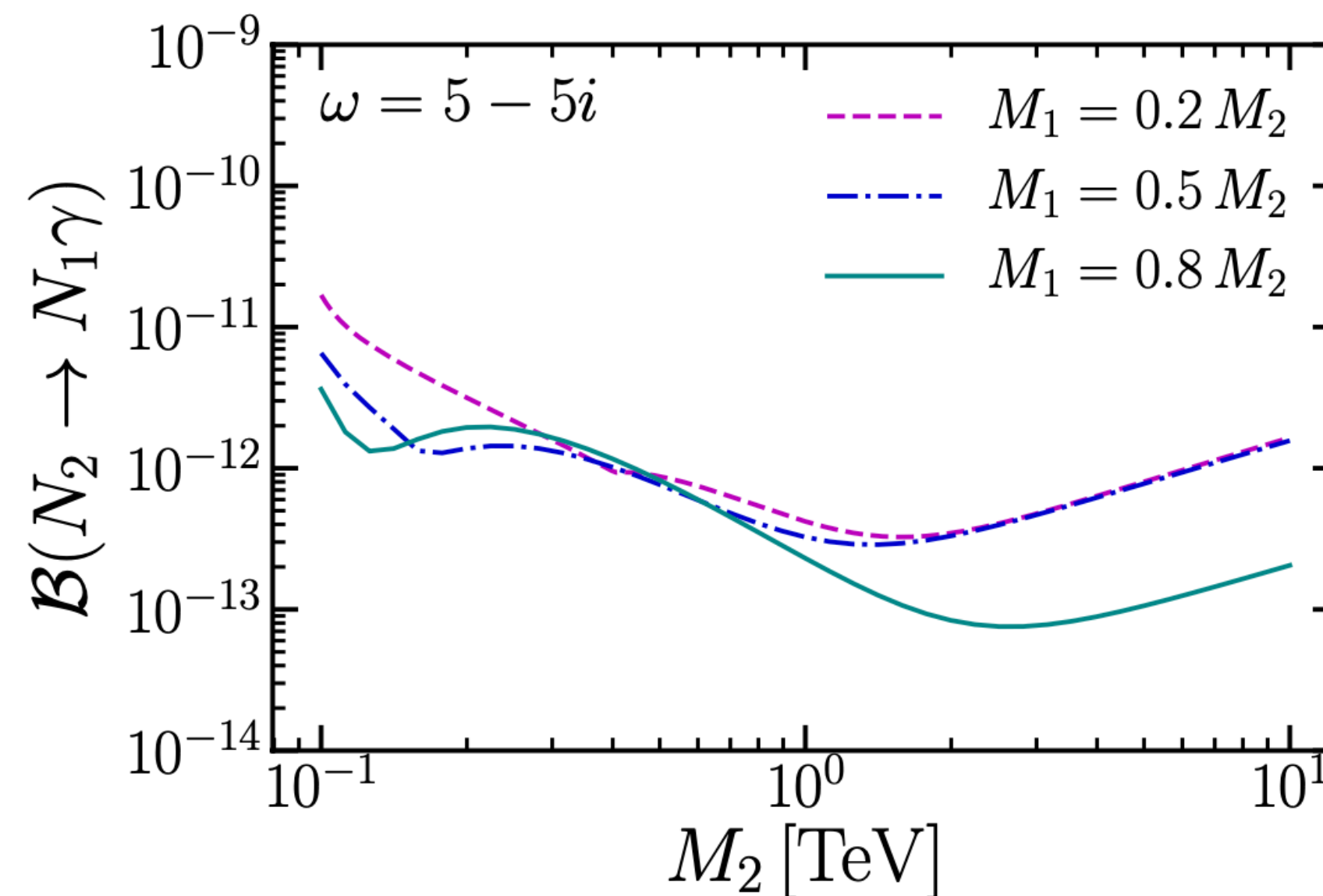
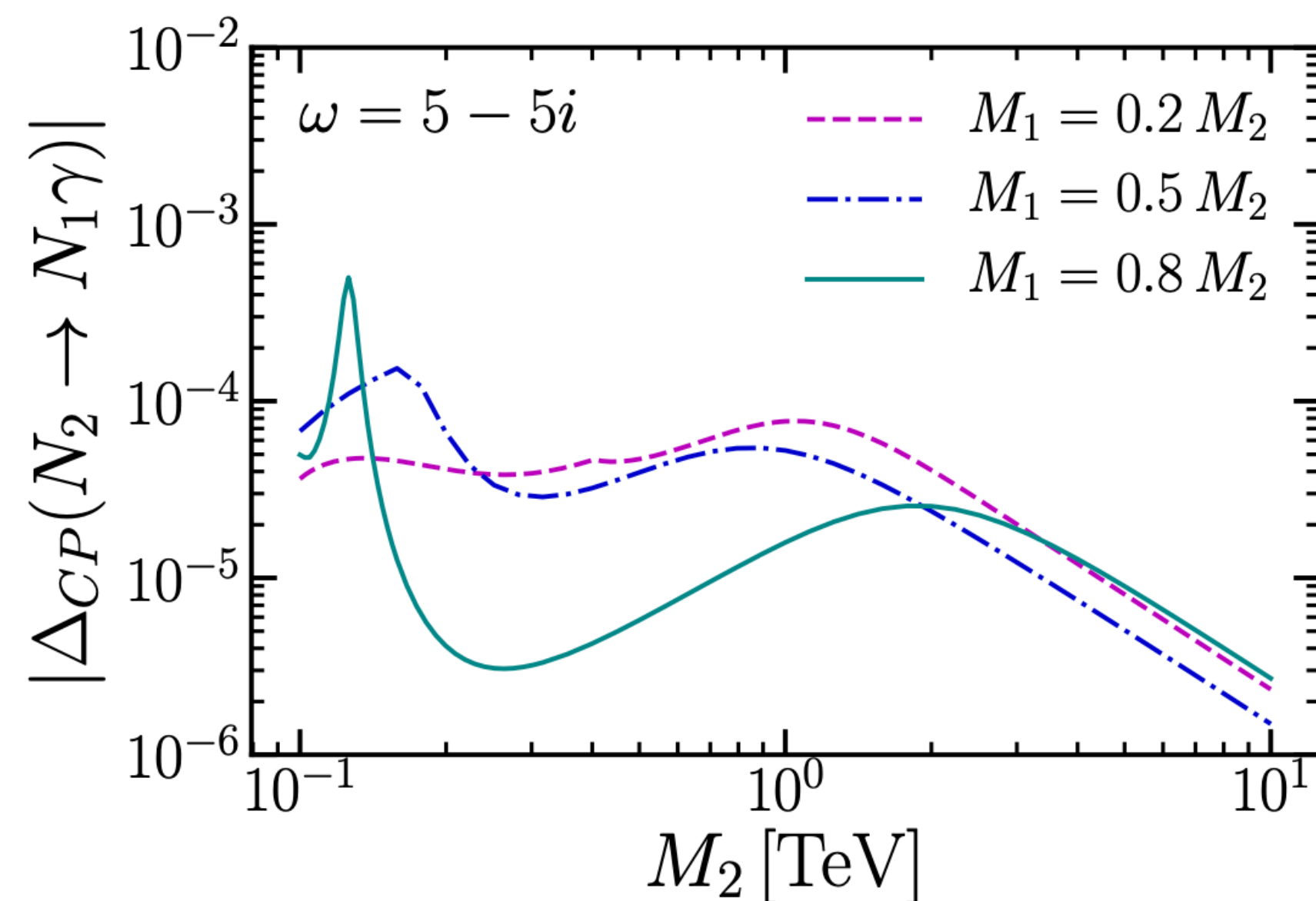
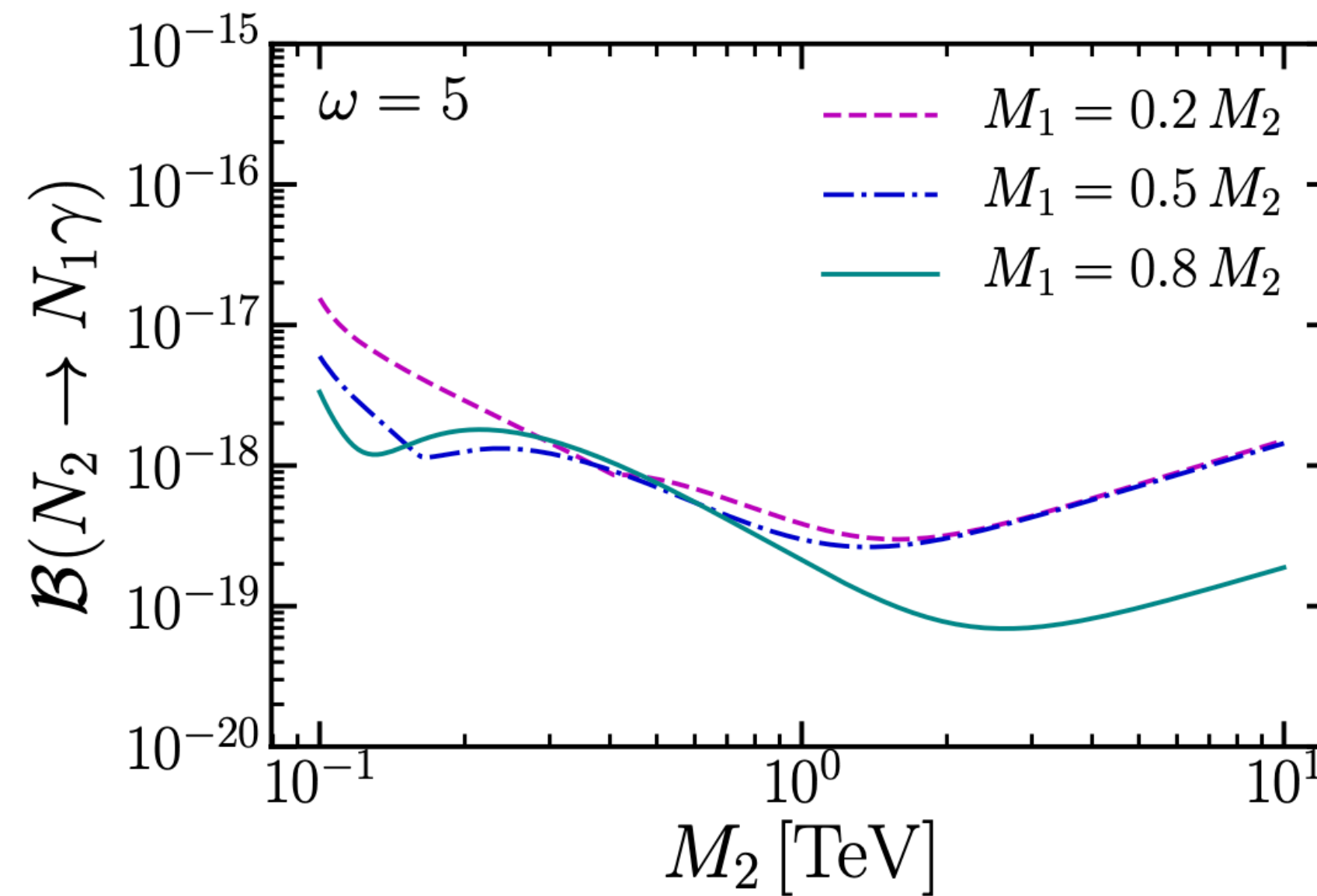
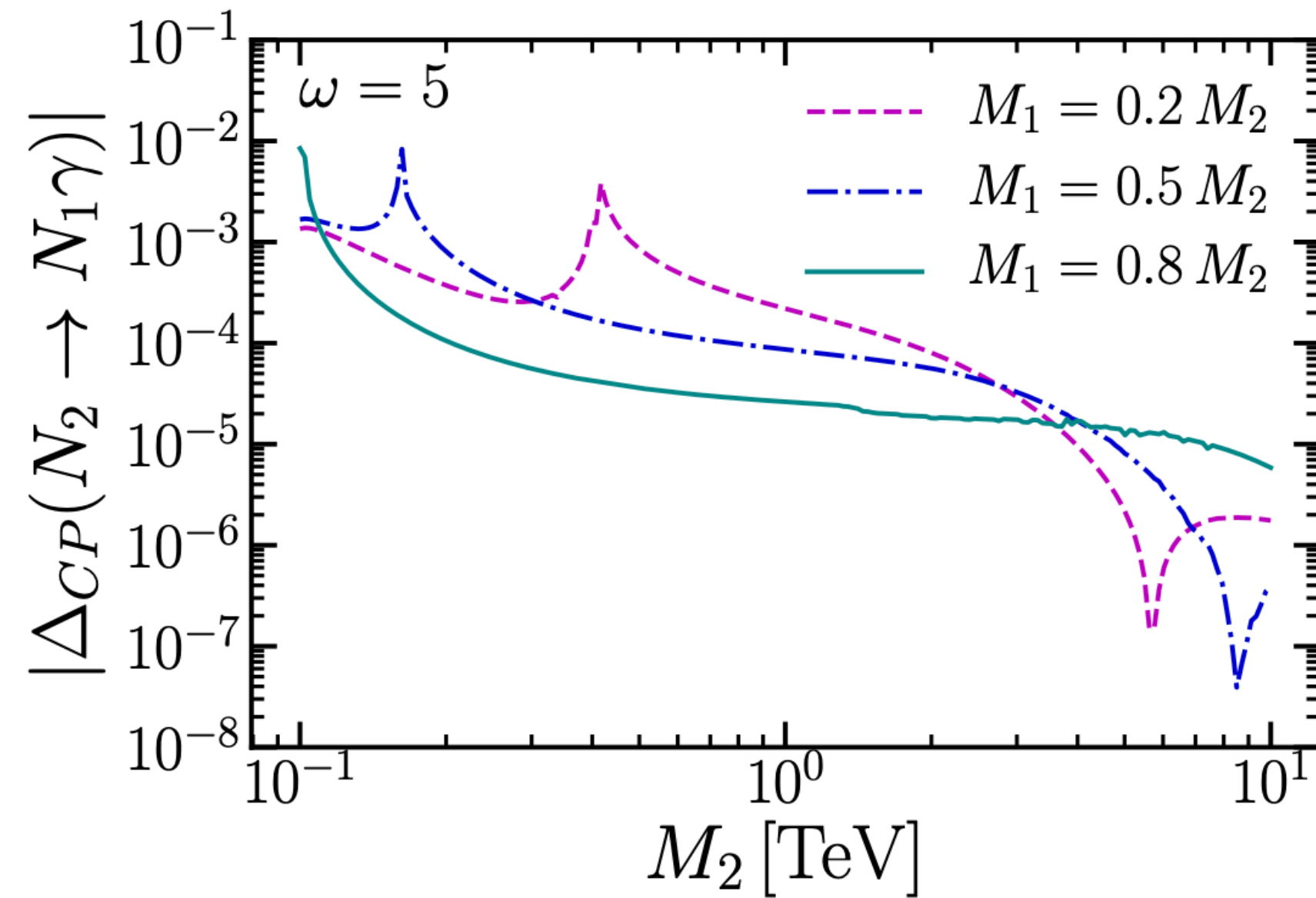
- $N_2 \rightarrow N_1 + \gamma$

$$\Delta_{CP}(N_2 \rightarrow N_1\gamma) = \frac{\sum_{\alpha,\beta} \mathcal{J}_{\alpha\beta}^{54} \left[\text{Im}(\mathcal{F}_{45,\alpha} \mathcal{F}_{45,\beta}^*) M_2^2 - \text{Im}(\mathcal{F}_{54,\alpha} \mathcal{F}_{54,\beta}^*) M_1^2 \right] - 2\mathcal{V}_{\alpha\beta}^{54} \text{Im}(\mathcal{F}_{45,\alpha} \mathcal{F}_{54,\beta}^*) M_2 M_1}{\sum_{\alpha,\beta} \mathcal{R}_{\alpha\beta}^{54} \left[\text{Re}(\mathcal{F}_{45,\alpha} \mathcal{F}_{45,\beta}^*) M_2^2 + \text{Re}(\mathcal{F}_{54,\alpha} \mathcal{F}_{54,\beta}^*) M_1^2 \right] - 2\mathcal{C}_{\alpha\beta}^{54} \text{Re}(\mathcal{F}_{45,\alpha} \mathcal{F}_{54,\beta}^*) M_2 M_1}.$$

This channel may lead to large CP violation.

Benchmark plot of CP asymmetries

Balaji, Ramirez-Quezada,
YLZ, 2008.12795



Oscillation parameters all fixed at their best-fit values, and $2\sigma = 180^\circ$ assumed

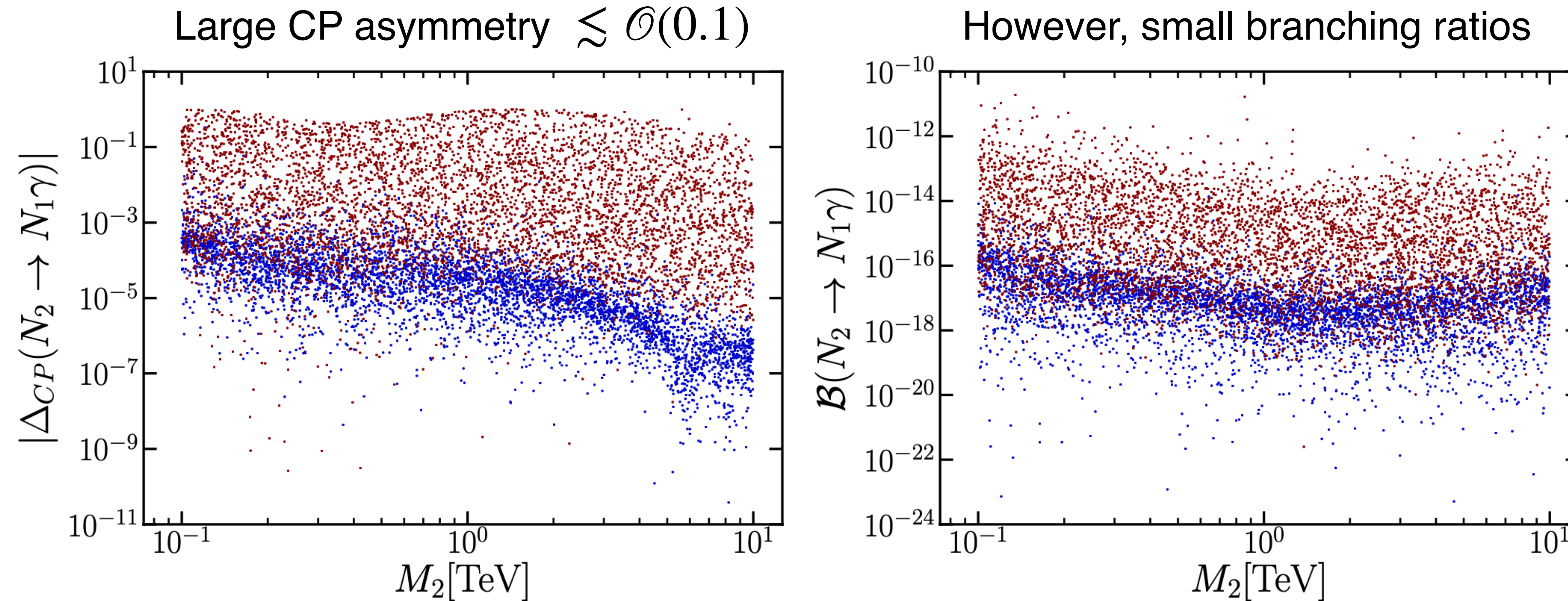
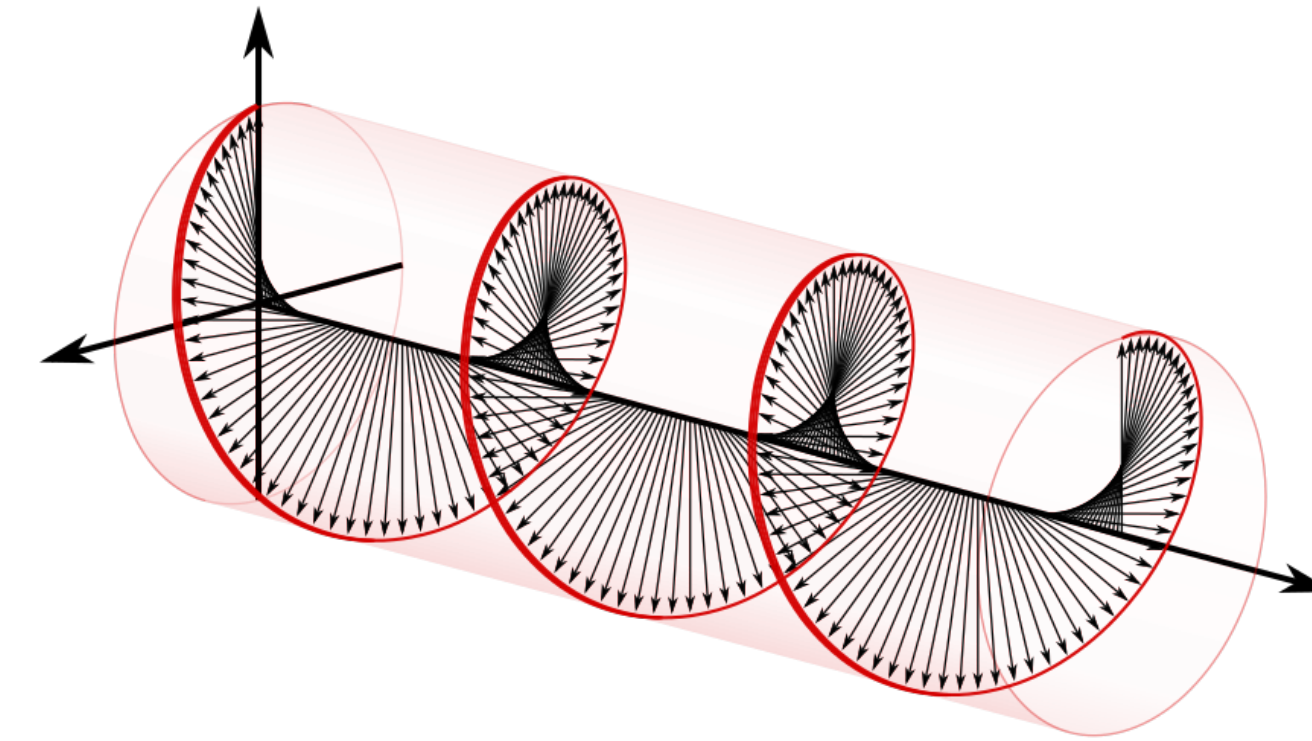


Figure 3: The CP asymmetry parameter Δ_{CP} (left) and branching ratio (right) scanned in the region M_2 in $[0.1, 10]$ TeV and the ratio M_1/M_2 in $[0.1, 1)$, where both masses are scanned in the logarithmic scale. The red region refers to $\omega = [0, 2\pi] + i[-5, 5]$ while the blue region is the smaller $\omega = [0, 2\pi]$. All oscillation parameters are scanned in the 3σ ranges, $\omega = [0, 2\pi]$ and $\zeta = +1$ are used. The scan performed for the $\zeta = -1$ branch gives the same distribution and is thus omitted.

- In a flux of photon, a net circular polarisation represents the number density asymmetry between left- and right-circularly-polarised photons. It is characterised by the Stokes parameter

$$V = |\vec{\epsilon}_+ \cdot \vec{E}| - |\vec{\epsilon}_- \cdot \vec{E}|$$



- Astrophysical sources

Faraday conversion, Bi-refringence, Synchrotron emission, ...

- Astroparticle sources: P and CP violation must be required

Boehm, Degrande, Mattelaer, Vincent, 1701.02754

- A net circular polarisation can be obtained CPV radiative decay of keV neutrino dark matter

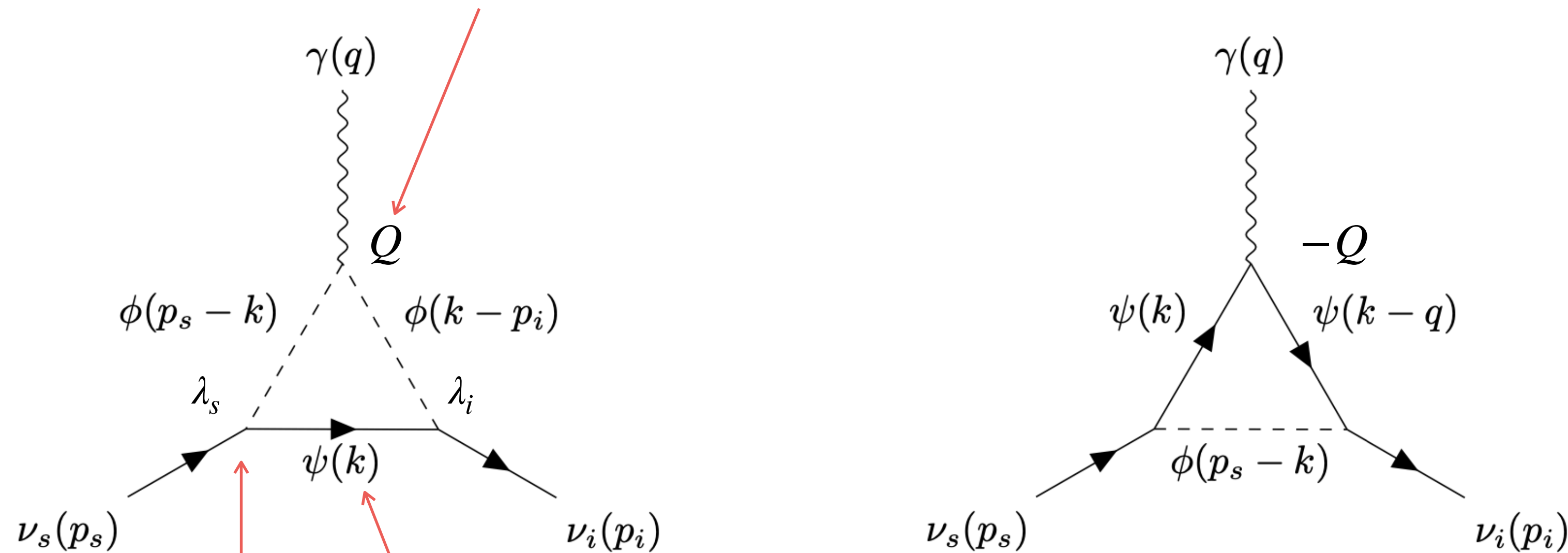
$$V \sim \Delta_{CP,+}^D - \Delta_{CP,+}^D \quad \text{for Dirac DM}$$

$$V \sim \Delta_{CP}^M \quad \text{for Majorana DM}$$

- A toy model:

keV neutrino $\nu_s \Rightarrow$ DM
 + a pair of opposite millicharged particles ϕ & ψ

small millicharge $Q < 10^{-4}e$ to avoid QED precision measurement

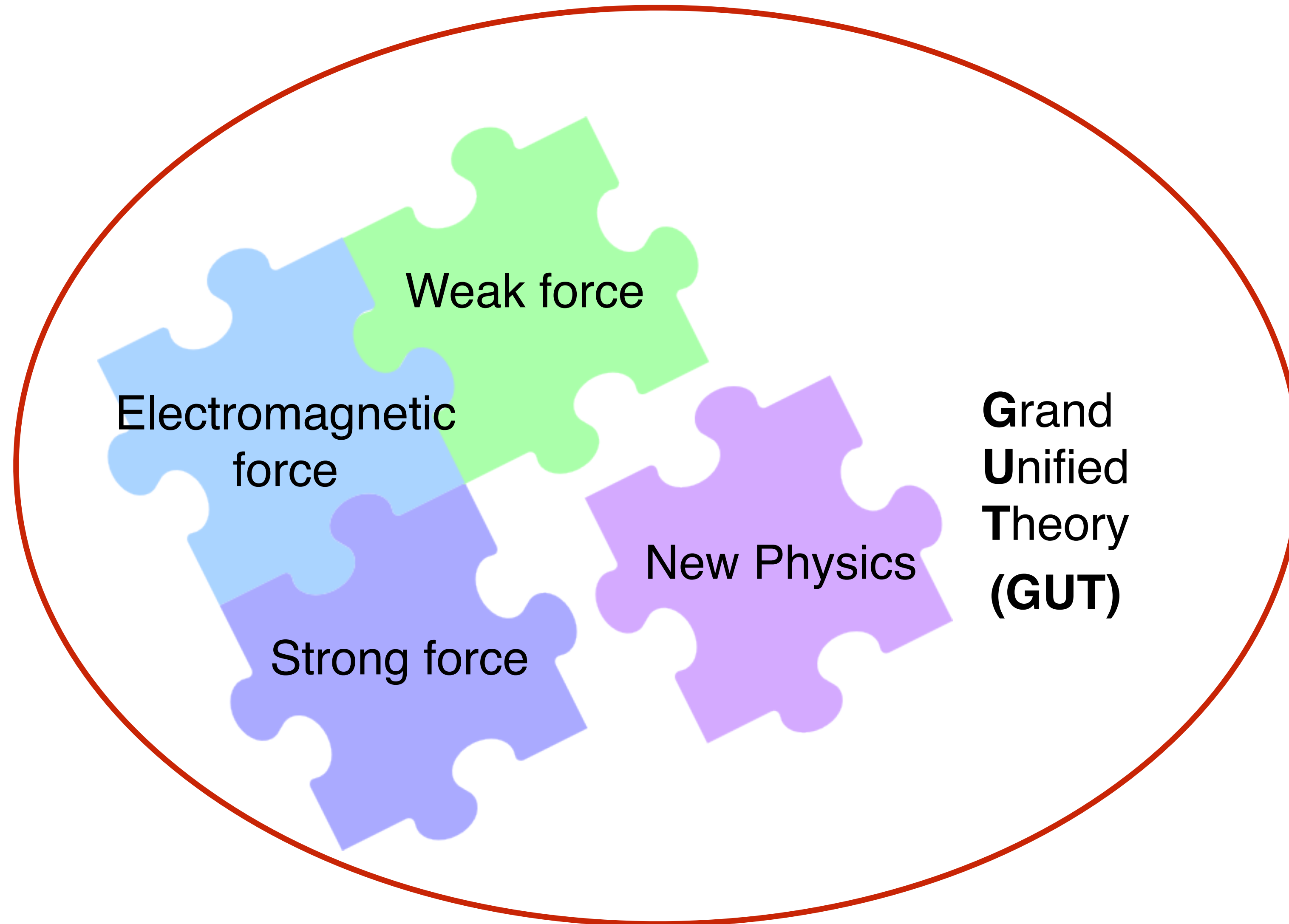


$m_\phi + m_\psi < m_s$ to generate imaginary part of loop integration

tiny λ_s to forbid fast decay of DM, and $\text{Im}(\lambda_i(U^\dagger U)_{is}\lambda_s^*) \neq 0$ for CPV

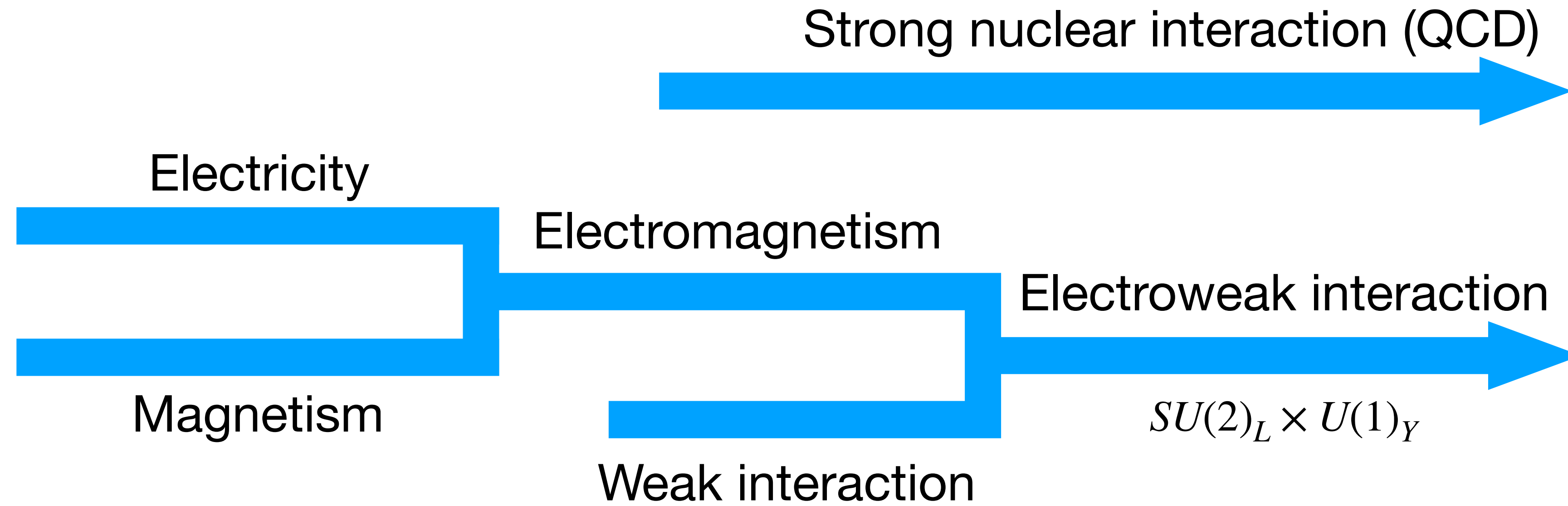
$\Rightarrow V \sim \Delta_{CP}^M \sim 10^{-5}$ still far away from being detectable

Probe GUTs via proton decay



Gravity... not included

A long road of unifications



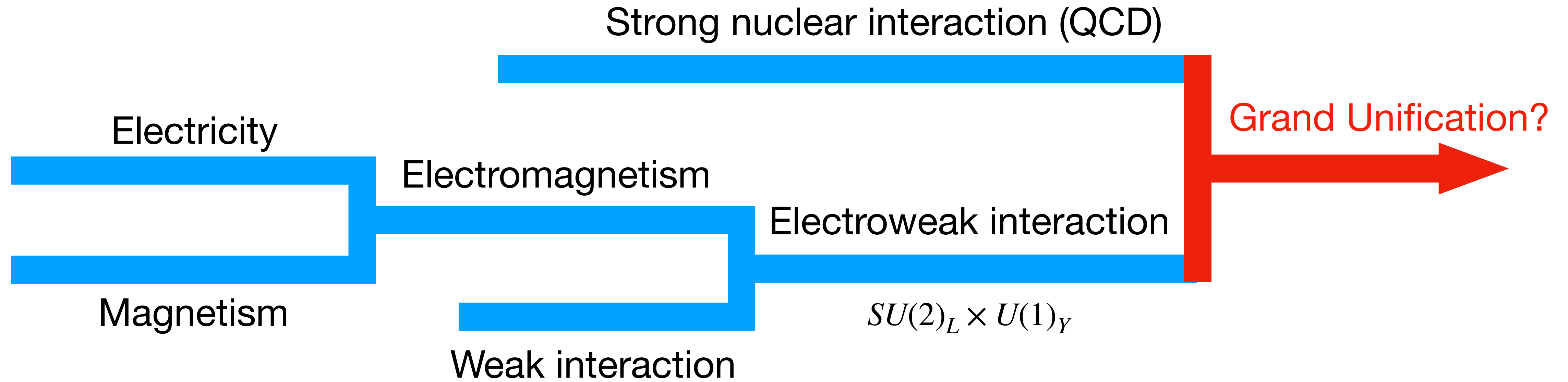
James C. Maxwell

$$\begin{aligned}\nabla \cdot \mathbf{E} &= 4\pi\rho \\ \nabla \cdot \mathbf{B} &= 0 \\ \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{B} &= 4\pi\mathbf{J} + \frac{\partial \mathbf{E}}{\partial t}\end{aligned}$$



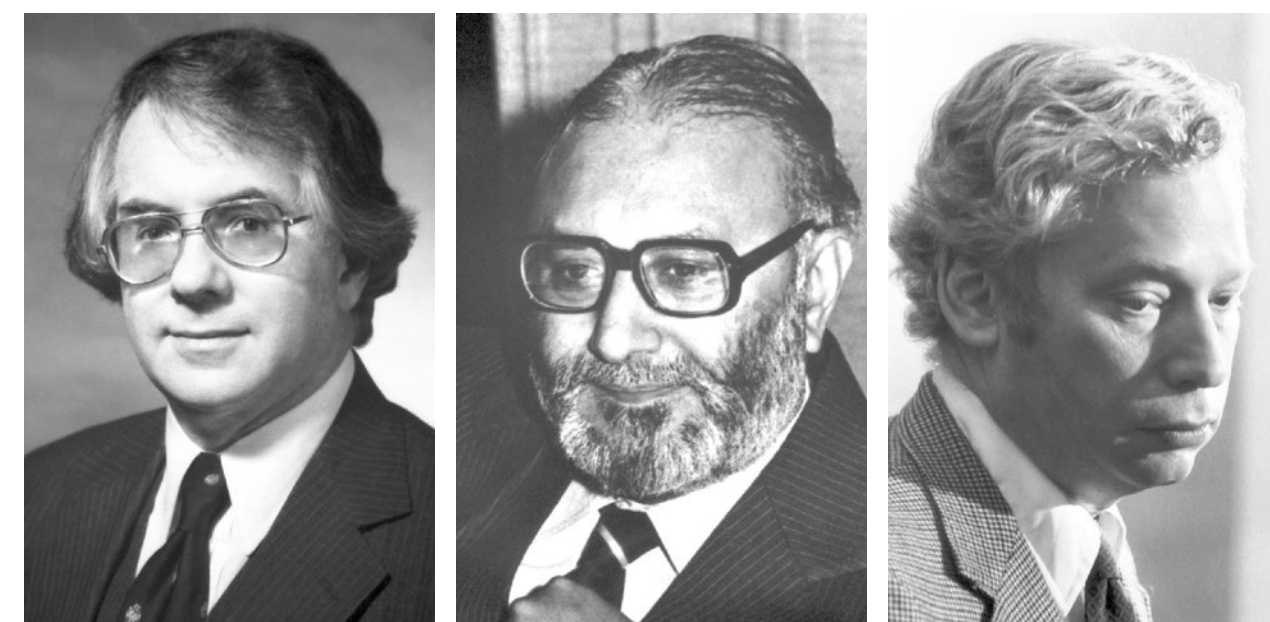
Glashow, Salam, Weinberg

A long road of unifications



$$\begin{aligned}\nabla \cdot \mathbf{E} &= 4\pi\rho \\ \nabla \cdot \mathbf{B} &= 0 \\ \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{B} &= 4\pi\mathbf{J} + \frac{\partial \mathbf{E}}{\partial t}\end{aligned}$$

James C. Maxwell



Glashow, Salam, Weinberg

Roads to GUTs

- Unification of symmetries

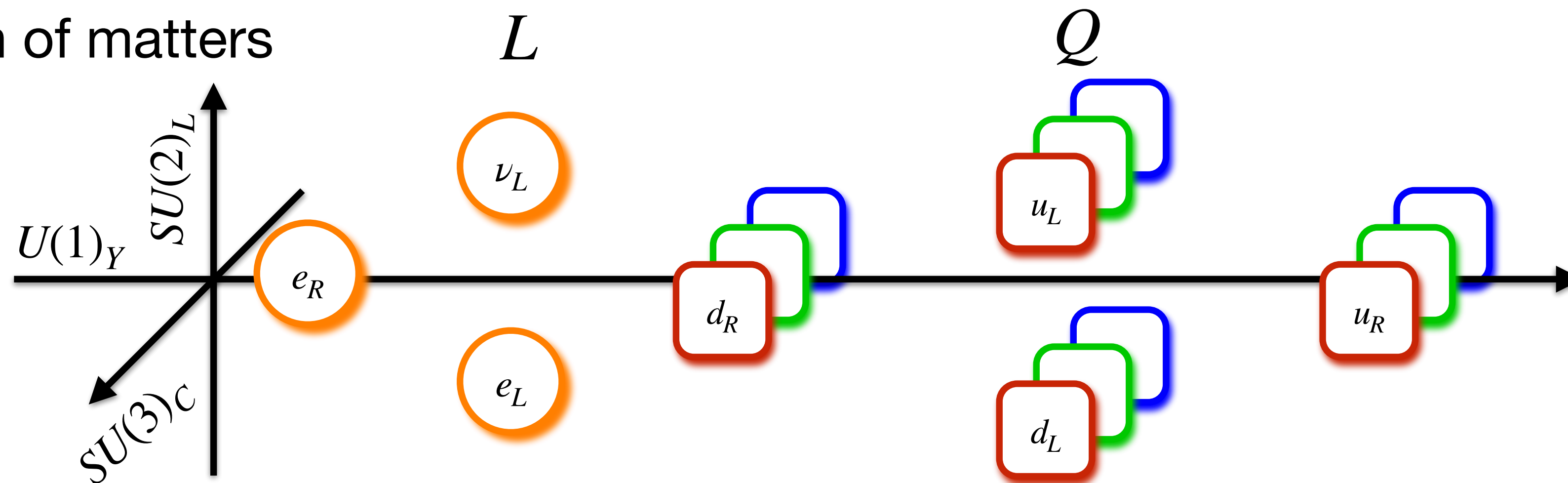
$$G_{\text{GUT}} \supset G_{\text{SM}} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

- Unification of couplings

$$\begin{array}{c}
 \downarrow \qquad \qquad \downarrow \quad \text{EW} \quad \downarrow \\
 g_3 \quad = \quad g_2 \quad = \quad g_1 \quad \text{up to a loop} \\
 \qquad \qquad \qquad \qquad \qquad \qquad \text{correction factor}
 \end{array}$$

The scale where three gauge couplings are unified, denoted as M_{GUT} in this talk

- Unification of matters

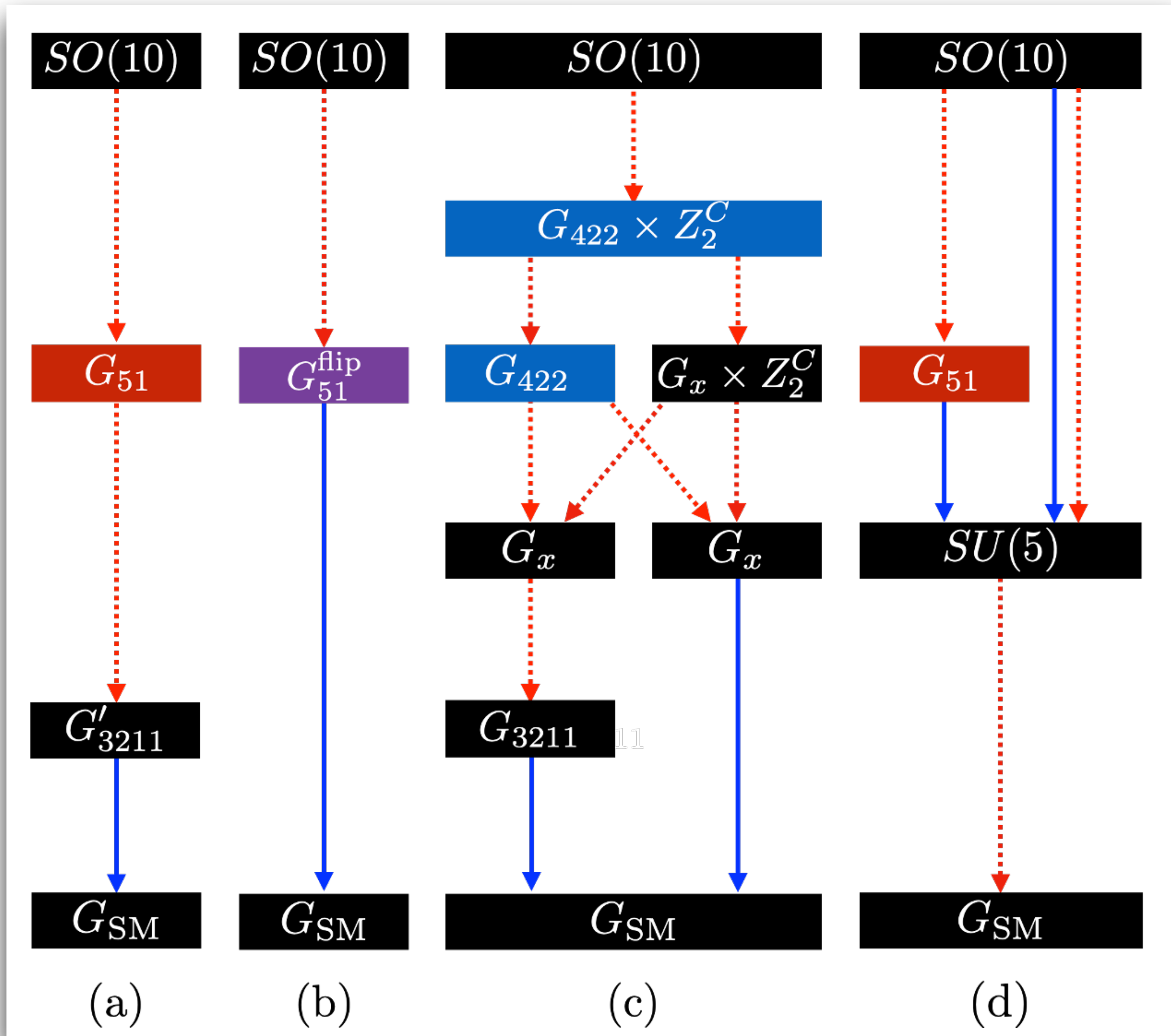


Weak hypercharge: $Y = -1$ $Y = -\frac{1}{2}$ $Y = -\frac{1}{3}$ $Y = \frac{1}{6}$ $Y = \frac{2}{3}$

Roads to GUTs

- Georgi-Glashow (1974) $SU(5)$ Quarks & leptons $\sim \bar{\mathbf{5}} + \mathbf{10}$
- More realistic $SU(5)$ e.g., including new particles to generate neutrino masses
- $SU(5) \times U(1)_{B-L}$ $\bar{\mathbf{5}} + \mathbf{10} + \mathbf{1}, \nu_R \sim \mathbf{1}$
- Flipped $SU(5) \times U(1)_X$ Rujula, Georgi, Glashow (1980); Barr,(1982); Derendinger, Kim, Nanopoulos (1984); Antoniadis, Ellis, Hagelin, Nanopoulos (1989)
 $u \leftrightarrow d, \nu \leftrightarrow e$
- Pati-Salam (1973), $SU(4)_c \times SU(2)_L \times SU(2)_R = G_{422}$
 $(\mathbf{4}, \mathbf{2}, \mathbf{1}) : \psi_L = \begin{pmatrix} u^1 & u^2 & u^3 & \nu \\ d^1 & d^2 & d^3 & e \end{pmatrix}_L, (\bar{\mathbf{4}}, \mathbf{1}, \mathbf{2}) : \psi_R = \begin{pmatrix} u^1 & u^2 & u^3 & \nu \\ d^1 & d^2 & d^3 & e \end{pmatrix}_R^c$
- $SO(10)$ GUTs $\mathbf{16} = \bar{\mathbf{5}} + \mathbf{10} + \mathbf{1} = (\mathbf{4}, \mathbf{2}, \mathbf{1}) + (\bar{\mathbf{4}}, \mathbf{1}, \mathbf{2})$
 Fritzsche, Minkowski (1975) $SO(10) \quad SU(5) \quad SU(4)_c \times SU(2)_L \times SU(2)_R$

1st entity: groups & representations



SO(10) breaking chain

$$G_{422} = SU(4)_C \times SU(2)_L \times SU(2)_R$$

$$G_{51} = SU(5) \times U(1)_X$$

$$G_{51}^{flip} = SU(5)_{flip} \times U(1)_{flip}$$

$$Z_2^C: \psi_L \leftrightarrow \psi_R^c$$

$$G_x = G_{421} \text{ or } G_{3221}$$

$$G_{3221} = SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

$$G_{421} = SU(4)_C \times SU(2)_L \times U(1)_Y$$

$$G_{3211} = SU(3)_C \times SU(2)_L \times U(1)_R \times U(1)_{B-L}$$

$$G'_{3211} = SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_X$$

$$G_{SM} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

Unwanted topological defects:
monopoles and domain walls

In any breaking chains, inflation has to be introduced to inflate unwanted defects

$$G_{422} = SU(4)_C \times SU(2)_L \times SU(2)_R$$

$$G_{51} = SU(5) \times U(1)_X$$

$$G_{51}^{\text{flip}} = SU(5)_{\text{flip}} \times U(1)_{\text{flip}}$$

$$Z_2^C: \psi_L \leftrightarrow \psi_R^c$$

$$G_x = G_{421} \text{ or } G_{3221}$$

$$G_{3221} = SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

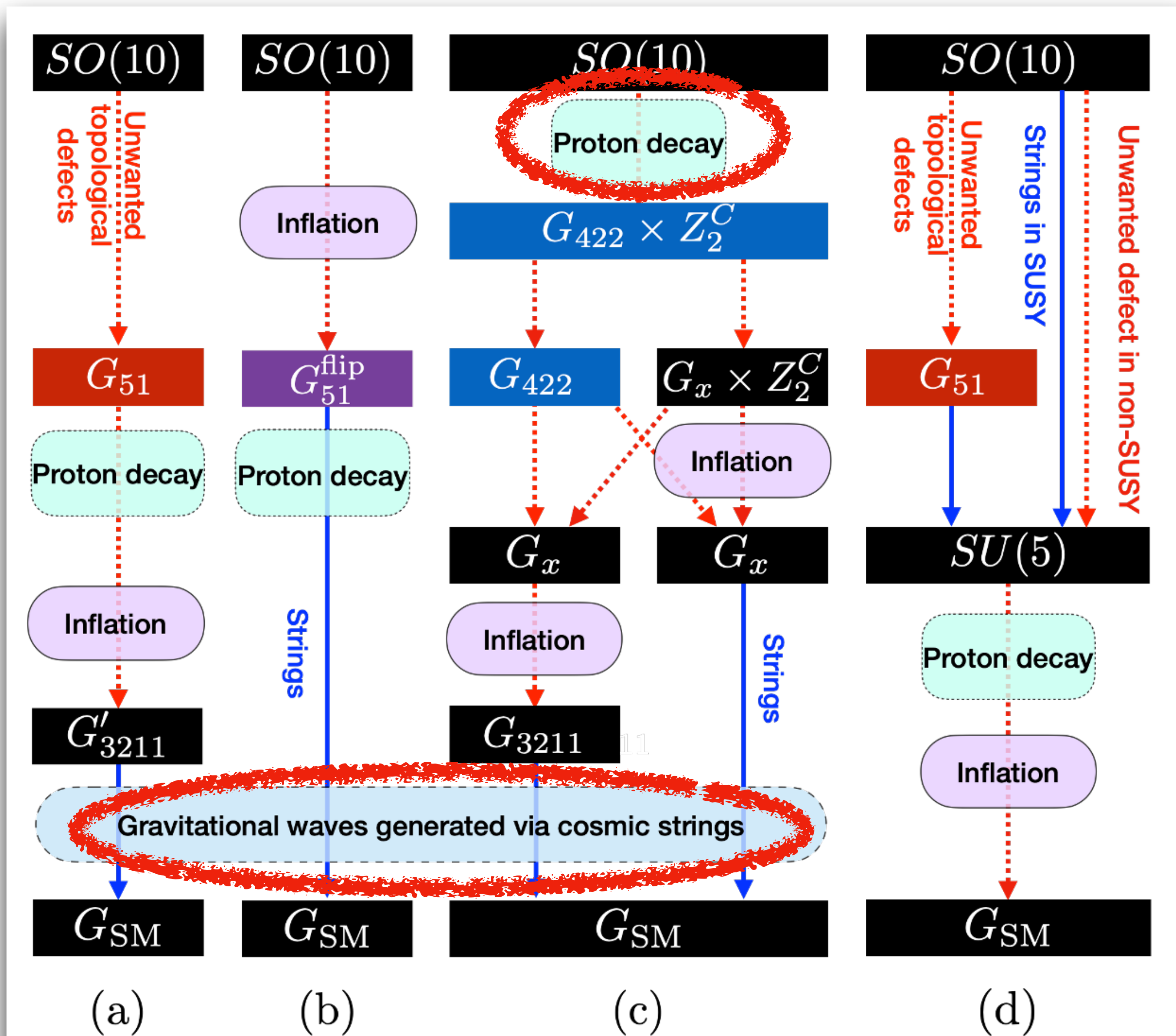
$$G_{421} = SU(4)_C \times SU(2)_L \times U(1)_Y$$

$$G_{3211} = SU(3)_C \times SU(2)_L \times U(1)_R \times U(1)_{B-L}$$

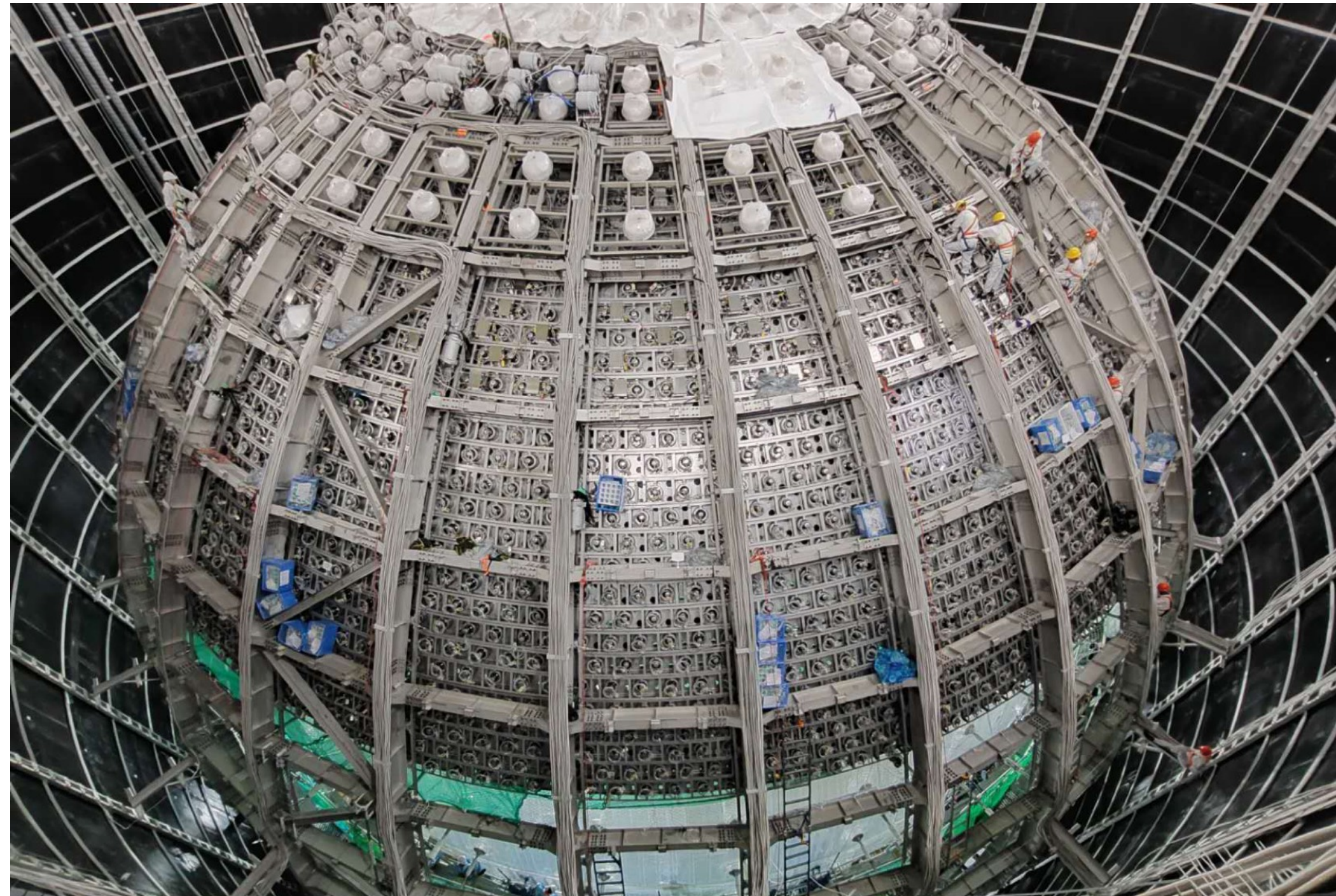
$$G'_{3211} = SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_X$$

$$G_{\text{SM}} = SU(3)_C \times SU(2)_L \times U(1)_Y$$

King, Pascoli, Turner, **YLZ**, 2005.13549

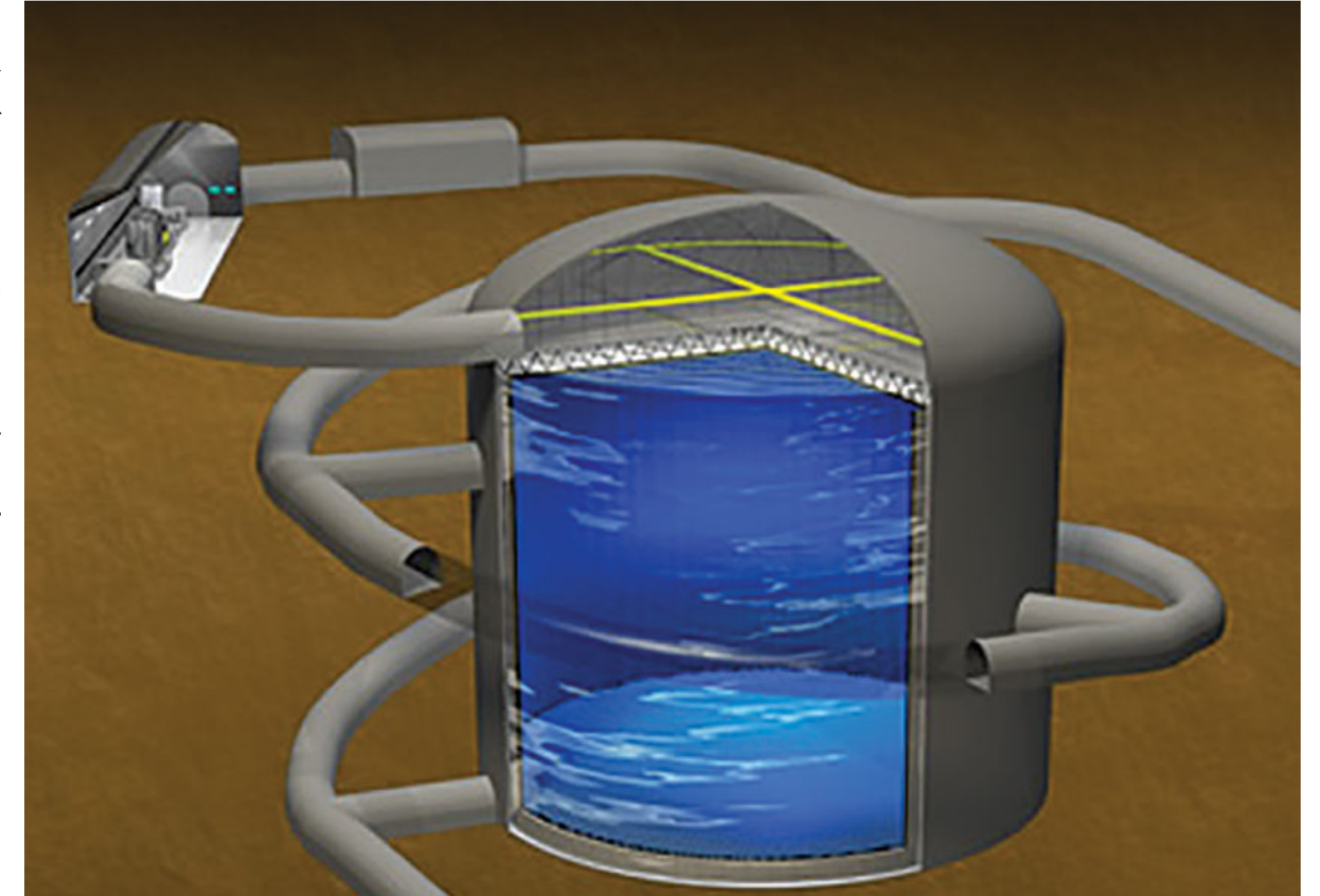


Upcoming large-scale neutrino experiments



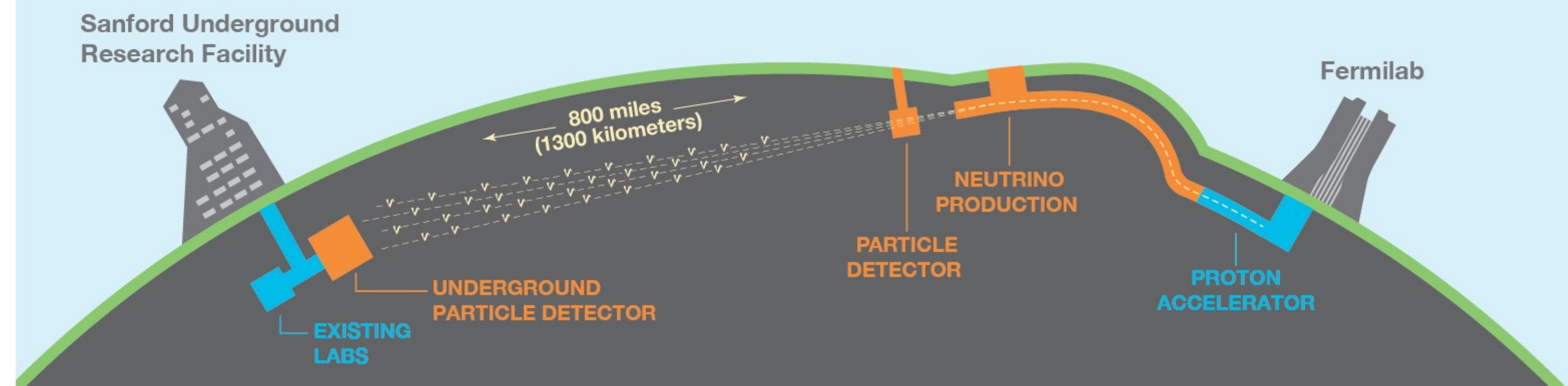
Hyper-K
expected to
run in 2027

188 kt FV
 $\sim 6 \times 10^{34}$
proton



JUNO, run next year
20kt FV $\sim 7 \times 10^{33}$ proton

DUNE, run in 2030?



Binding between GUTs and neutrino experiments

KamiokaNDE [edit]

https://en.wikipedia.org/wiki/Kamioka_Observatory#KamiokaNDE

The first of the Kamioka experiments was named KamiokaNDE for **Kamioka Nucleon Decay Experiment**. It was a large water Čerenkov detector designed to search for proton decay. To observe the decay of a particle with a lifetime as long as a proton an experiment must run for a long time and observe an enormous number of protons. This can be done most cost effectively if the target (the source of the protons) and the detector itself are made of the same material. Water is an ideal candidate because production of Čerenkov background from cosmic ray muons in such a large detector located on the surface of the Earth would be far too large. The muon rate in the KamiokaNDE experiment was about 0.4 events per second, roughly five orders of magnitude smaller than what it would have been if the detector had been located at the surface.^[4]

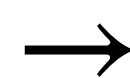
KamiokaNDE for Kamioka Nucleon Decay Experiment.

The distinct pattern produced by Čerenkov radiation allows for particle identification, an important tool both understanding the potential proton decay signal and for rejecting backgrounds. The ID is possible because the sharpness of the edge of the ring depends on the particle producing the radiation. Electrons (and therefore also gamma rays) produce fuzzy rings due to the multiple scattering of the low mass electrons. Minimum ionizing muons, in contrast produce very sharp rings as their heavier mass allows them to propagate directly.

Construction of Kamioka Underground Observatory (the predecessor of the present Kamioka Observatory, Institute for Cosmic Ray Research, University of Tokyo) began in 1982 and was completed in April, 1983. The detector was a cylindrical tank which contained 3,000 tons of pure water and had about 1,000 50 cm diameter photomultiplier tubes (PMTs) attached to the inner surface. The size of the outer detector was 16.0 m in height and 15.6 m in diameter. The detector failed to observe proton decay, but set what was then the world's best limit on the lifetime of the proton.



KamiokaNDE



Kamiokande-II



Super-Kamiokande



...



Masatoshi Koshiba

Observe
neutrino flux
from SN
1987A

Observe
neutrino
oscillation
in 1998

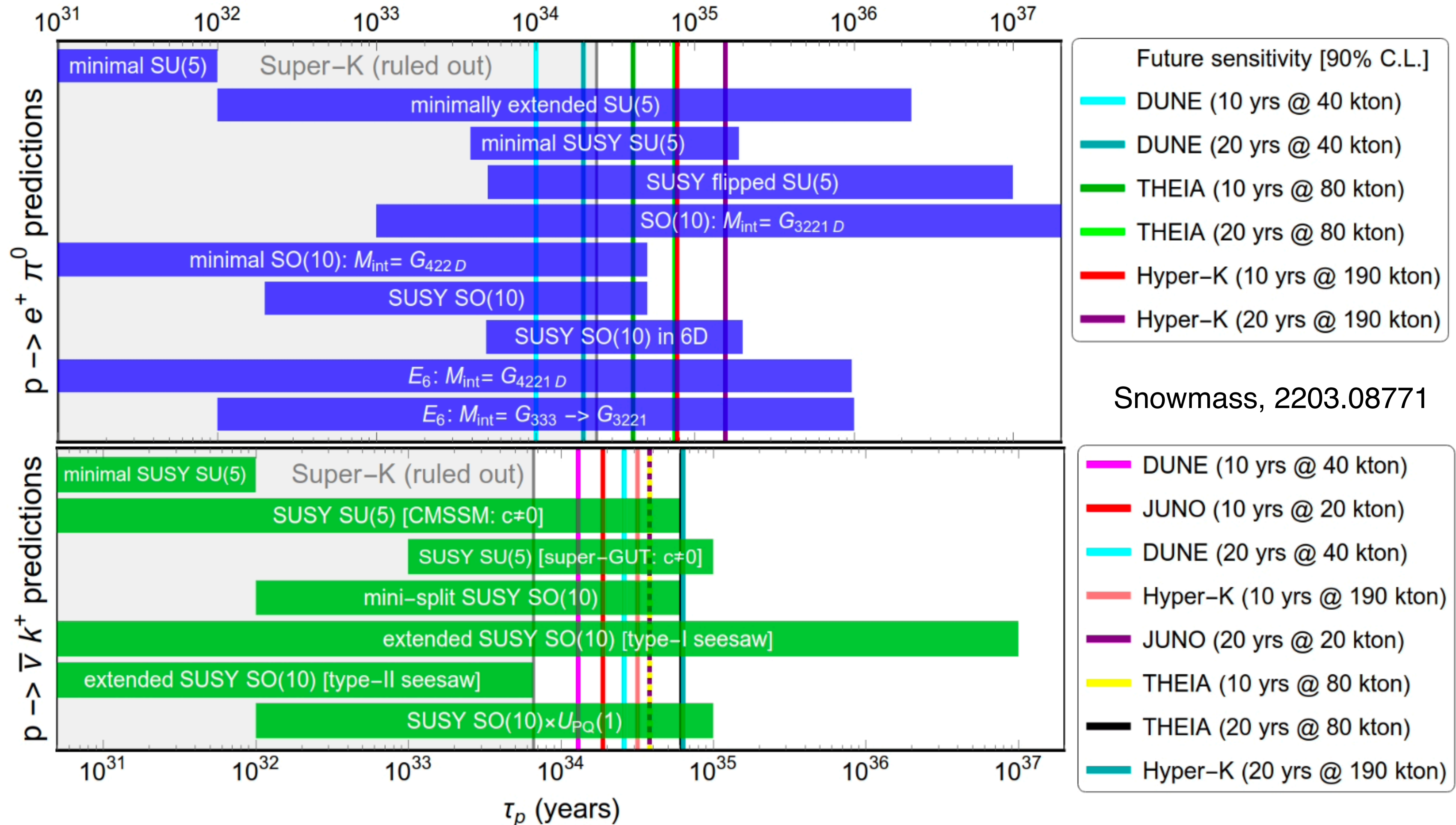


Totsuka Yoji

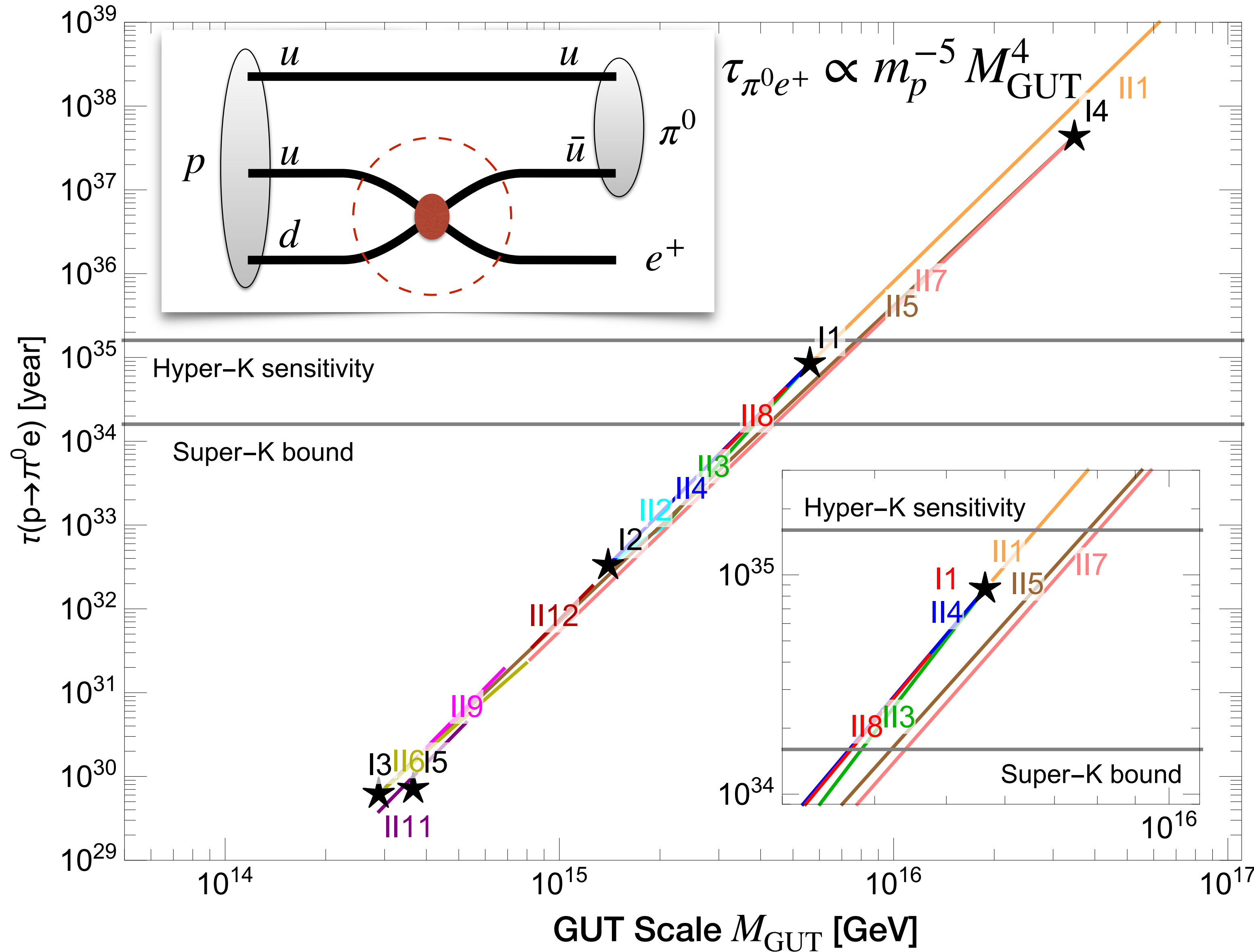


Takaaki Kajita

Proton decay measurements in upcoming neutrino experiments



Proton decay in SO(10) GUTs

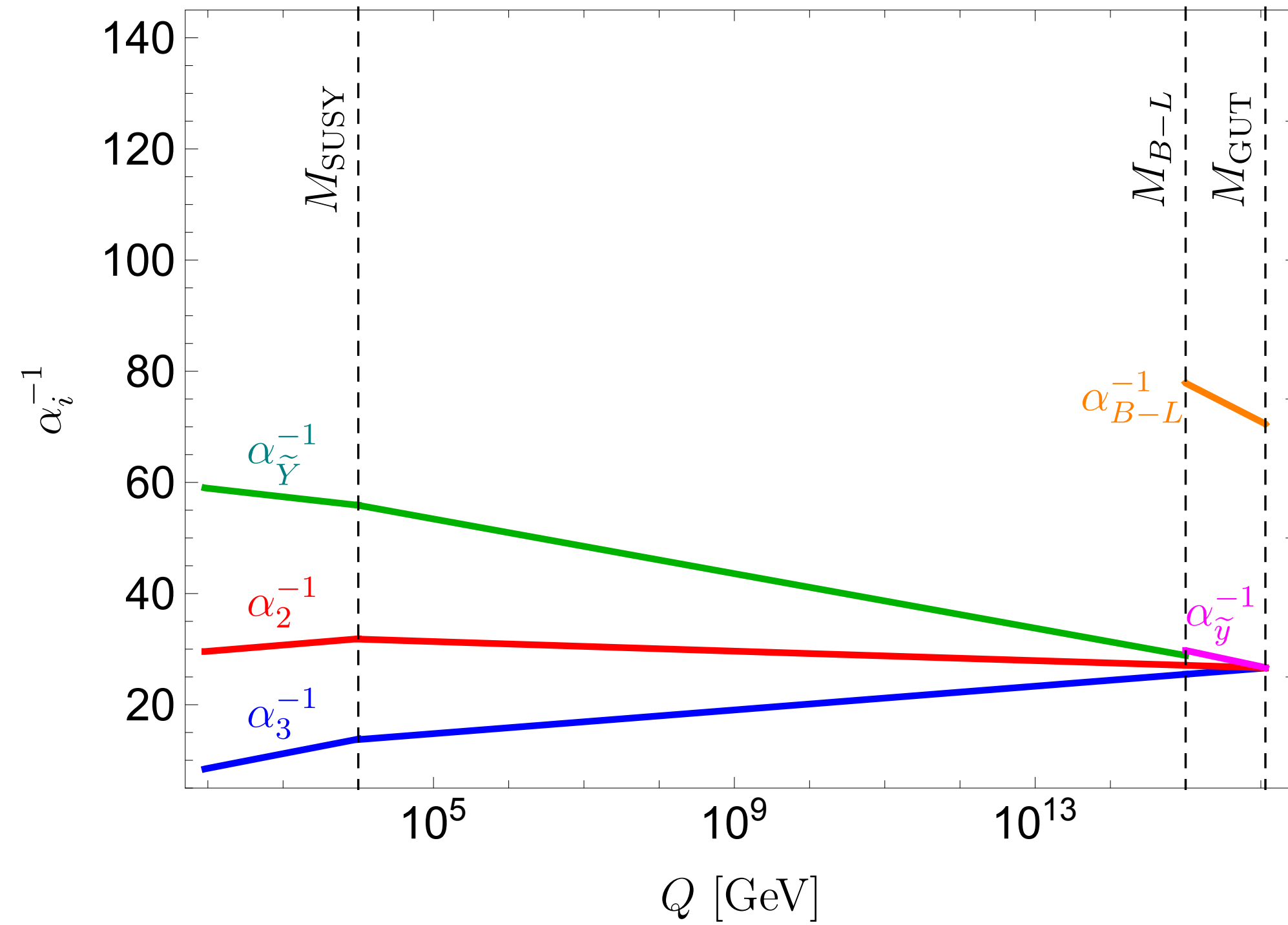


$SO(10)$	$\xrightarrow{\text{defect Higgs}}$	G_2	$\xrightarrow{\text{defect Higgs}}$	G_1	$\xrightarrow{\text{defect Higgs}}$	G_{SM}
II1:	$\frac{m}{210}$	G_{422}	$\frac{m}{45}$	G_{3221}	$\frac{s}{126}$	
II2:	$\frac{m,s}{54}$	G_{422}^C	$\frac{m}{210}$	G_{3221}^C	$\frac{s,w}{126}$	
II3:	$\frac{m,s}{54}$	G_{422}^C	$\frac{m,w}{45}$	G_{3221}	$\frac{s}{126}$	
II4:	$\frac{m,s}{210}$	G_{3221}^C	$\frac{w}{45}$	G_{3221}	$\frac{s}{126}$	
II5:	$\frac{m}{210}$	G_{422}	$\frac{m}{45}$	G_{421}	$\frac{s}{126}$	
II6:	$\frac{m,s}{54}$	G_{422}^C	$\frac{m}{45}$	G_{421}	$\frac{s}{126}$	
II7:	$\frac{m,s}{54}$	G_{422}^C	$\frac{w}{210}$	G_{422}	$\frac{m}{126,45}$	
II8:	$\frac{m}{45}$	G_{3221}	$\frac{m}{45}$	G_{3211}	$\frac{s}{126}$	
II9:	$\frac{m,s}{210}$	G_{3221}^C	$\frac{m,w}{45}$	G_{3211}	$\frac{s}{126}$	
II10:	$\frac{m}{210}$	G_{422}	$\frac{m}{210}$	G_{3211}	$\frac{s}{126}$	
II11:	$\frac{m,s}{54}$	G_{422}^C	$\frac{m,w}{210}$	G_{3211}	$\frac{s}{126}$	
II12:	$\frac{m}{45}$	G_{421}	$\frac{m}{45}$	G_{3211}	$\frac{s}{126}$	

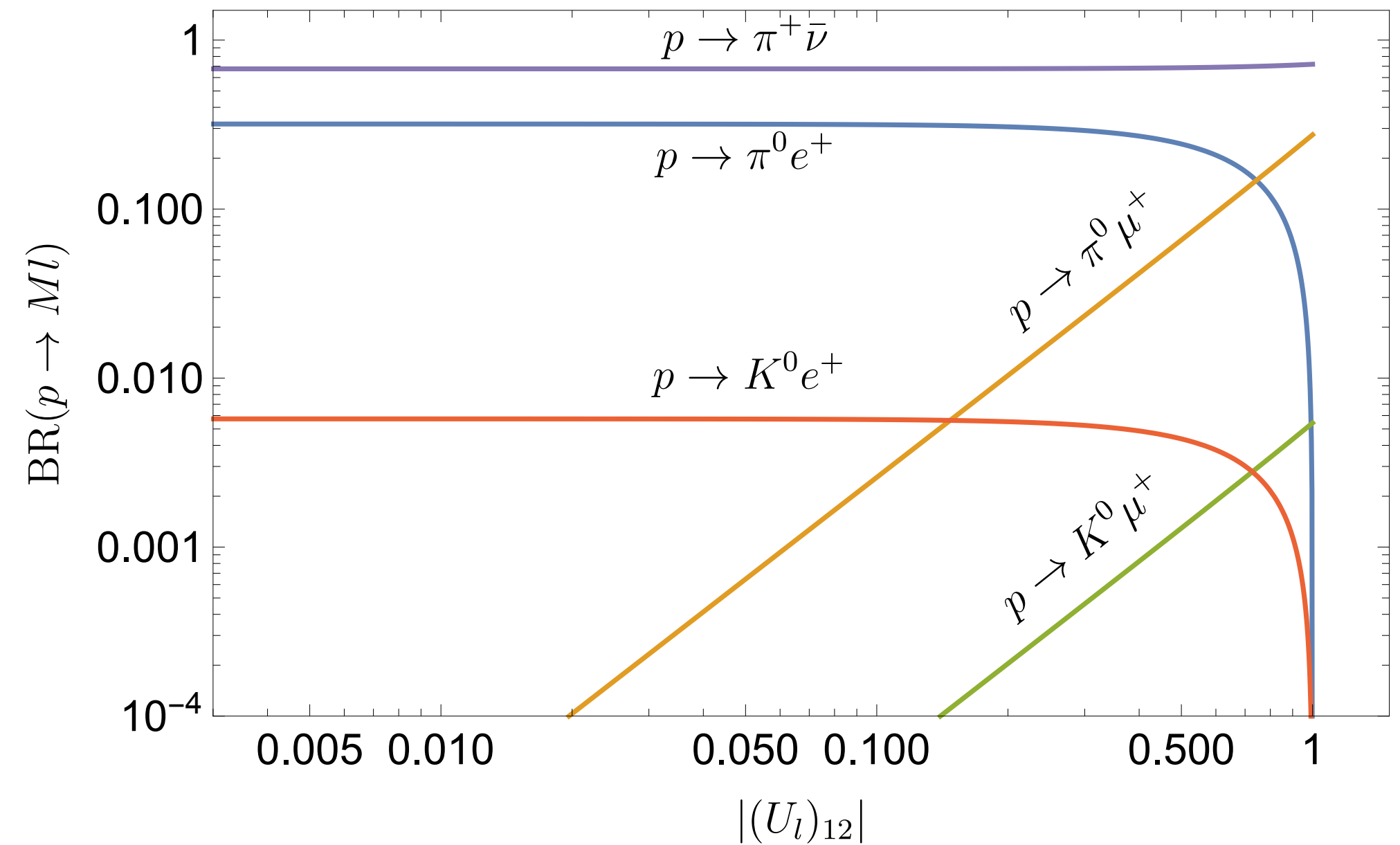
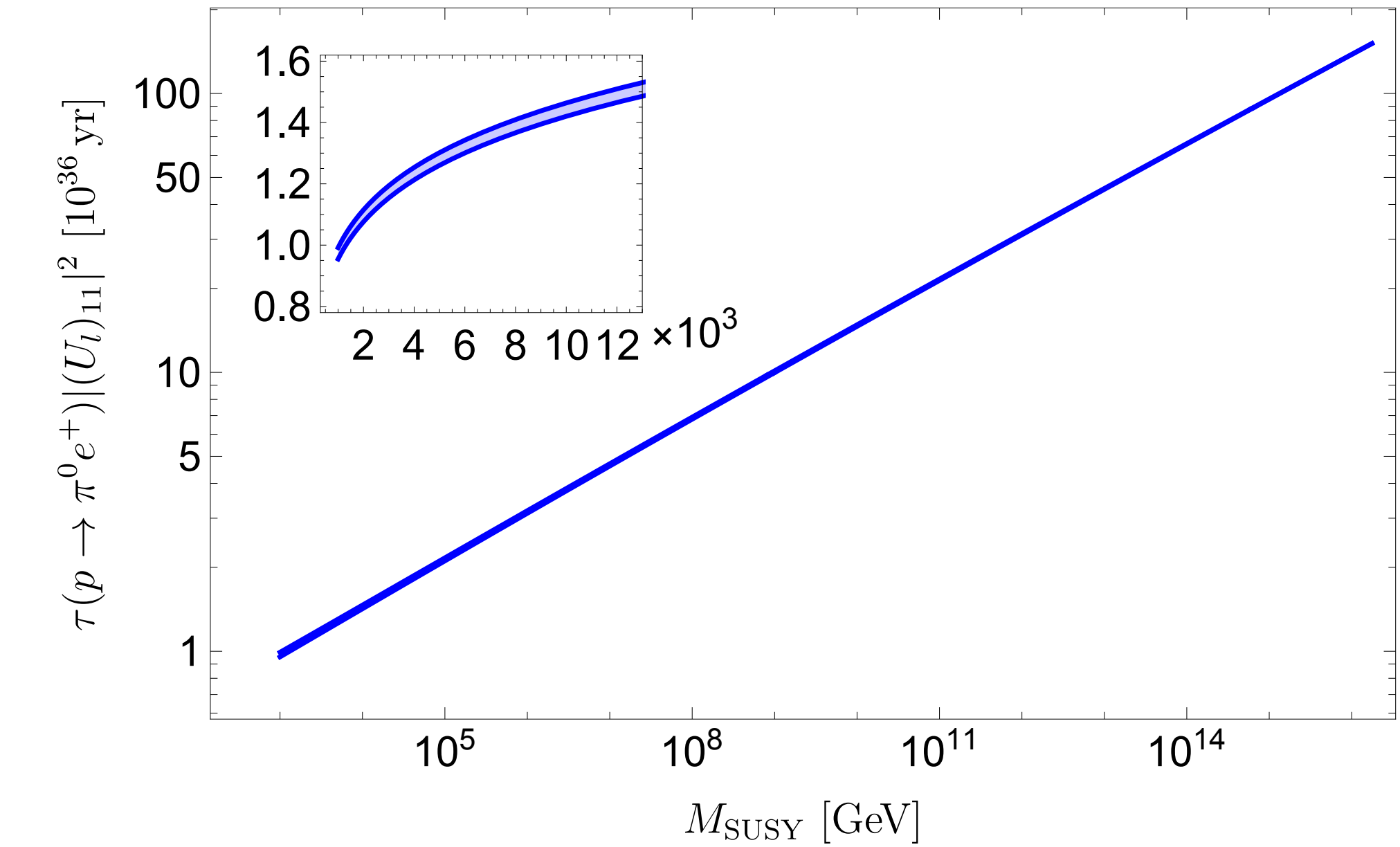
King, Pascoli, Turner, **YLZ**,
2106.15634

Proton decay in flipped SU(5)

$$u \leftrightarrow d, \nu \leftrightarrow e$$

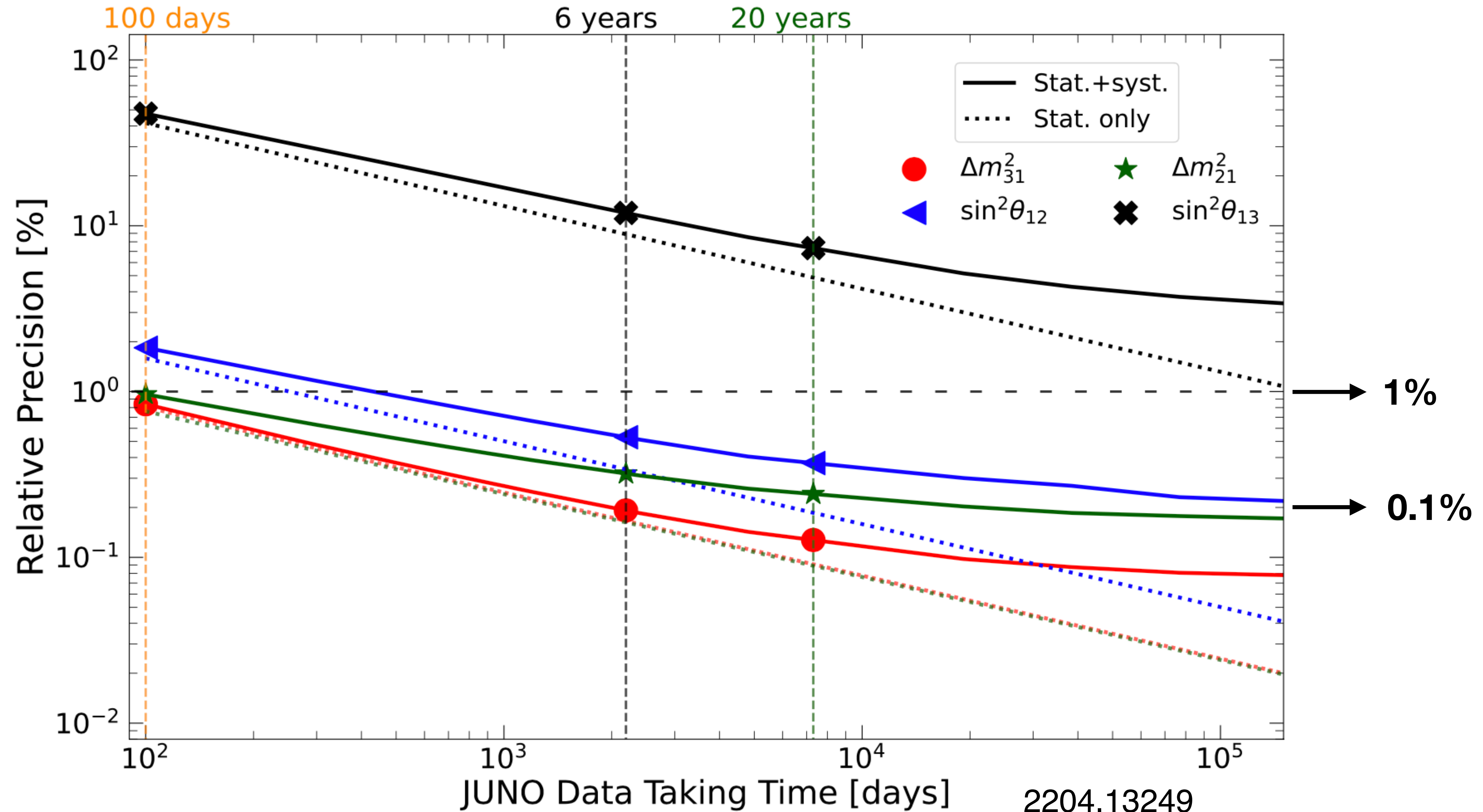


King, Leontaris, **YLZ**,
2311.11857

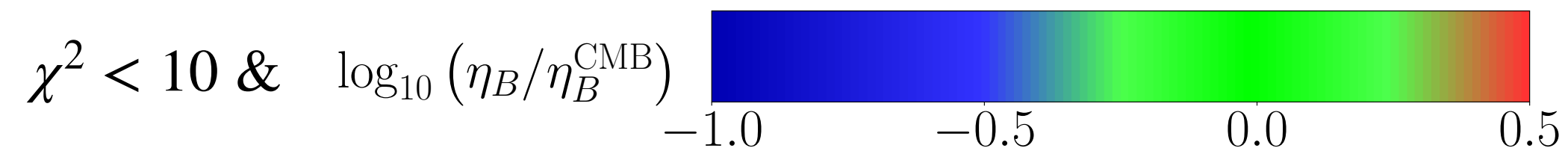
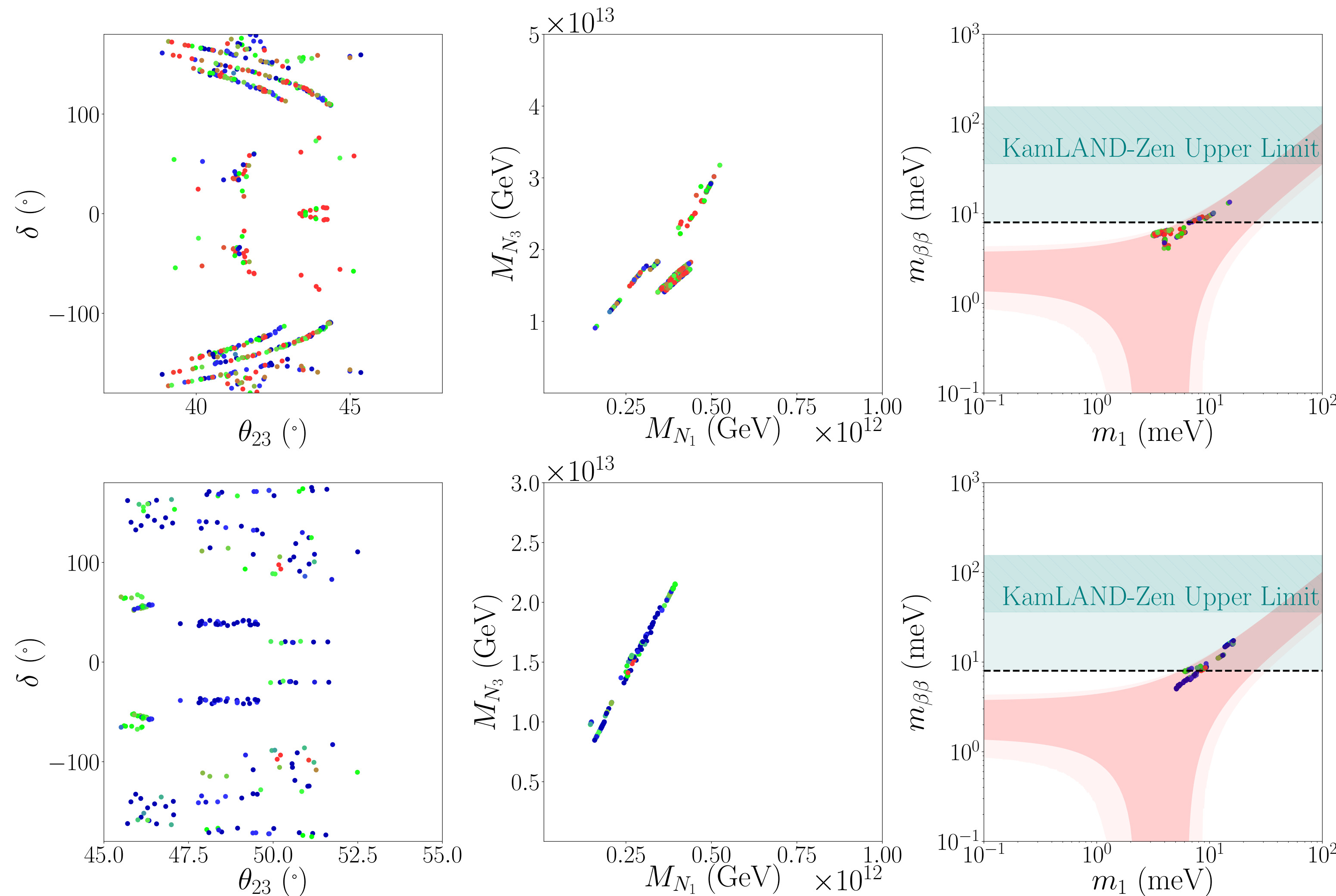


Precision measurements of lepton mixing in upcoming neutrino experiments

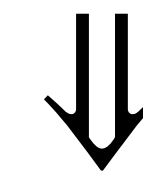
An era of precision measurement of neutrino oscillations!



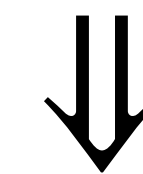
Thermal leptogenesis in SO(10)



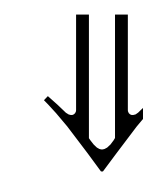
Data of quark masses,
CKM mixing, lepton
masses, PMNS mixing



Heavy neutrino masses
and Dirac ν Yukawa
couplings



CP violation in heavy
neutrino decay



Thermal leptogenesis

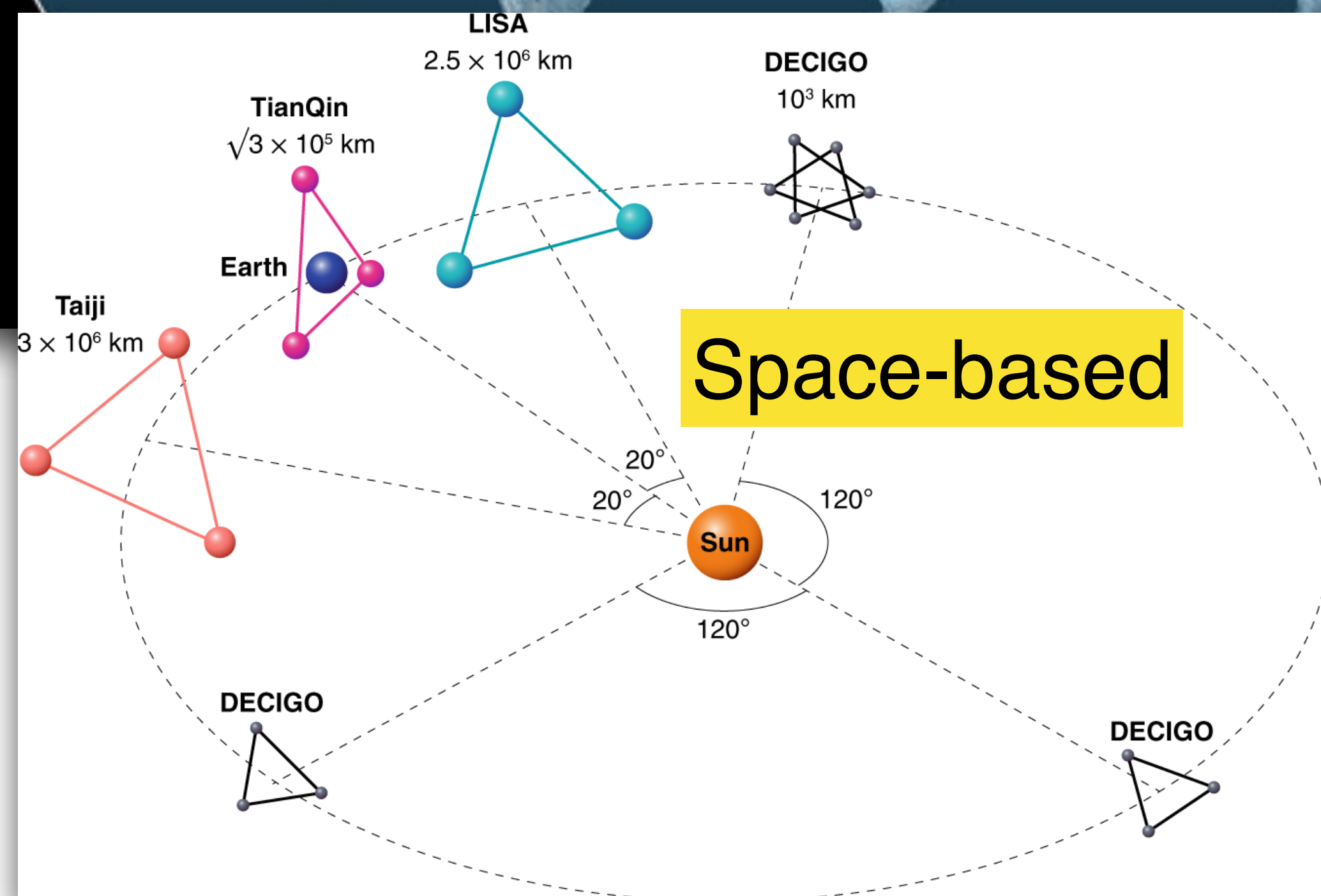
Fu, King, Marsili, Pascoli,
Turner, **YLZ**, arXiv:2209.00021

Undergoing and upcoming GW measurements

Ground-based



Pulsar-Timing Arrays (PTAs)



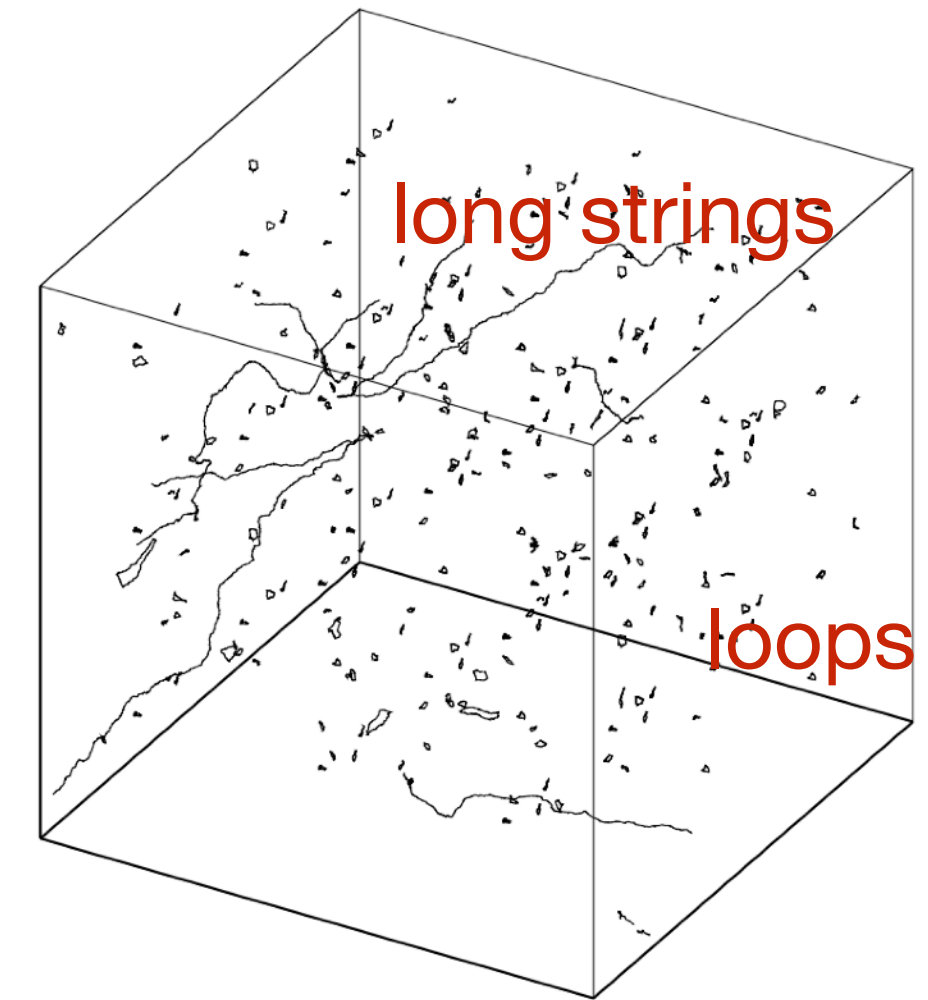
Space-based

Mechanisms of gravitational wave (GW) genesis in GUTs

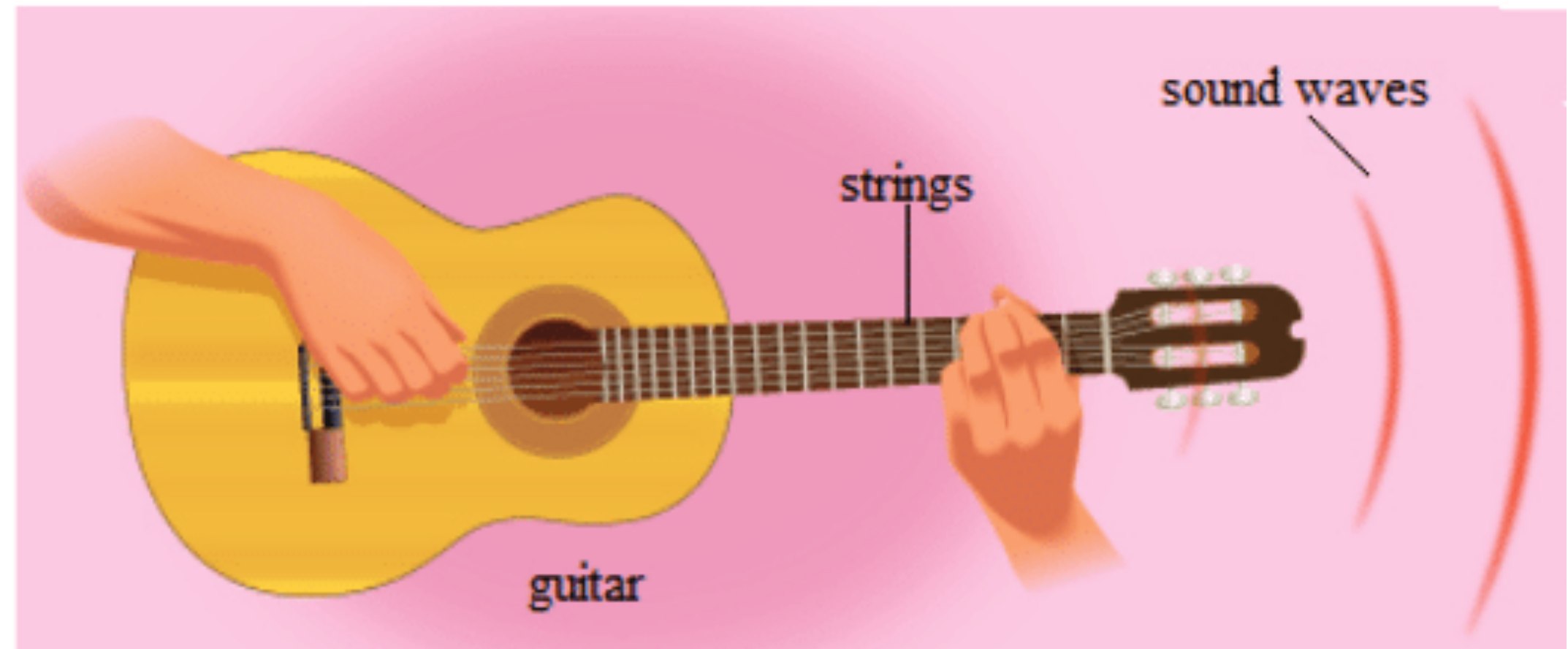
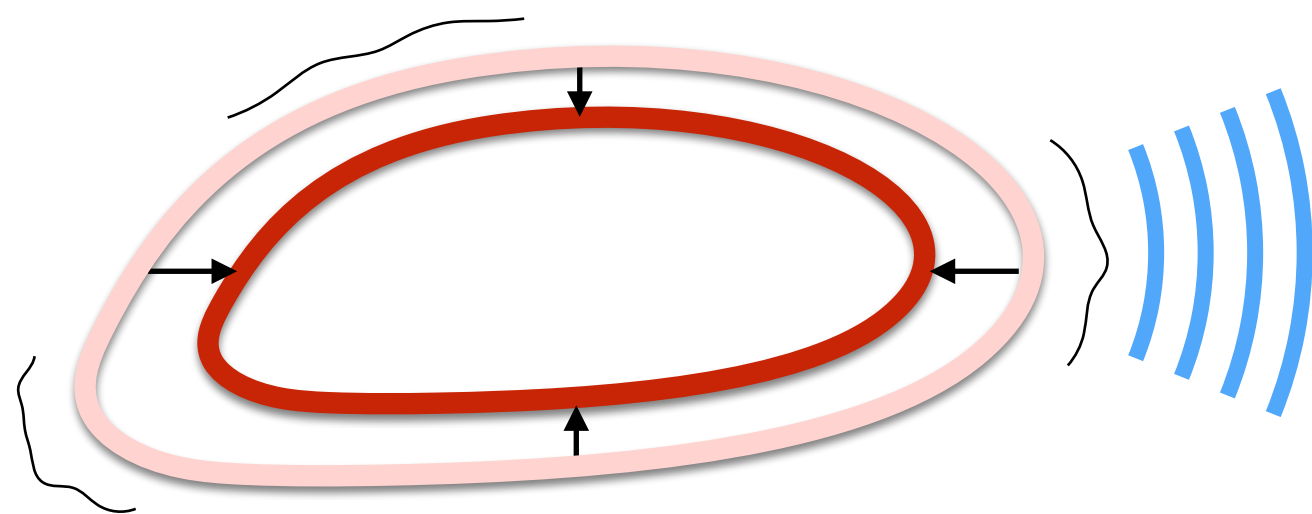
GW via cosmic strings

- Most GUTs include a $U(1)_{B-L}$ symmetry.
- Spontaneous breaking of this $U(1)$ generates cosmic strings.
- Strings intersect and intercommute to form loops and cusps
- Loops oscillates via gravitational radiation

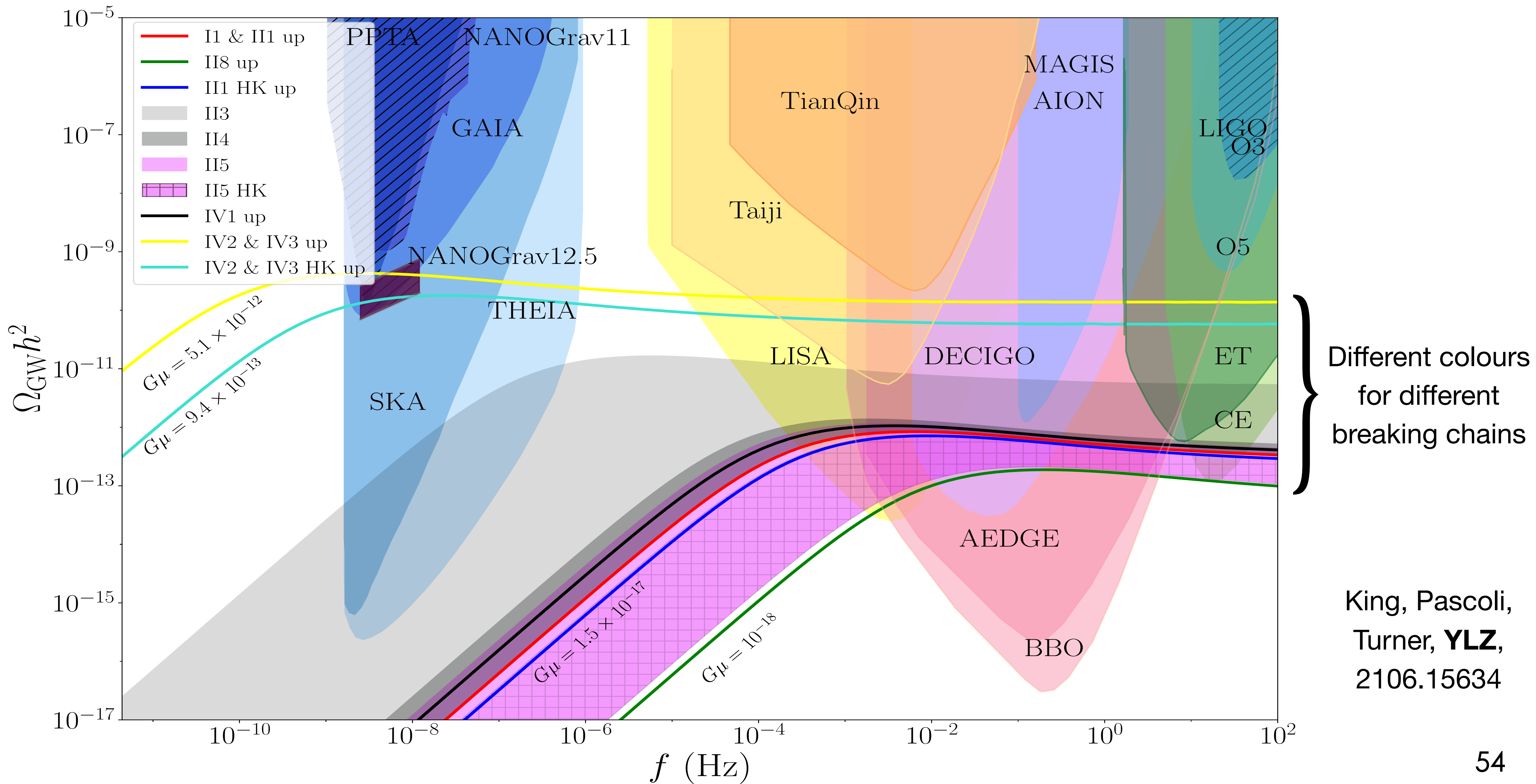
$$\pi_1(U(1)) = \mathbb{Z}$$



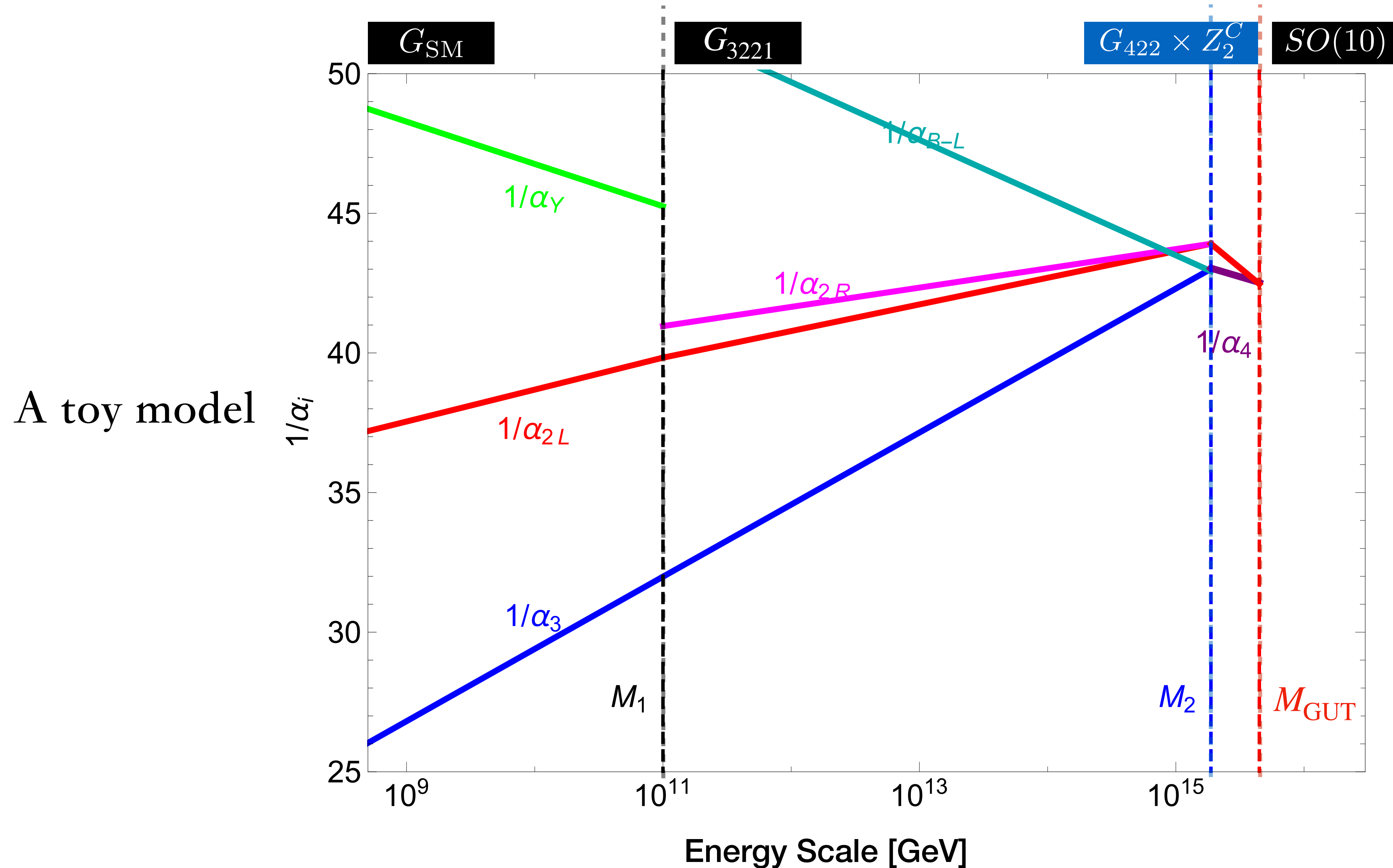
Vanchurin, Olum, Vilenkin, 0511159



Predictions for GW spectrum in SO(10) GUTs



Gauge unification correlates GUT scale with intermediate scales

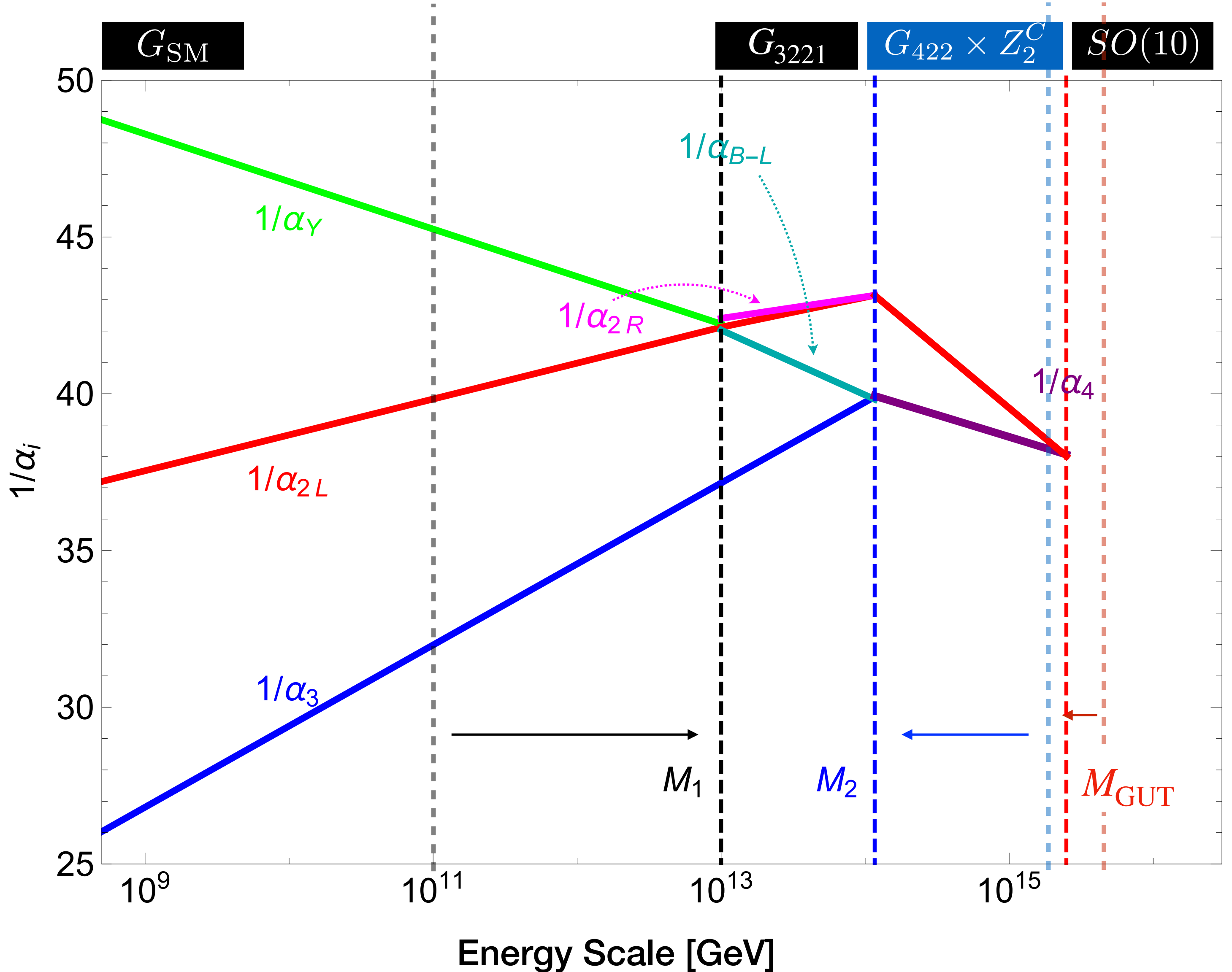


M_i understood as the mass of heavy gauge boson there

No new particle introduced if not necessary

Gauge unification correlates GUT scale with intermediate scales

A toy model

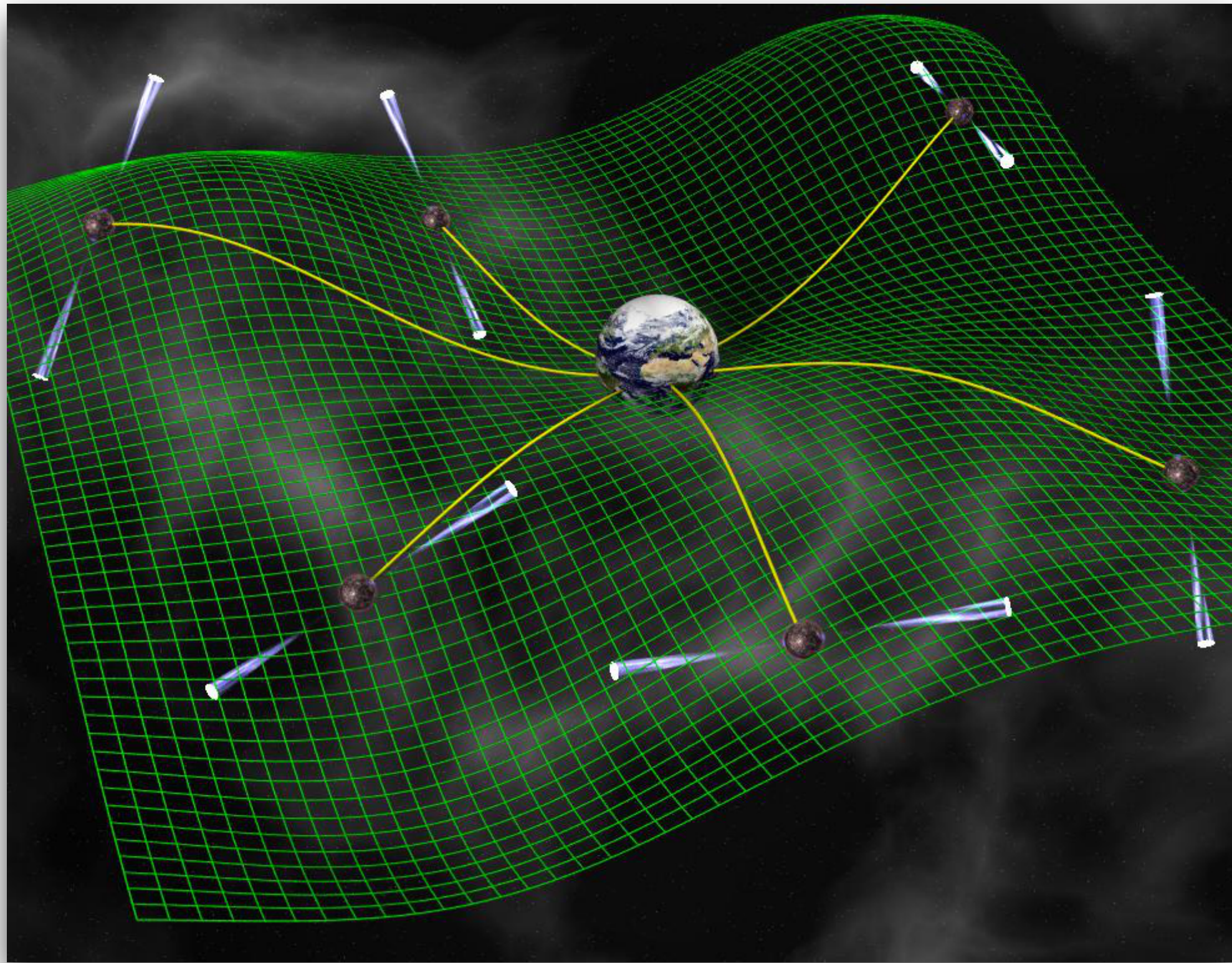


M_i understood as the mass of heavy gauge boson there

No new particle introduced if not necessary

Announcement of PTA measurements this summer

On 28 Jun 2023



The **NANOGrav** 15 yr Data Set: Evidence for a Gravitational-wave Background
2306.16213

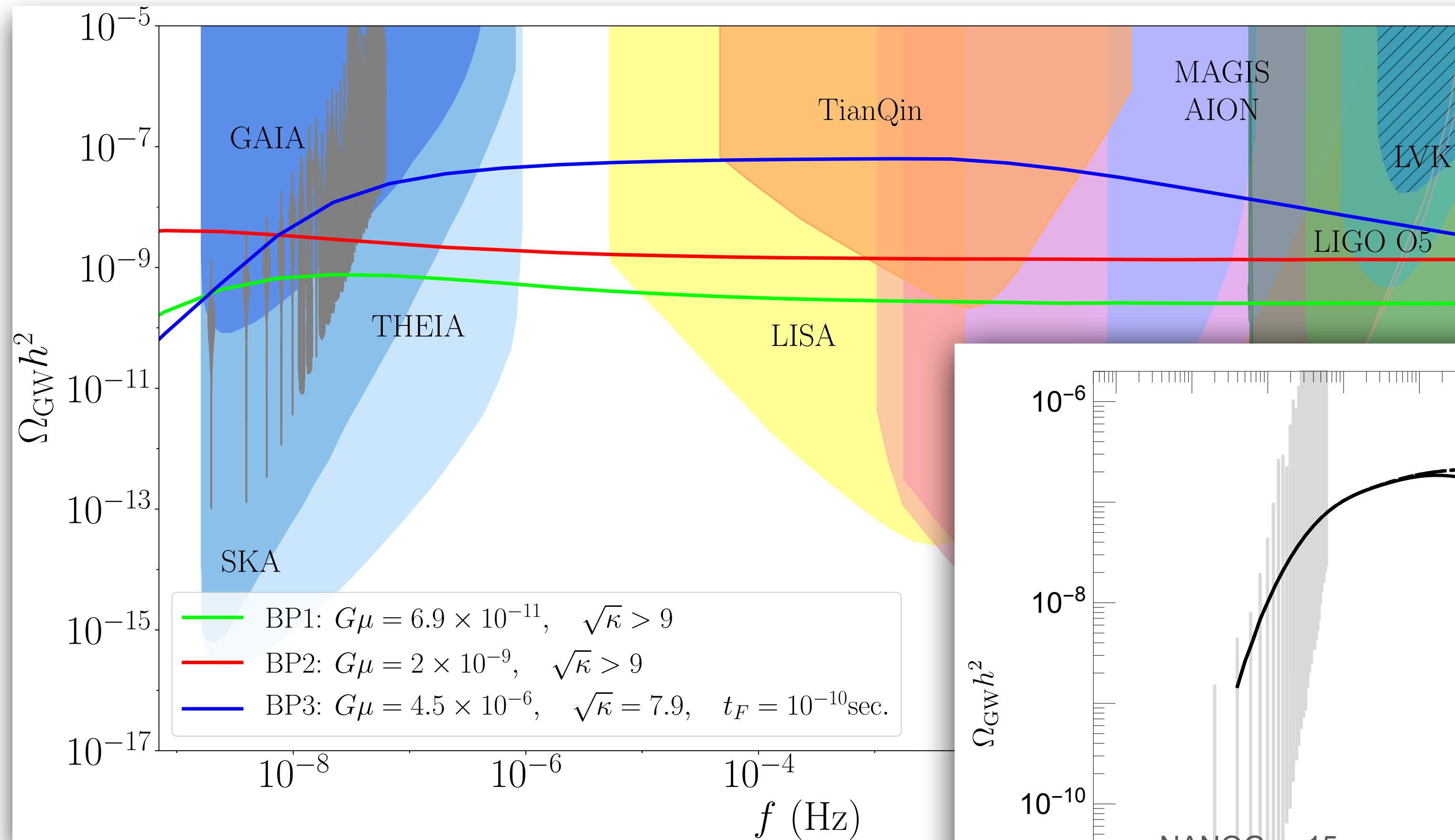
The second data release from the **European Pulsar Timing Array III**. Search for gravitational wave signals
2306.16214

Search for an isotropic gravitational-wave background with the **Parkes Pulsar Timing Array**
2306.16215

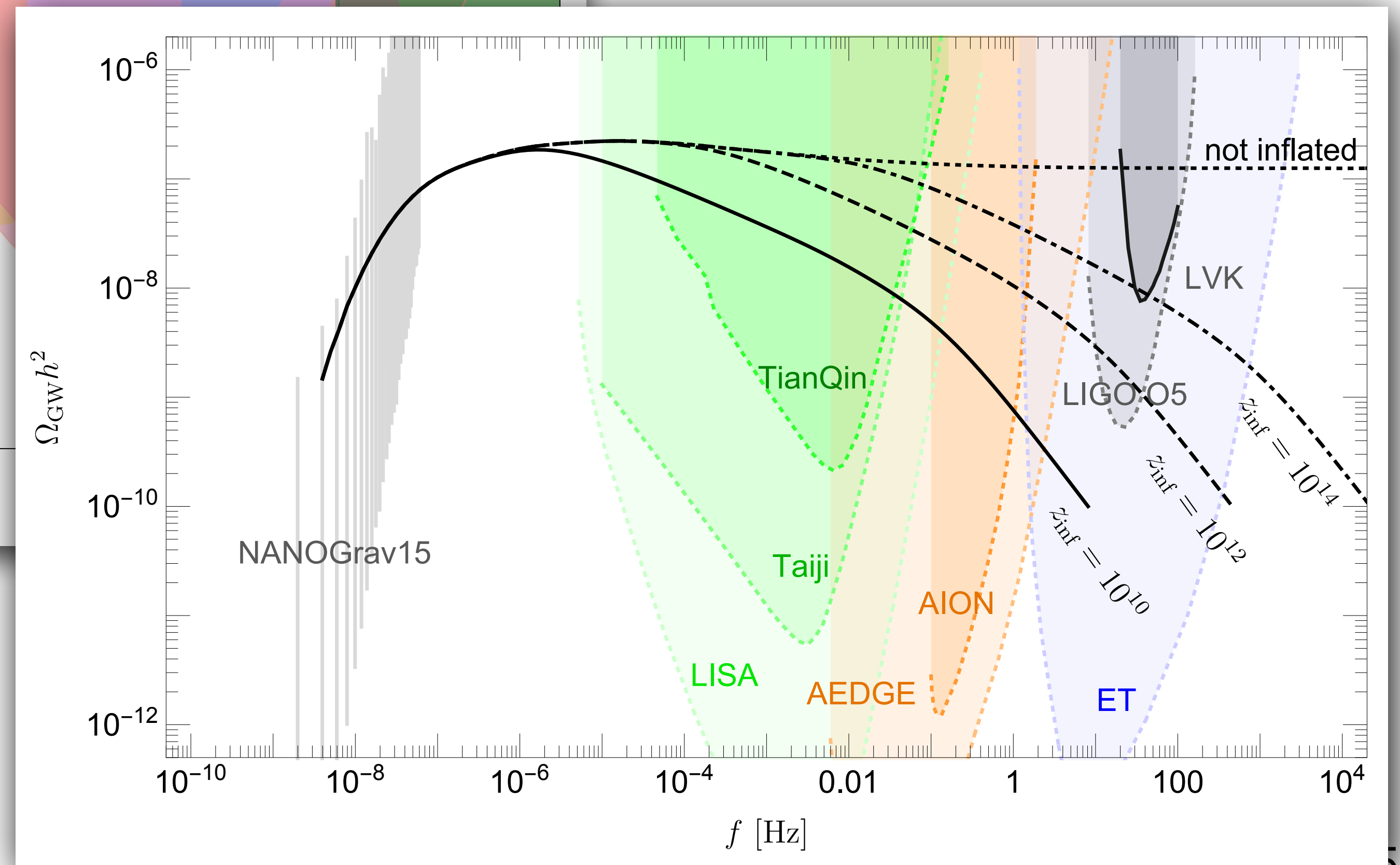
Searching for the nano-Hertz stochastic gravitational wave background with the **Chinese Pulsar Timing Array Data Release I**
2306.16216

If cosmic GW background is observed, then what is the origin?

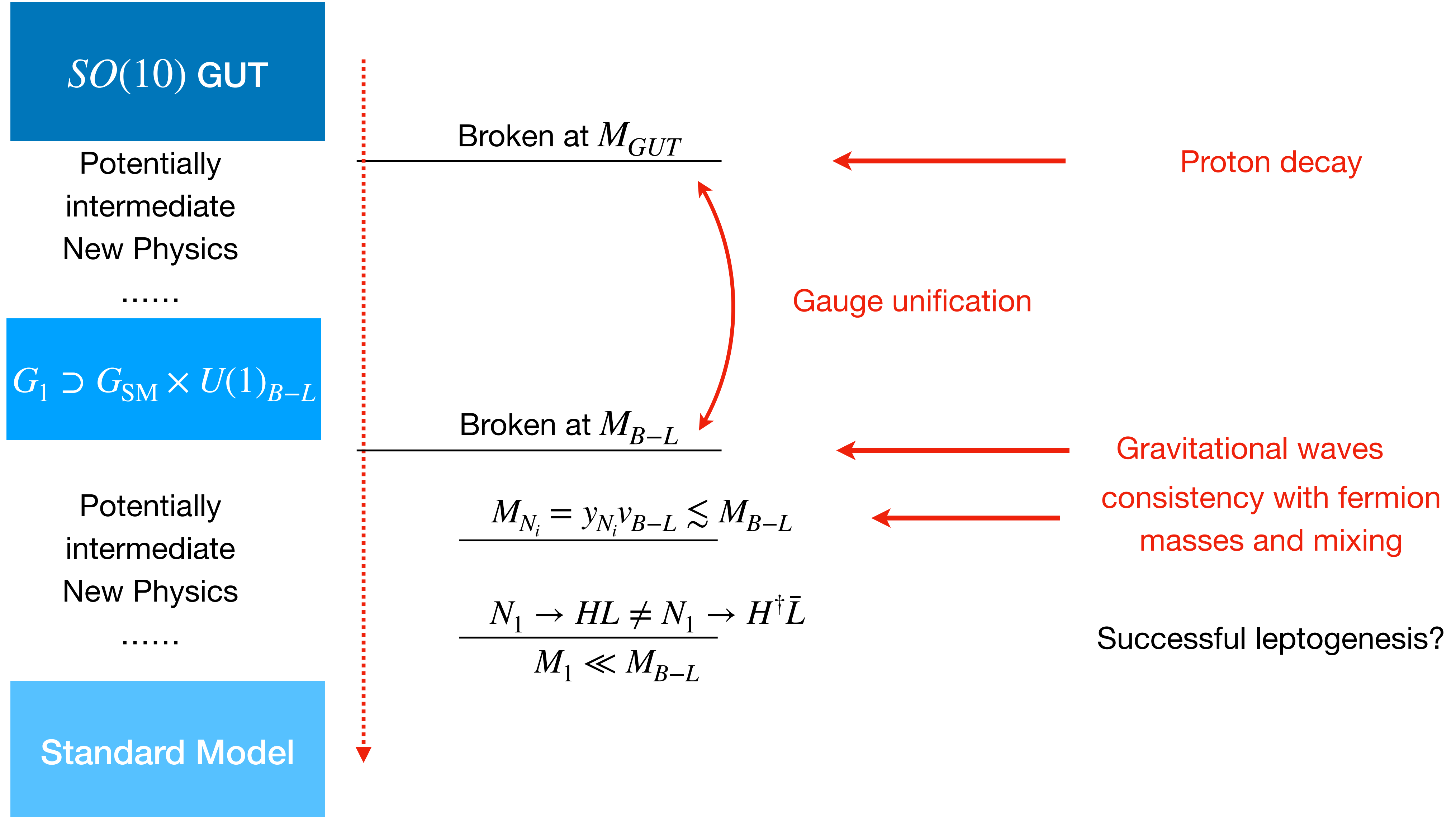
GW from metastable cosmic strings in GUTs, supported by NANOGrav 15



GWs in flipped SU(5)
King, Leontaris, **YLZ**,
2311.11857



Complementary test of GUTs



A wide-angle photograph of Tongjian Lake at dusk. The sky is a gradient of light blue and yellow, indicating the setting sun. In the background, dark, silhouetted mountains rise against the sky. The foreground shows the calm surface of the lake, which perfectly reflects the sky and the lights from a promenade or walkway along the shore. The lights are small, warm-toned dots that create a series of vertical reflections on the water's surface.

Thank you for your listening!

@ 铜鉴湖
Tongjian Lake